#### Whole Plant Energy Balance

#### Topics to be covered this week:

- 1. Why it's of concern in ecophysiology
- 2. The Penman-Monteith Equation
- 3. Aerodynamic Coupling and the Omega factor
- 4. Energy balance of leaves vs. canopies

## Whole Plant Energy Balance

- Why does it concern ecophysiologists?
- Transpiration of water is a large part of the plant energy budget – knowing energy budget links to plant water budget.



# Whole Plant Energy Balance

#### Why does it concern ecophysiologists?

•Stomata control transpiration – and assimilation too. Thus energy balance connects with carbon relations. The Penman-Monteith energy balance equation allows us to solve for stomatal conductance.

 $\boldsymbol{\boldsymbol{\mathcal{E}}} = \frac{\{\boldsymbol{\boldsymbol{s}}(\boldsymbol{\boldsymbol{\mathcal{D}}}_{n} - \boldsymbol{\boldsymbol{\mathcal{G}}}) + \boldsymbol{\boldsymbol{\rho}}_{a}\boldsymbol{\boldsymbol{\mathcal{C}}}_{p}\boldsymbol{\boldsymbol{\mathcal{G}}}_{H}\boldsymbol{\boldsymbol{\delta}}\boldsymbol{\boldsymbol{\mathcal{E}}}\}}{\boldsymbol{\boldsymbol{\lambda}}[\boldsymbol{\boldsymbol{s}} + (\boldsymbol{\boldsymbol{\gamma}}\boldsymbol{\boldsymbol{\mathcal{G}}}_{H} / \boldsymbol{\boldsymbol{\mathcal{G}}}_{W})]}$ 



#### Whole Plant Energy Balance

Why does it concern ecophysiologists?

•Leaf or canopy temperature depends on the overall energy balance – and numerous physiological processes depend on temperature.

#### Whole Plant Energy Balance

Also Important for:

Land surface energy balance/climate forcing studies

Hydrological sciences

## Whole Plant Energy Balance

Finally to pique your interest:

Generally, speaking, known incoming energy to terrestrial ecosystems is not balanced by known transformations of this energy: there is a missing energy gap.



# Leaf or canopy energy balance is expressed by the Penman-Monteith equation.

Penman (1948) considered energy balance on water surfaces only, and 'fudge factors' were applied for crop energy balance.

Later, Penman (1953) and Monteith (1965) explicitly included latent heat transfer from leaves and canopies.

Penman HL (1948) Natural evaporation from open water, bare soil and grass. Proc. Royal Soc. London A, 193: 120-145. Penman HL (1953) The physical basis of irrigation control. Report of the 13th Intl. Hort. Congress. 2: 913-914.

Monteith JL (1965) Evaporation and Environment. Symposia of the Soc. Exp. Bio. 19:205-234.





#### Note:

Rn is the amount of energy available to heat up leaves, evaporate water, etc., but its important to realize that plants control Rn through stomata and latent heat (transpirations) – so Rn is not exclusively a 'meteorological' variable.



#### Can also piece together net radiation from longwave and shortwave components – thermopile detectors



(longwave) W/m2



 $R_n = C + \lambda E + M + S$ 

C is sensible heat loss from leaf/canopy Sensible means 'measurable' in terms of thermometry.

C is given by:

 $C = g_H (\rho c_p) (T_{leaf} - T_{air})$ 

Where  $g_H$  is conductance to heat transfer (m s<sup>-1</sup>)  $\rho$  is density of air (kg m<sup>-3</sup>) (1.2 kg/m3 @ 25 deg C)  $C_p$  is specific heat capacity (J kg<sup>-1</sup> K<sup>-1</sup> =1012 for air)

Units:  $(m \, s^{-1}) (kg \, m^{-3}) (J \, kg^{-1} \, K^{-1}) (K) = J \, s^{-1} \, m^{-2} = Watts \, m^{-2}$ 

