## For full credit, YOU MUST SHOW ALL YOUR WORK. Answer all questions, using diagrams where possible. Each question carries 25 points. Time allowed: 1 hour 20 minutes. Good luck!

1. Tim's preferences over goods $x$ and $y$, the only goods he consumes, are represented by the utility function

$$
U(x, y)=\operatorname{Min}[2 x+y, x+2 y]
$$

where $x$ and $y$ denote the quantities of the two goods he consumes.
(a) Draw Tim's indifference curve for utility level 24.
(b) Calculate the marginal rate of substitution at $(x, y)=(10,7)$.
(c) Calculate Tim's optimal consumption bundle $\left(x^{*}, y^{*}\right)$ when Tim has an income of $I=\$ 24$ and $p_{x}=\$ 1, p_{y}=\$ 1$.
(d) If $p_{y}$ increases to $\$ 6$, while $I$ and $p_{x}$ remain the same as in part (c), what will be Tim's new optimal consumption bundle $\left(x^{* *}, y^{* *}\right)$ ? Calculate how much of the change, if any, from $y^{*}$ to $y^{* *}$ is due to the substitution effect and how much is due to the income effect.
2. Mary's utility function is

$$
U(H, c)=\operatorname{Min}\left[H, \frac{c}{50}\right]
$$

where $H$ is the number of leisure (non-labor) hours she has per day (maximum value, 24) and $c$ is her daily consumption of goods, measured in dollars. She buys goods using all the income she earns from working.
(a) Find Mary's supply curve of labor and draw it in a clearly labeled diagram.
(b) How many hours would Mary work if her wage rate was $\$ 100$ per hour?
(c) How many hours would Mary work if her wage rate was $\$ 50$ per hour?
(d) Suppose Mary wins a lottery that pays her $\$ 200$ per day. Her daily consumption of goods is now $\$ 200$ plus what she earns from working. Find her new supply curve of labor. How many hours would she work if faced with a wage rate of $\$ 50$ per hour?
3. The Widget Corporation's production function is

$$
q(K, L)=\frac{K L}{K+L}
$$

where $K, L$ are the amounts of capital and labor it uses.
(a) What is the shape of a typical isoquant for Widget Corp? Prove your answer.
(b) Find Widget Corp's long run cost function.
(c) Draw Widget Corp's long run cost curve in a clearly labeled diagram.
4. The market for gadgets is perfectly competitive. Currently, the price of gadgets is $\$ 20$ and 10 million gadgets are sold annually.
(a) The government decides to impose an excise tax of $\$ 4$ per gadget. In reporting this, the local newspaper concludes that the government can expect to collect $\$ 40$ million in tax revenue each year from this new tax. Under what circumstances would this conclusion be true?
(b) Suppose the elasticity of demand for gadgets is -1 and the elasticity of supply is 3 . How much tax revenue can the government actually expect to collect per year from this tax?
(c) If, instead of the per-unit excise tax, the government was thinking of imposing a percentage sales tax on the sale of gadgets, what would the percentage tax have to be in order to raise the same amount of revenue as the $\$ 4$ excise tax?

