

## Sequence Divergence & The Molecular "Clock"

### Sequence Divergence

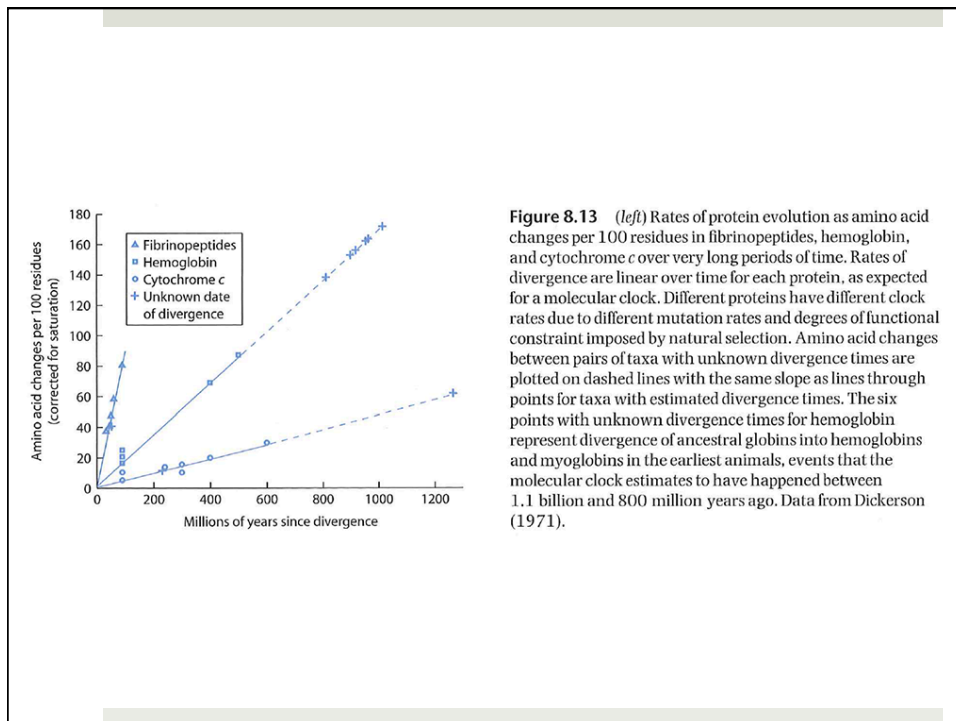
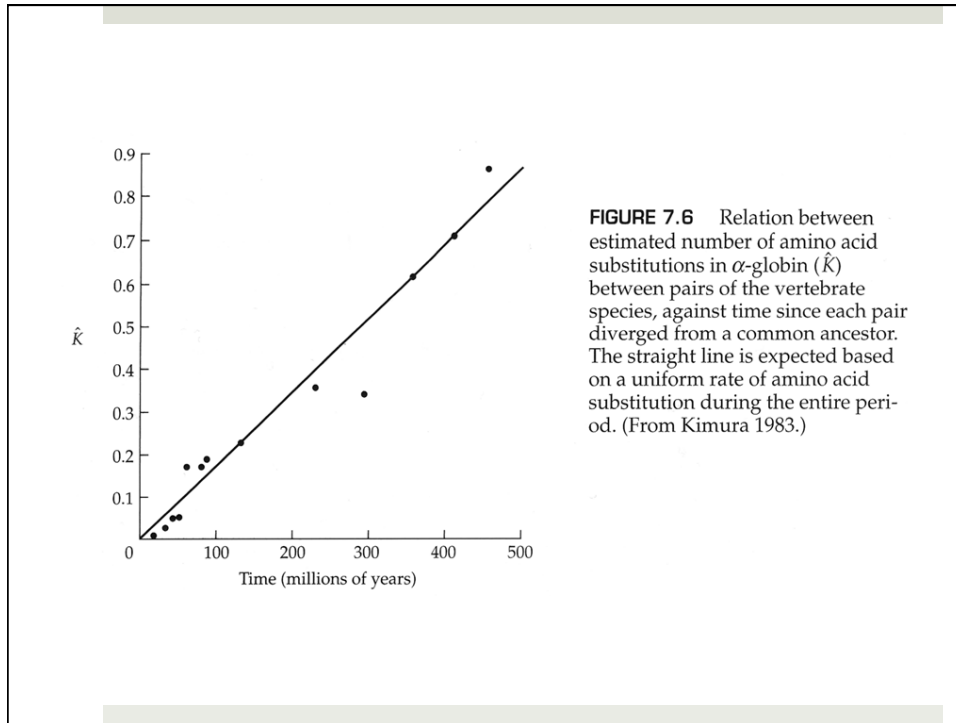
- ❖ simple genetic distance,  $d$  = the proportion of sites that differ between two aligned, homologous sequences
- ❖ given a constant mutation/substitution rate,  $d$  should provide a measure of time since divergence
  - ❖ but this is complicated by **multiple hits** (homoplasy)
  - ❖ corrected distance metrics account for the fact that there are **not** an infinite number of sites in a sequence

