

9/19 p1

$$CV = E(P', U^0) - E(P', U') = I'$$

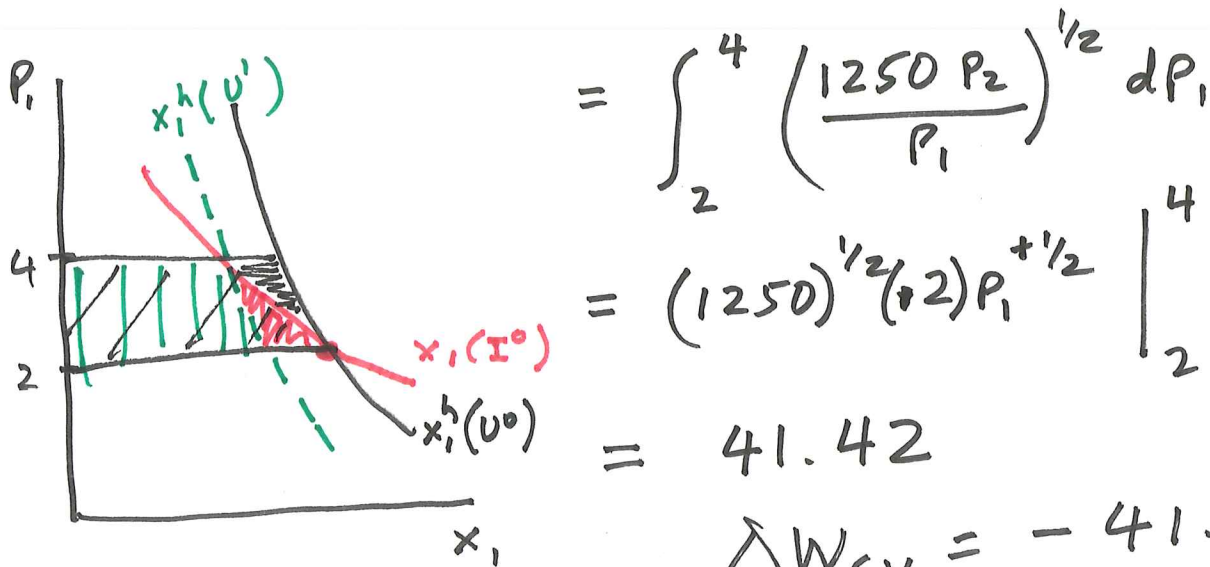
$$\text{If } I_1 = I_0 = E(P^0, U^0)$$

$$\text{then } CV = E(P', U^0) - E(P^0, U^0)$$

In our example,

$$CV = \int_{\mathbb{R}^2}^{\mathbb{R}^4} \frac{\partial E}{\partial p_1} \cdot dp_1$$

$$= \int_{p_1^0}^{p_1^1} x_1^h dp$$



$$= \int_2^4 \left( \frac{1250 p_2}{p_1} \right)^{1/2} dp_1$$

$$= (1250)^{1/2} \left( \frac{1}{2} \right) p_1^{+1/2} \Big|_2^4$$

$$= 41.42$$

$$\Delta W_{CV} = -41.42$$

$$\Delta W_{CS} = -34.66$$

9/19 p2

$$EV = E(P^0, U^1) - E(P^0, U^0)$$

If  $I_0 = I_1$ , then

$$EV = E(P^0, U^1) - E(P^1, U^1)$$

$$= \int_{P_1^1}^{P_1^0} \frac{\partial E}{\partial P_1} \cdot dP_1$$

$$= \int_{P_1^1}^{P_1^0} x_1^h(U^1) \cdot dP_1$$

$$= (625)^{1/2} \cdot 2P_1^{1/2} \Big|_4^2$$

$$= -29.29$$

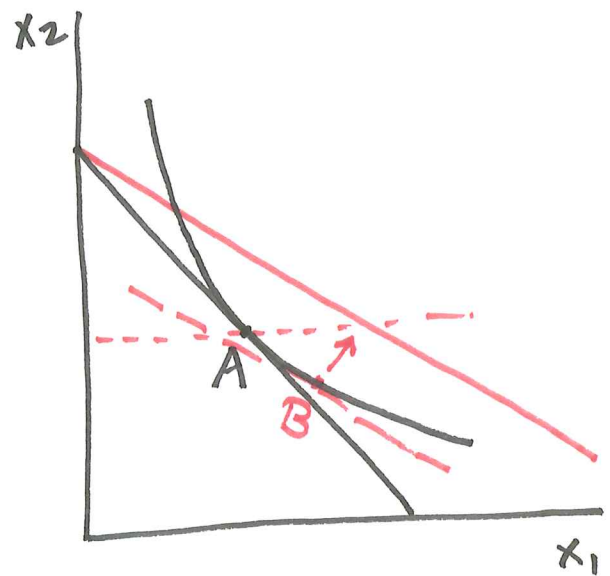
$$x_1 = x_1(P_1, P_2, \underline{I})$$

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Cross-price Effects.