 $R_n = C + \lambda E + M + S$  $\lambda E = \lambda g_w \Delta C_w$ 

Where  $\lambda$  is latent heat of water (2.4-2.5 MJ kg<sup>-1</sup> for 0-45 °C) g<sub>w</sub> is leaf/canopy conductance to water (m s<sup>-1</sup>)  $\Delta$ C is water vapor concentration difference (kg m<sup>-3</sup>)

Units: (J kg<sup>-1</sup>) (m s<sup>-1</sup>) (kg m<sup>-3</sup>) = J s<sup>-1</sup> m<sup>-2</sup> = W m<sup>-2</sup>

# $R_n = C + \lambda E + M + S$

And, 
$$\Delta C_{W} = (\rho_{a}M_{W}/M_{A})\Delta e/(P-e)$$

Where  $\rho_a$  is density of air (kg m<sup>-3</sup>);  $M_W$  is molecular weight of water (18 g mol<sup>-1</sup>)  $M_A$  is the effective molecular weight of dry air (~29 g mol<sup>-1</sup>) So  $M_W/M_A = 0.622$ P is atmospheric pressure (~101.3 kPa) And  $\Delta e$  is vapor pressure difference (kPa) Units for  $\Delta C_W$ : (kg m<sup>-3</sup>) (g mol<sup>-1</sup>)/(g mol<sup>-1</sup>) (kPa/kPa) = kg m<sup>-3</sup> Units for  $\lambda E$  : (J/kg)(m/s)(kg/m3) = W/m2

$$\begin{split} R_n &= C + \lambda E + M + S \\ Thus, \lambda E &= \lambda \; g_W \; \Delta C_W \; becomes \\ \lambda E &= \lambda \; g_W \; (\rho_a M_W / M_A) \Delta e / (P-e) \\ & but \; (P-e) \; \sim P \; since \; P >> e \\ So, \\ \lambda E &\approx \lambda \; g_W \; (\rho_a M_W / M_A) \Delta e / P, \; \; OR, \\ \lambda E &\approx \lambda \; g_W (\rho_a \; 0.622) (e_{s(TI)} - e_a) / P \end{split}$$



Measurement of  $\lambda E$  at the leaf scale – leaf cuvette/infrared gas analyzers.



$$R_n = C + \lambda E + M + S$$

M is energy stored in chemical bonds, dominated by photosynthesis and respiration, and usually < 5% of Rn. Thus, it can for most purposes be ignored in terms of the overall plant energy balance.

 $R_n = C + \lambda E + M + S$ S is energy used for heating leaves, wood, soil. Generally small except for massive stems, forests, leaves, cacti. Here we will ignore it by assuming either small plants or steady state conditions.



#### Recap so far:

We've described each of the terms in:

$$R_n = C + \lambda E + M + S$$

And by ignoring the last two terms we have

 $R_n = C + \lambda E$ 

$$R_n = g_H(\rho c_p)(T_{leaf} - T_{air}) + \lambda g_W(\rho_a 0.622)(e_{s(TI)} - e_a)/P$$

Doesn't look very nice!

The main problem with

$$R_n = g_H(\rho c_p)(T_{leaf} - T_{air}) + \lambda g_W(\rho_a 0.622)(e_{s(TI)} - e_a)/P$$

Is that it requires knowledge of  $T_{leaf}$  (or  $T_{canopy}$ ) – difficult to obtain.

If we could somehow eliminate  ${\rm T}_{\rm leaf}$  from the equation life would be much easier.

This is what Penman did.