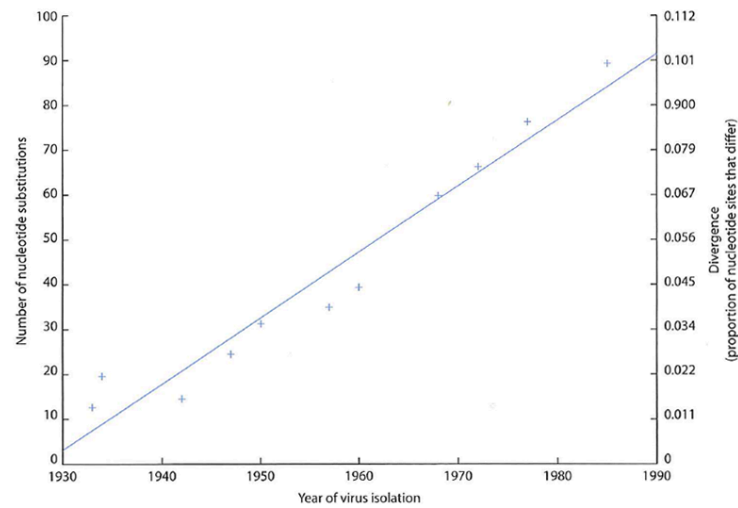
## Expected sequence divergence

- ❖ for neutral polymorphisms, substitution rate = mutation rate
- ❖ thus, for two diverging lineages...  $k = 2T\mu$ 
  - ❖ where  $k$  = the number of substitutions observed between two species and  $T$  is the time since divergence
  - ❖ note that  $T$  and  $\mu$  can be measured either in years or generations
- ❖ solving for  $T$ ...  $T = \frac{k}{2\mu}$ 
  - ❖ note that  $2\mu$  is often expressed as the "rate of sequence divergence" (i.e., twice the per lineage rate)

## Rates and Dates: Divergence Time Estimates

- ❖ requires calibration with fossil or geological events
- ❖ typically assumes a "molecular clock"
  - ❖ Zuckerkandl & Pauling (1962)
- ❖ but new methods allow a relaxation of the molecular clock assumption

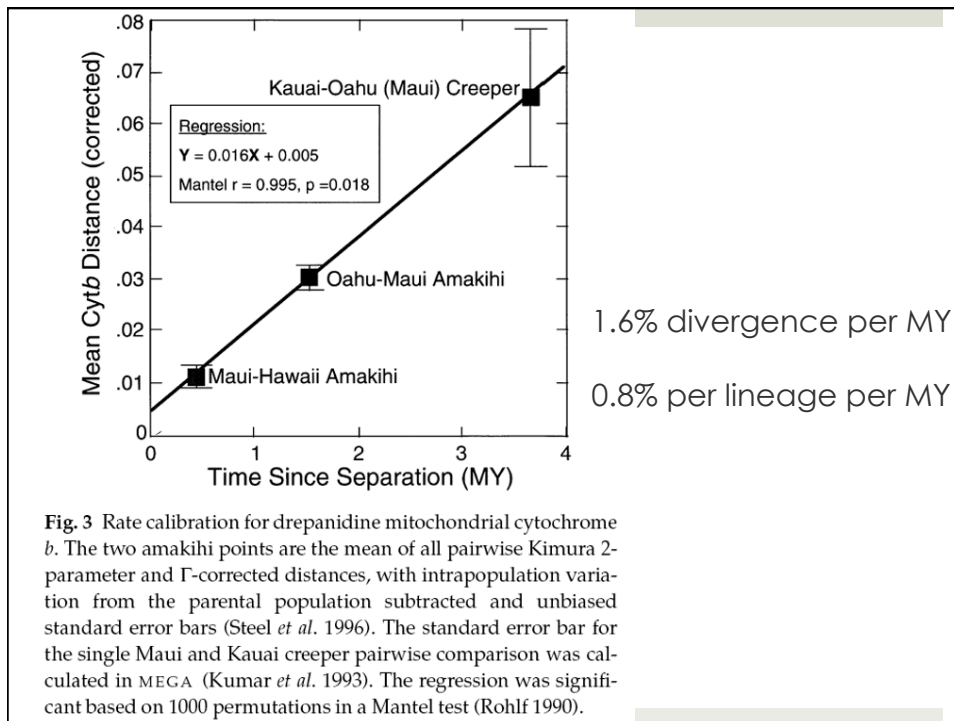
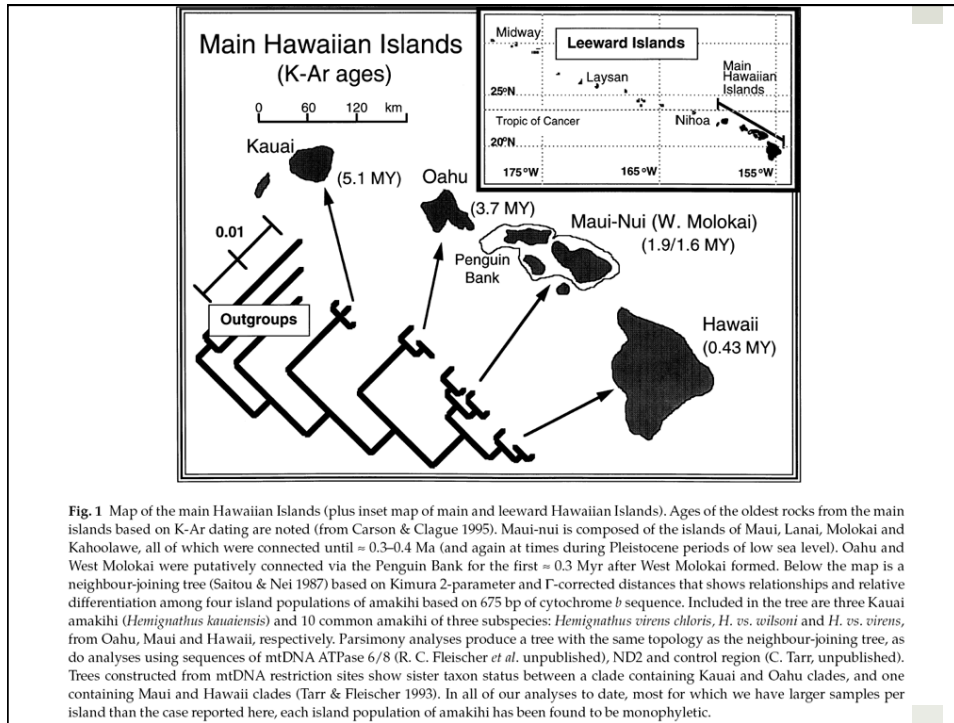