$$\frac{\partial x_2}{\partial P_1} > 0 \quad : \quad \begin{array}{l} \text{gross} \\ \wedge \\ \text{substitutes} \end{array}$$

$$\frac{\partial x_2}{\partial P_1} < 0 \quad : \quad \begin{array}{l} \text{gross} \\ \wedge \\ \text{complements} \end{array}$$



$$\frac{\partial x_1}{\partial P_1} = \frac{\partial x_1^h}{\partial P_1} - x_1^h \frac{\partial x_1}{\partial I}$$

$$\frac{\partial x_2}{\partial P_1} = \underbrace{\frac{\partial x_2^h}{\partial P_1}}_{\text{circled}} - \underbrace{x_1^h \frac{\partial x_2}{\partial I}}_{\substack{+ \quad + \\ -}}$$

$$\frac{\partial E}{\partial P_1} = x_1^h \Rightarrow \frac{\partial x_1^h}{\partial P_1} = \frac{\partial^2 E}{\partial P_1^2}$$

$$\frac{\partial E}{\partial P_2} = x_2^h \Rightarrow \frac{\partial x_2^h}{\partial P_1} = \frac{\partial^2 E}{\partial P_1 \partial P_2}$$

$$\frac{\partial x_1}{\partial P_2} = \underbrace{\frac{\partial x_1^h}{\partial P_2}}_{\text{circled}} - x_2^h \frac{\partial x_1}{\partial I}$$

$\frac{\partial^2 E}{\partial P_1 \partial P_2}$  ↓

$$\frac{\partial x_2}{\partial P_1} = \frac{\partial x_2^h}{\partial P_1} - x_1^h \frac{\partial x_2}{\partial I} < 0 \text{ possibly if } x_1^h \text{ large small}$$

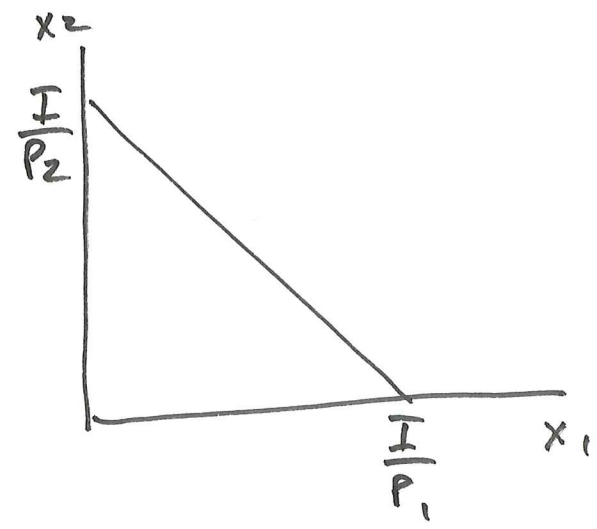
$$\frac{\partial x_1}{\partial P_2} = \frac{\partial x_1^h}{\partial P_2} - x_2^h \frac{\partial x_1}{\partial I} > 0 \text{ possibly if } x_2^h \text{ small}$$

Net Substitutes :  $\frac{\partial x_2^h}{\partial P_1} > 0$   
 " Complements :  $\frac{\partial x_2^h}{\partial P_1} < 0$

### Homogeneity of Demand Function.

homogeneous of degree zero.

$$x_1(P_1, P_2, I) = x_1\left(\frac{I}{P_1}, \frac{I}{P_2}, I\right)$$



$$x_1 = x_1(p_1, p_2, p_3, \dots, p_n, I)$$

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$$\frac{p_1}{x_1} \frac{\partial x_1}{\partial p_1} + \frac{p_2}{x_1} \frac{\partial x_1}{\partial p_2} + \dots + \frac{p_n}{x_1} \frac{\partial x_1}{\partial p_n} + \frac{I}{x_1} \frac{\partial x_1}{\partial I} = 0$$

$$\epsilon_1 + \epsilon_{12} + \epsilon_{13} + \dots + \epsilon_{1n} + \eta = 0$$

Cobb-Douglas:  $U(x_1, x_2) = x_1^2 x_2^3$

$$x_1^* = \frac{2}{5} \cdot \frac{I}{p_1} = \frac{2}{5} I^{\circ} p_1^{-1} p_2^{\circ}$$

$$\epsilon_1 = \frac{\partial x_1}{\partial p_1} \cdot \frac{p_1}{x_1} = -1$$

$$\eta = 1$$

$$\epsilon_{12} = 0$$

$$\epsilon_1 + \epsilon_{12} + \eta = -1 + 0 + 1 = 0$$

Interpretation of  $\lambda$

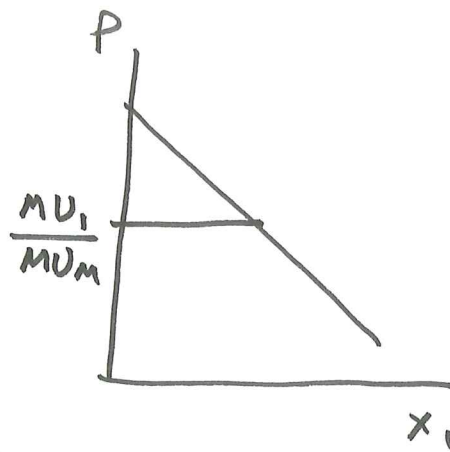
$$\mathcal{L} = U(x_1, x_2) + \lambda [I - p_1 x_1 - p_2 x_2]$$

$$U^*(x_1^*, x_2^*)$$

$$\text{What is } \frac{\partial U^*}{\partial I} = \frac{\partial \mathcal{L}}{\partial I} = \lambda$$

$\lambda$ : marginal utility of income

$$P_i = \frac{MU_i}{MU_M}$$



$$\frac{\partial \mathcal{L}}{\partial x_i} = u_i - \lambda P_i = 0$$

$$P_i = \frac{u_i}{\lambda}$$

## Revealed Preference Approach to Law of Demand.

Weak Axiom of R.P. If a consumer chooses A when B is available, she has revealed a preference for A over B.