 $\mathsf{R}_{\mathsf{n}} = \mathsf{g}_{\mathsf{H}}(\rho \; c_{\mathsf{p}})(\mathsf{T}_{\mathsf{leaf}} - \mathsf{T}_{\mathsf{air}}) + \lambda \mathsf{g}_{\mathsf{W}}(\rho_{\mathsf{a}} \mathbf{0.622})(\mathsf{e}_{\mathsf{s(TI)}} - \mathsf{e}_{\mathsf{a}})/\mathsf{P}$ 

 $(e_{s(TI)}-e_a) = (e_{s,Ta}-e_a) - de_s/dT *(T_a-T_{leaf})$ 

(from last page,) = VPD + s(T<sub>leaf</sub> - T<sub>air</sub>)

VPD is just a F(Tair, Rel. Humidity) – easy to measure. S is simply a property of water vapor and can be just read off the chart.

But we still have  $(T_{leaf} - T_{air})$  – which we still need to 'get rid of'.

 $R_n = g_H(\rho_a c_p)(T_{leaf} - T_{air}) + \lambda g_W(\rho_a 0.622)(e_{s(TI)} - e_a)/P$ 

Fortunately, we now have two terms in the above equation in  $T_{leaf} - T_{air}$ . The blue term (C) AND the yellow term ( $\lambda E$ ).

For the  $\lambda E$  term we can replace  $T_{\text{leaf}}$  –  $T_{\text{air}}$  in terms of C:

 $\lambda E = \lambda g_W (0.622 \rho_a/P) [VPD + (S C/g_H \rho_a c_p)]$ 

=  $\lambda g_W(0.622 \rho_a/P)[VPD + (S (Rn - \lambda E) / g_H \rho_a c_p)]$ 

Gather terms and solve for E:

Finally, going back to the overall energy balance equation:  $C = R_n - \lambda E$ 

We obtain

$$E = \frac{SR_n + \rho_a c_p g_H VPD}{\lambda [S + (Pc_p / 0.622\lambda)g_H / g_W]}$$

This, my friends, is the Penman-Monteith equation. Note: no  $T_{leaf}$ 

Let's clean up  

$$E = \frac{sR_n + \rho_a c_p g_H VPD}{\lambda [s + (Pc_p / 0.622\lambda)g_H / g_W]}$$

a bit:

Let  $\gamma = P c_p / 0.622 \lambda$  (= 65-68 Pa/K from 0-50 °C) And let *D* stand for VPD. **Then**,

$$E = \frac{sR_n + \rho_a c_p g_H D}{\lambda [s + \gamma (g_H / g_W)]}$$

$$E = \frac{sR_n + \rho_a c_p g_H D}{\lambda [s + \gamma (g_H / g_W)]}$$

Looks better, but is still limited in application:

 $R_n$  depends on  $T_{leaf/canopy}$ , and one would need a net radiometer for each and every vegetation plot to use this equation.

But there is another way around this...



Clearly we cant just replace  $R_n$  with  $R_{ni}$  because  $R_{ni} = R_n + \varepsilon \sigma (T_s^{4} - T_a^{4})$  (I'm using  $T_s = T_{ieaf}$  or  $T_{canopy}$  from now on) And this is still problematic because of  $T_s$ . But we can use a trick that ultimately gets  $T_s$  out of the way: We substitute  $T_s = T_a + \Delta T$  above to get  $R_{ni} = R_n + \varepsilon \sigma [(T_a + \Delta T)^4 - T_a^4]$   $= R_n + \varepsilon \sigma [T_a^4 + 4T_a^3 \Delta T + 6T_a^2 (\Delta T)^2 + 4T_a (\Delta T)^3 + (\Delta T)^4 - T_a^4]$  $= R_n + \varepsilon \sigma [4T_a^3 \Delta T + 6X_a (\Delta T)^2 + 4T_a (\Delta T)^3 + (\Delta T)^4 - T_a^4]$ 

And since  $T_a >> \Delta T$ , we can drop the higher order  $\Delta T$  terms

So, R<sub>ni</sub> ≅ R<sub>n</sub> + 4εσT<sub>a</sub>³(T<sub>s</sub>-T<sub>a</sub>)

This second term can also be expressed as  $(4\epsilon\sigma T_a{}^3/\rho c_p) \rho c_p(T_s-T_a)$ 

And now it looks very much like the term

 $C = g_{H} \rho c_{p} (T_{s} - T_{a})$ 

for sensible heat flux.