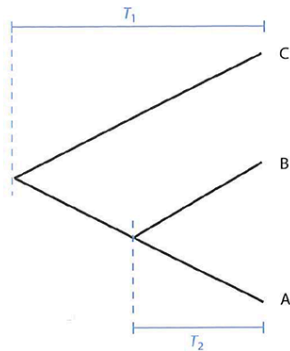


**Figure 8.12** Rates of nucleotide change in the NS gene that codes for “nonstructural” proteins based on 11 human influenza A virus samples isolated between 1933 and 1985. The number of years since isolation and DNA sequence divergence from an inferred common ancestor are positively correlated. The pattern of increasing substitutions as time since divergence increases is expected under the molecular clock hypothesis. The observed rate of substitution was approximately  $1.9 \times 10^{-3}$  substitutions per nucleotide site per year, a very high rate compared to most genes in eukaryotes. The line is a least-squares fit. Data from Buonagurio et al. (1986).

Fleischer *et al.* 1998. Evolution on a volcanic conveyor belt: using phylogeographic reconstructions and K-Ar based ages of the Hawaiian Islands to estimate molecular evolutionary rates. *Mol. Ecol.* 7:533-545.



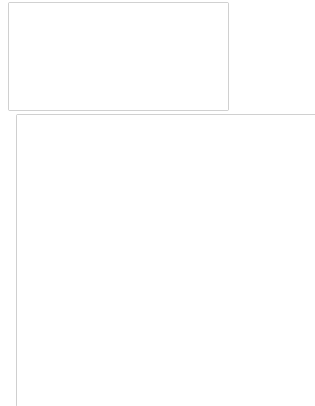




**Figure 8.14** A schematic phylogenetic tree that can be used to date divergence events under the assumption of a constant rate of divergence over time or a molecular clock.  $T_1$  is the time in the past when species C and the ancestor of species A and B diverged.  $T_2$  is the time in the past when species A and B diverged. If either  $T_1$  or  $T_2$  are known, the rate of molecular evolution per unit of time can be estimated from observed sequence divergences. This rate of divergence can then be used to estimate the unknown amount of time that elapsed during other divergences.

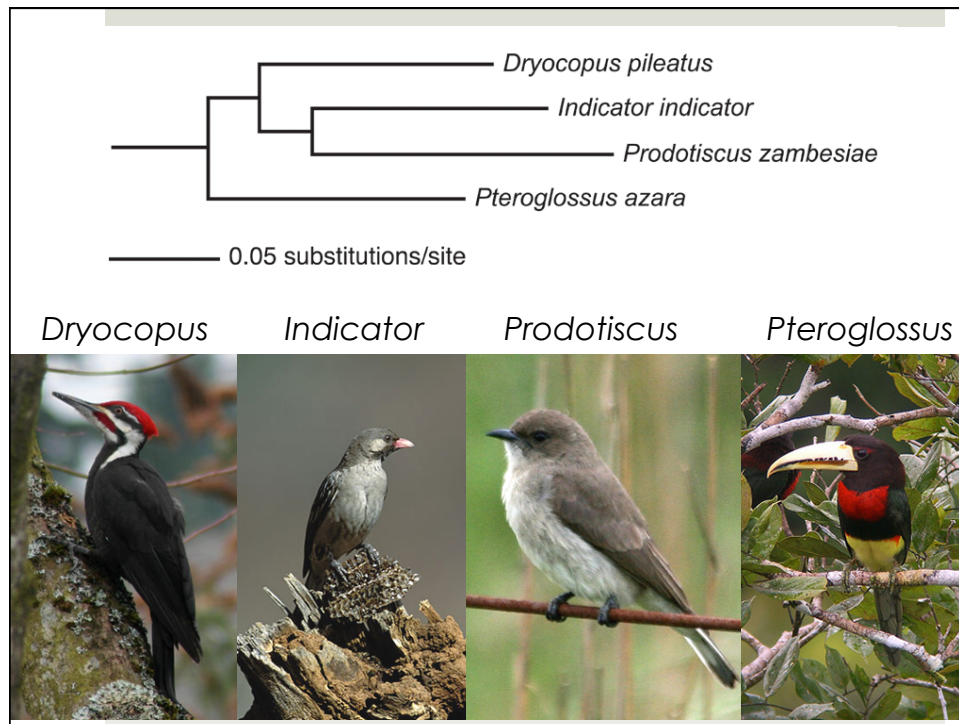
suppose  $T_1$  is known...

$$\mu = \frac{1}{2} \left( \frac{K_{AC}}{2T_1} + \frac{K_{BC}}{2T_1} \right)$$



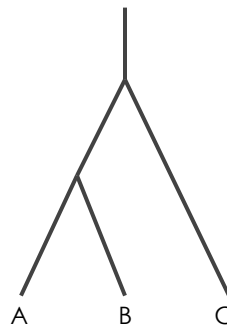
## Problems with dating...

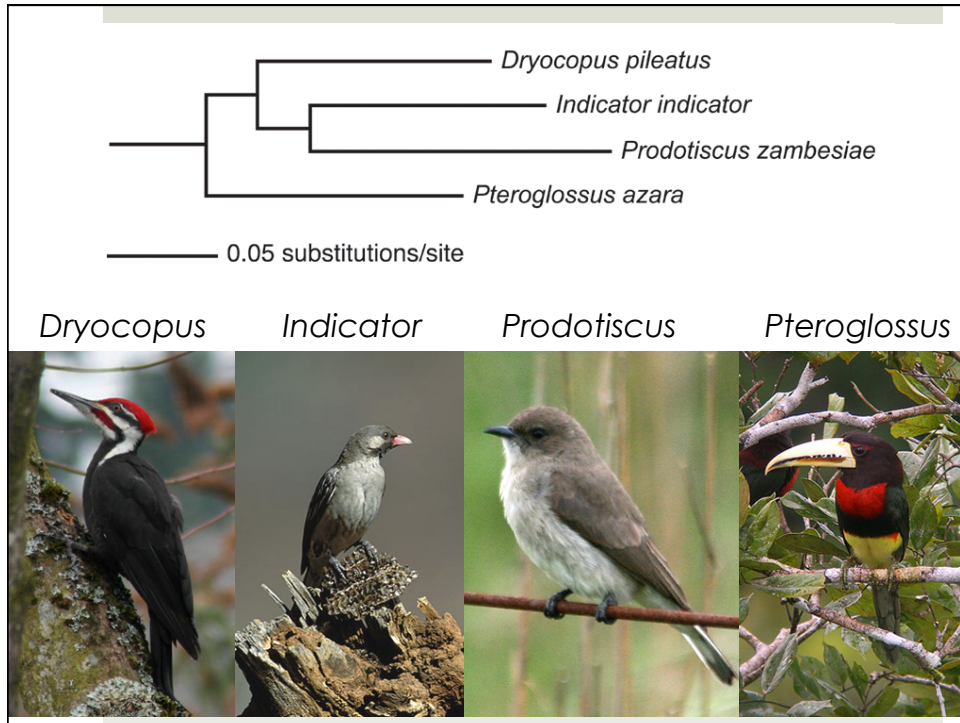
- ❖ uncertainty in calibration points
- ❖ fossil evidence provides lower bound on age only
- ❖ variance of genetic distance estimates
- ❖ "saturation" of genetic distances
- ❖ extrapolation outside of calibrated range
- ❖ ancestral polymorphism
- ❖ \*\*variation in substitution rate among lineages\*\*



## Relative Rates Test

- ❖ compares genetic distances between two taxa (A, B) and an outgroup (C)
- ❖ if evolutionary rate is constant, distances should be equal
- ❖  $d_{AC} = d_{BC}$





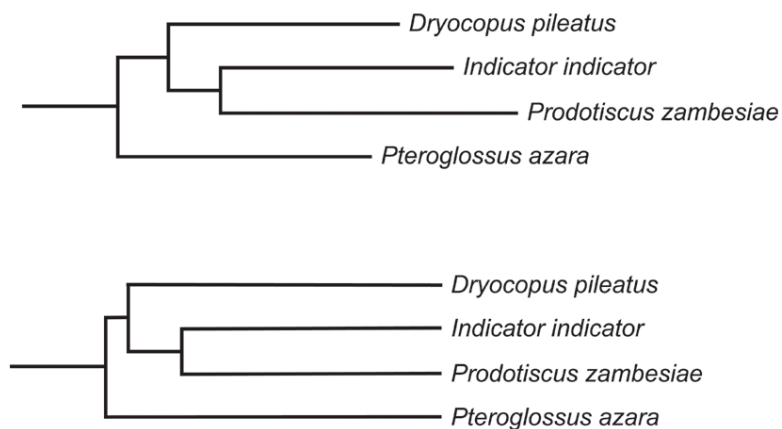
A phylogenetic tree identical to the one above, showing the relationships between *Dryocopus pileatus*, *Indicator indicator*, *Prodotiscus zambesiae*, and *Pteroglossus azara*. A scale bar indicates 0.05 substitutions/site.