Taking this analogy further, we can define a 'radiative conductance' as:

$$g_R = 4\varepsilon\sigma T_a^3/\rho c_p$$

So that  $R_n \cong R_{ni} - g_R \rho c_p (T_s - T_a)$ 

We still have  $T_s$  though (recall that's what we're trying to get rid of)!

We can 'bundle'  $g_R$  in with  $g_H$  since they operate in parallel and both are associated with  $T_s$ - $T_a$ . So  $g_{HR} = g_H + g_R$ 

Thus, we can take the original PM equation:

$$E = \frac{sR_n + \rho_a c_p g_H D}{\lambda [s + \gamma (g_H / g_W)]}$$

And replace it with:

$$E = \frac{sR_{ni} + \rho_a c_p g_{RH} D}{\lambda [s + \gamma (g_{RH} / g_W)]}$$
 Done!

So why is this better??  $E = \frac{sR_{ni} + \rho_a c_p g_{RH} D}{\lambda [s + \gamma (g_{RH} / g_W)]}$ The g<sub>H</sub> part of g<sub>RH</sub> is a f(windspeed, leaf shape, or canopy geometry) – can be modeled or measured independently R<sub>ni</sub> can be estimated simply from Ta D is easily computed from RH and Ta

 $g_{\rm W}$  can be modeled or measured with gas exchange (scaling issue...), or the whole equation can be 'inverted' to solve for  $g_{\rm W}$  instead.

Now lets build upon the PM Energy Balance Equation:

Aerodynamic Coupling and the Omega factor

Example of wind chill

Aerodynamic coupling fundamentally describes how much physiological control plants have over water loss (stomata) versus how much structural (boundary layer) control plants have over water loss

This is important because it allows us to assess the importance of stomata vs. canopy structure to water and energy budgets in a broader context of plant interaction with the environment.

It can roughly be thought of as 'degree of ventilation'. Well ventilated leaves or canopies ('fractally' shaped) are highly 'coupled' to the external atmospheric envt, while poorly ventilated canopies (umbrella shaped) are 'decoupled' from the atmosphere

Well (poorly) coupled leaves/plants conduct/convect heat away efficiently (inefficiently), and therefore maintain foliage temperatures close to (not close to) bulk air temperature.











The relative values of  $g_H$  (or  $g_{RH}$ ) and  $g_W$  are at the heart of the concept of aerodynamic coupling.

$$E = \frac{sR_n + \rho_a c_p g_H D}{\lambda [s + \gamma (g_H / g_W)]}$$

We need to step back and deconstruct  $g_H$  (or  $g_{RH}$ ) and  $g_W$  first to see where the stomatal vs. boundary layer terms fall out. For simplicity, we will consider the above version of the PM equation for this purpose.



So 
$$g_H/g_W = g_a \times [(1/g_a) + (1/g_s)] = 1 + g_a/g_s$$
  
And thus  $E = \frac{sR_n + \rho_a c_p g_H D}{\lambda [s + \gamma (g_H / g_W)]}$   
becomes  
 $E = \frac{sR_n + \rho_a c_p g_a D}{\lambda [s + \gamma (1 + g_a / g_s)]}$ 

Now we've more explicitly separated out the boundary layer vs. stomatal components and can consider their relative controls on E

$$E = \frac{sR_n + \rho_a c_p g_a \mathcal{D}^0}{\lambda [s + \gamma (1 + g_a / g_s)]}$$

If  $g_a << g_s$  (or  $g_a \rightarrow 0$ ) the above equation reduces to

$$E = \frac{sR_n}{\lambda[s+\gamma]}$$

If  $g_a << g_s$  (or  $g_a \rightarrow 0$ ) transpiration is controlled only by net radiation, and is independent (or decoupled) from bulk atmospheric humidity (VPD)

$$E_{equilibrium} = \frac{sR_n}{\lambda[s+\gamma]}$$

Because  $g_a$  and not  $g_s$  is 'bottleneck' in overall E transport, it simply does not matter what stomates are doing!