Comparison	Sites	Differences						All	TVs
		AG	CT	AC	AT	CG	GT		
<i>Dryocopus</i> vs <i>Indicator</i>	8991	323	754	360	149	61	30	1677	600
<i>Dryocopus</i> vs <i>Prodotiscus</i>	8991	322	772	458	157	78	44	1831	737



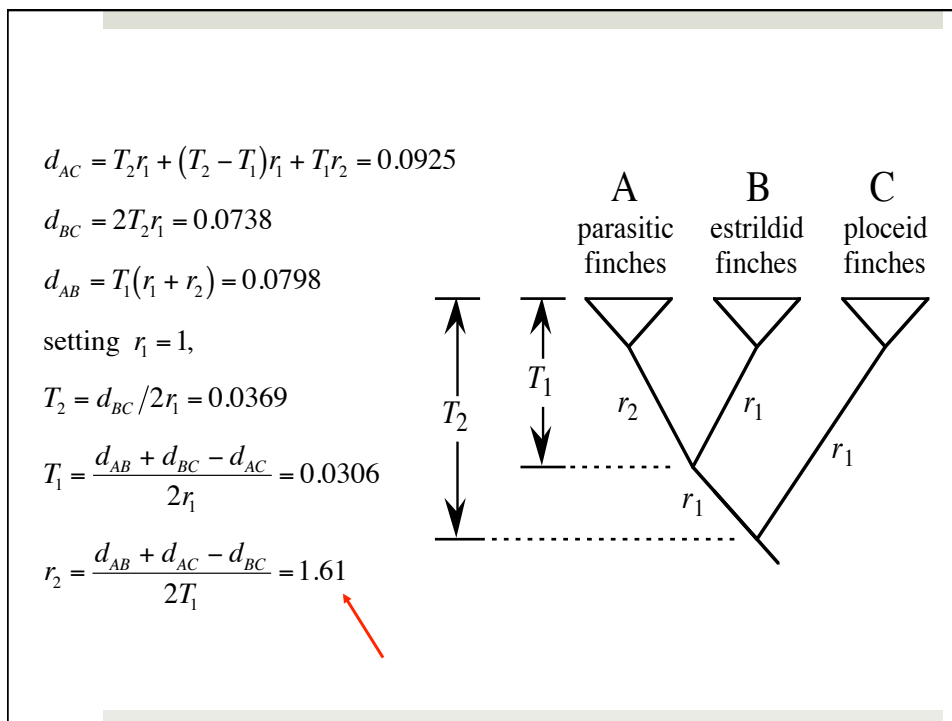
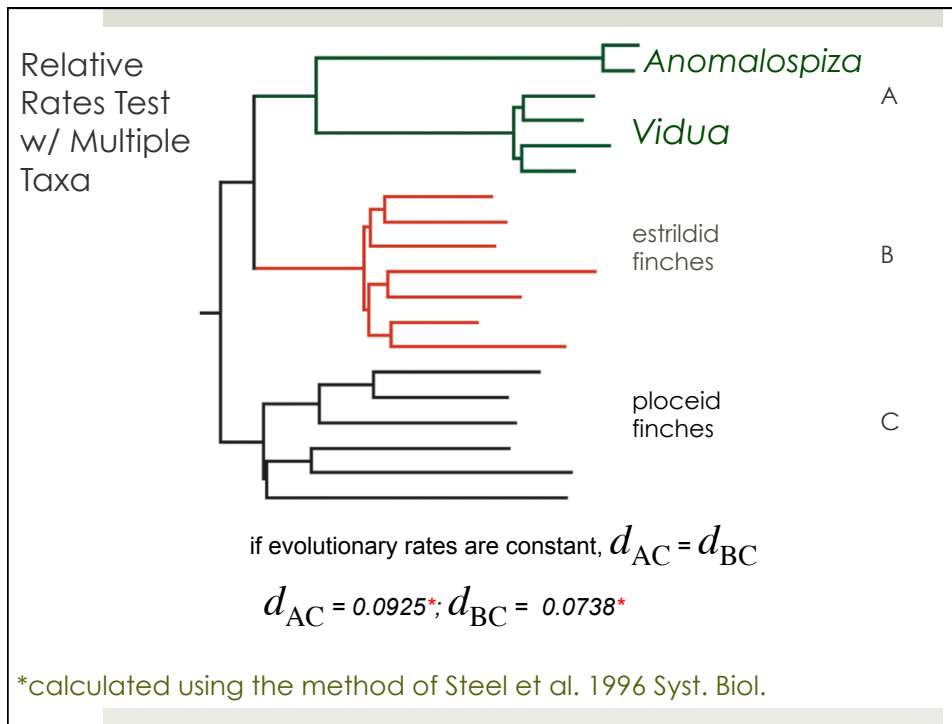
## Likelihood ratio test for rate constancy

- ❖ compare the likelihood (probability) of the data when a molecular clock is enforced versus the likelihood when all branches are free to vary in length (product of time and mutation rate)

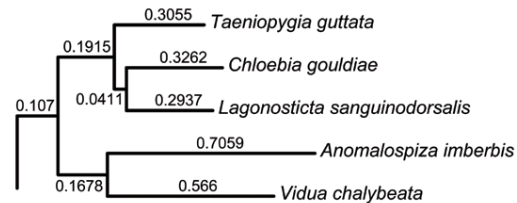


No clock:  $-\ln L = 27859.36$   
 Clock:  $-\ln L = 27904.29$   
 $2 \times \Delta \ln L = 89.86, p < 0.0001$

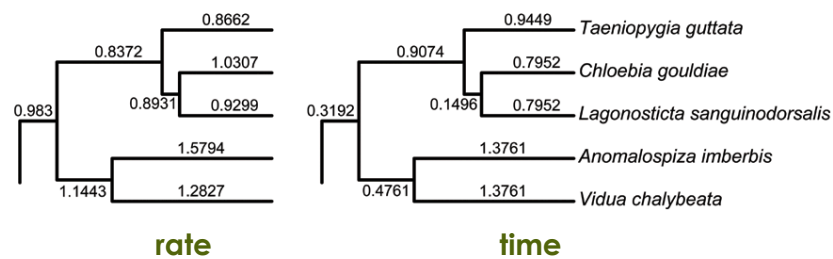
- test statistic:  $2 \times \Delta \ln L$  is distributed approximately as  $X^2$  (chi-square) with  $n-2$  degrees of freedom, where  $n$  = number of terminal taxa
  - unconstrained tree:  $2n-3$  branch lengths
  - constrained tree:  $n-1$  branch lengths



MrBayes: branch lengths (product of time and rate)



BEAST: separate estimates of rate and time



## Variation in Evolutionary Rate

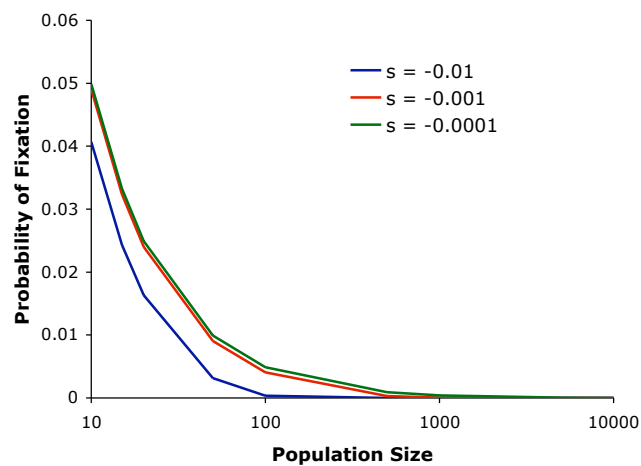
- ❖ rates may vary among lineages due to...
  - ❖ differences in life history
    - ❖ especially generation time, metabolic rate
  - ❖ diversifying natural selection
    - ❖ but likely limited to few sites in few genes
  - ❖ population history
    - ❖ the rate of neutral evolution does not depend on population size
    - ❖ the rate of nearly neutral evolution does!

## Nearly Neutral Theory

- ❖ what happens in small populations when selection is weak?
  - ❖ changes in allele frequency due to drift and selection are approximately equal  $|2Ns| \approx 1$
- ❖ probability of fixation for a new, “nearly neutral” allele:

$$\Pr(A \text{ fixed}) = \frac{2s}{1 - e^{-4Ns}}$$

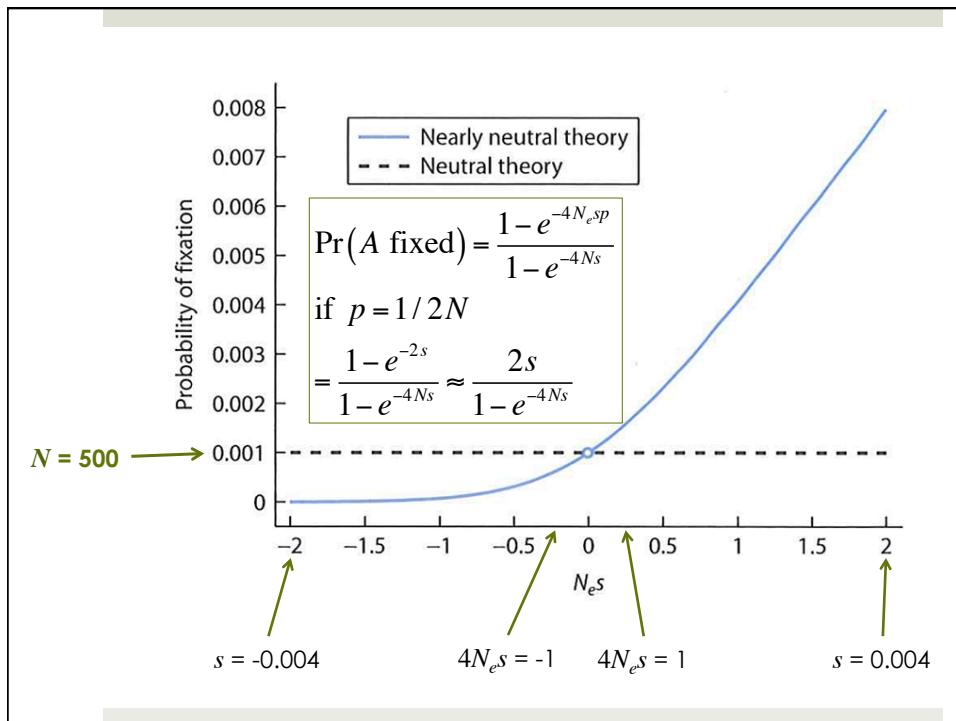
$$w_{AA} = 1 + \underline{s}, \quad w_{Aa} = 1 + \underline{s/2}, \quad w_{aa} = 1$$



$$\Pr(A \text{ fixed}) = \frac{2s}{1 - e^{-4Ns}}$$

## What qualifies as nearly neutral?

- ❖ Hamilton:  $2s = 1/2N_e$  or  $4N_e s = 1$ 
  - ❖ value at which “the processes of genetic drift and selection are **equal**”
- ❖ Hartl & Clark:  $|2Ns| \approx 1$
- ❖ Hedrick:  $s < 1/(2N)$  or  $2Ns < 1$
- ❖ Ohta & Gillespie (1996):  $s \approx 1/N$  or  $Ns \approx 1$