We call this E<sub>equilibrium</sub> because in this case, stomata may close or open, but if they do, they will change leaf-air vapor pressure difference in such a way to maintain a constant E



If  $g_a >> g_s$  (or  $g_a ->$  infinity) transpiration is controlled strongly by stomata, and is directly controlled by – or coupled to atmospheric humidity (VPD)

$$E_{imposed} = \frac{\rho_a c_p g_s D}{\lambda \gamma}$$

Because  $g_s$  and not  $g_a$  is the 'bottleneck' in overall E transport, stomates control it all

(We call this E<sub>imposed</sub> because ambient D is 'imposed' right at foliage surface with no intervening boundary layer of any significance)





In general, all leaves, plants, canopies, will fall somewhere in between the two extremes of  $g_a$  and  $g_s$  described previously.

If we define  $\Omega = (s/\gamma + 1)/(s/\gamma + 1 + g_a/g_s)$ Which we can see has a range of 0-1

Then we can express E from the PM equation as

 $E_{total} = \Omega E_{eq} + (1 - \Omega) E_{imp}$  (proof not shown)

The utility of  $\Omega$  is that it provides us with a very easy index of stomatal vs. enviromental control over transpiration

If  $g_a >> g_s$  then  $\Omega = (s/\gamma + 1)/(s/\gamma + 1 + g_a/g_s) = 0$  and coupling is strong

If  $g_a \ll g_s$  then  $\Omega = (s/\gamma + 1)/(s/\gamma + 1 + g_a/g_s) = 1$  and coupling is weak

If  $g_a \sim g_s$  then  $\Omega = (s/\gamma + 1)/(s/\gamma + 1 + g_a/g_s) \sim 0.5$ and coupling is intermediary

It can be shown (see Jarvis & McNaughton 1986) that  $\Omega$  may be equivalently expressed as

 $\Omega = 1 - (dE/E) / (dg_s/g_s)$ 

That is,  $\Omega$  is how much fractional change in E occurs with a fractional change in  $g_s$ . If a change in  $g_s$  makes zero difference to E, then stomates don't matter, boundary layers dominate, and  $\Omega = 1$ .

Here are some representative  $\Omega$  values for leaves and crops. The boundary layers and reference location for D may be very different between leaf and canopy scales <sup>118 Dergy balance and responsible</sup>

Single leaves	Leaf width (mm)	Ω	(dE/E)/(dg,/g
Rhubarb	500	0.8	0.2
Cucumber	250	0.7	0.3
Bean	60	0.5	0.5
Onion	8	0.3	0.7
Asparagus	1	0.1	0.9
Open field crops	Crop height (m)	Ω	(dE/E)/(dg,/g,
Grass	0.1	0.9	0.1
Strawberry	0.2	0.85	0.15
Tomato	0.4	0.7	0.3
Wheat	1.0	0.5	0.5
Raspberry	1.5	0.4	0.6
Citrus orchard	5.0	0.3	0.7
Forest	30	0.1	0.9
Other situations		Ω	(dE/E)/(dg,/g,)
Uncontrolled glasshouse		09-10	0.01
Lysimeters or 1 m <sup>9</sup> plots		< 0.1	> 0.0
Controlled environment chamber		< 0.1	> 0.9





Two critical features of this formulation are:

- 1. It explicitly carries with it biological control of stomata  $(g_w)$ .
- 2. It can be computed without direct knowledge of leaf or canopy temperature.

For these reasons, the PM equation is the most widely used basic energy balance formulation for vegetated surfaces.