## Nearly Neutral Theory - Summary

- ❖ the rate of neutral evolution is independent of population size
  - ❖ substitution rate equals mutation rate  $2N\mu \times \frac{1}{2N} = \mu$
- ❖ in contrast, the fate of nearly neutral mutations depends on population size
  - ❖ when  $N$  is small, the effect of genetic drift can be comparable to that of selection, making slightly deleterious mutations "effectively neutral"
- ❖ thus, lineages experiencing small population size should accumulate both neutral and nearly neutral mutations, leading to a faster rate of sequence evolution

$$|2Ns| \approx 1$$

## Testing the Nearly Neutral Theory

- ❖ how to distinguish neutral and nearly neutral mutations?
  - ❖ synonymous (silent) versus non-synonymous (replacement) substitutions?
  - ❖ synonymous likely to be neutral
  - ❖ non-synonymous more likely to be deleterious

- ❖ Ohta (1994) - generation time effect differs between synonymous and non-synonymous mutations

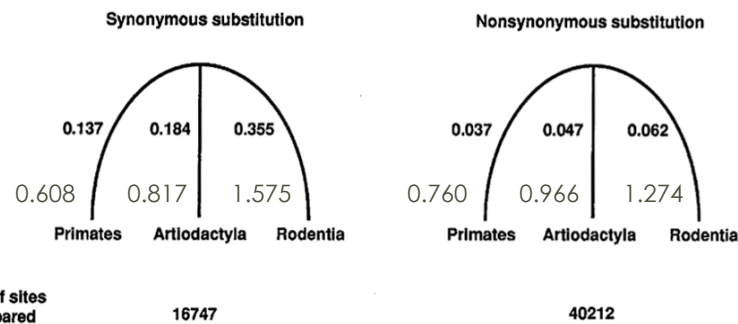
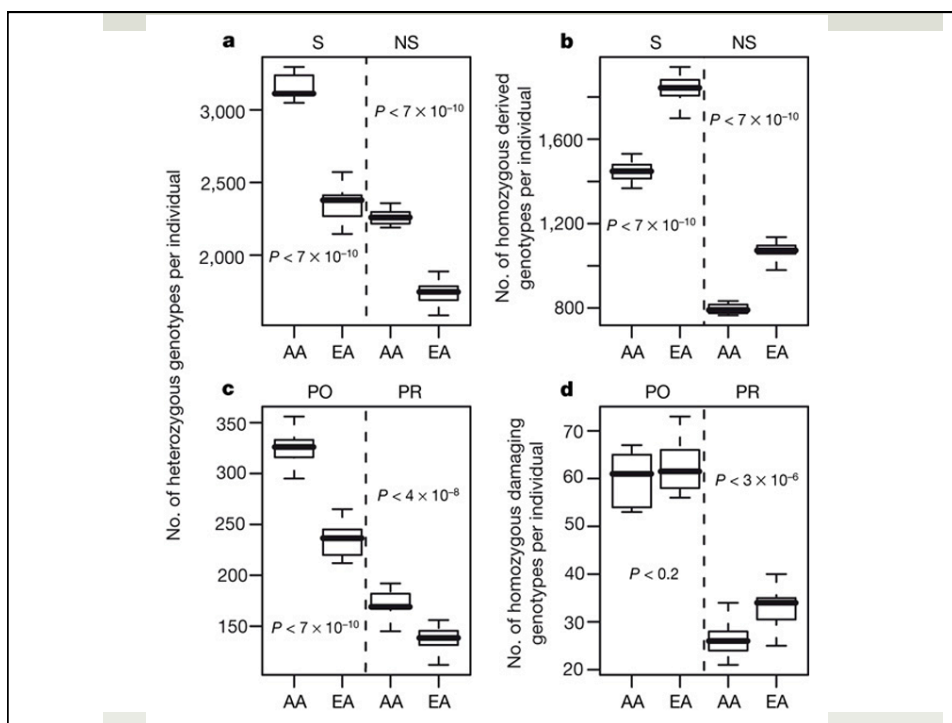


Fig. 1. Star phylogenies of 49 genes. Figures beside each branch are the estimated numbers of substitutions per site.

- ❖ interpreted as consequence of nearly neutral evolution
- ❖ inverse correlation between population size and body size/generation time

Lohmueller et al. 2007. Proportionally more deleterious genetic variation in European than in African populations. *Nature* 451: 994-997.

- ❖ used protein structure prediction to estimate the number of functionally consequential SNPs carried by each of 15 African Americans (AA) and 20 European Americans (EA)
- ❖ higher heterozygosity in AA, but...
- ❖ the proportion of SNPs that are non-synonymous is significantly higher in the EA sample (55.4%) than in the AA sample (47.0%)
- ❖ same result for SNPs that were inferred to be 'probably damaging' (15.9% in EA; 12.1% in AA)



Lohmueller et al. 2007. Proportionally more deleterious genetic variation in European than in African populations. *Nature* 451: 994-997.

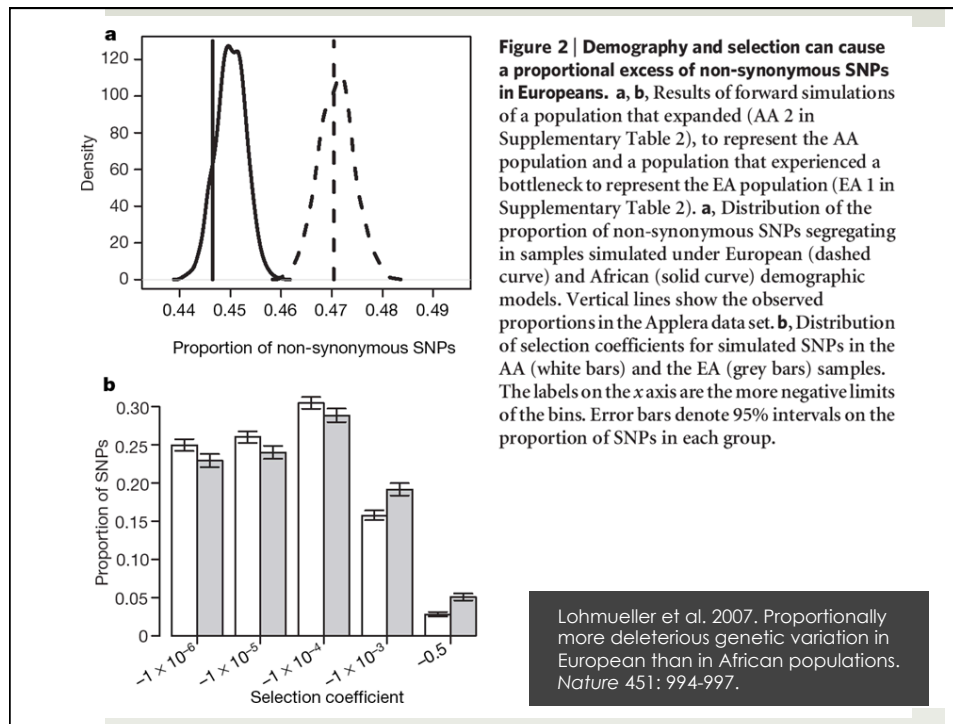
**Table 1 | Distribution of Appera SNPs by population and functional class**

Category	Shared	Private AA	Private EA	Mean derived frequency	
				AA*	EA†
Synonymous	8,056 (58.3%)	8,958 (53.0%)	3,879 (44.6%)	0.211	0.266
Non-synonymous	5,771 (41.7%)	7,950 (47.0%)	4,826 (55.4%)	0.174	0.202
Benign	4,448 (78.6%)	5,260 (67.7%)	2,928 (62.1%)	0.200	0.238
Possibly damaging	795 (14.0%)	1,572 (20.2%)	1,035 (22.0%)	0.113	0.119
Probably damaging	422 (7.4%)	942 (12.1%)	749 (15.9%)	0.099	0.108

\* Average frequency from SNPs segregating in the AA sample. No correction for ancestral misidentification was used.

† Average frequency from SNPs segregating in the EA sample. No correction for ancestral misidentification was used.





## Estimating $dN$ and $dS$

- ❖  $dN$  - non-synonymous divergence
- ❖  $dS$  - synonymous divergence

## Nei-Gojobori (1986) Method

1. calculate number of potentially synonymous and non-synonymous sites ( $s + n = 3$  per codon), disregarding stop codons

$$S = \sum_{j=1}^n \sum_{i=1}^3 f_i$$

e.g., Lysine:  
AAA:  $s = 1/3$   
AAG:  $s = 1/3$

e.g., Leucine:  
TTA:  $s = 2/3$   
TTG:  $s = 2/3$   
CTA:  $s = 1-1/3$   
CTG:  $s = 1-1/3$   
CTC:  $s = 1$   
CTT:  $s = 1$

$$N = 3n - S$$

## Nei-Gojobori (1986) Method

1. calculate number of potentially synonymous and non-synonymous sites ( $s + n = 3$  per codon), disregarding stop codons
2. calculate number of synonymous ( $s_d$ ) and non-synonymous ( $n_d$ ) differences for each codon
  1. if one difference, then obvious
  2. if two differences...

## two differences

- ❖ E.g., 2 possible routes...
    - (1) TTT (Phe) - GTT (Val) - GTA (Val)
      - 1 nonsynonymous, 1 synonymous
    - (2) TTT (Phe) - TTA (Leu) - GTA (Val)
      - 2 nonsynonymous
- $s_d = 0.5, n_d = 1.5$

## Nei-Gojobori (1986) Method

1. calculate number of potentially synonymous and non-synonymous sites ( $s + n = 3$  per codon), disregarding stop codons
2. calculate number of synonymous ( $s_d$ ) and non-synonymous ( $n_d$ ) differences for each codon
  1. if one difference, then obvious
  2. if two differences...
  3. if three differences...

## three differences

❖ E.g., 6 possible routes...

(1) **TTG** (Leu) - ATG (Met) - AGG (Arg) - **AGA** (Arg)

2 nonsynonymous, 1 synonymous

(2) TTG (Leu) - ATG (Met) - ATA (Ile) - AGA (Arg)

(3) TTG (Leu) - TGG (Trp) - AGG (Arg) - AGA (Arg)

~~(4) TTG (Leu) - TGG (Trp) - TGA (**Stop**) - AGA (Arg)~~

(5) TTG (Leu) - TTA (Leu) - ATA (Ile) - AGA (Arg)

~~(6) TTG (Leu) - TTA (Leu) - TGA (**Stop**) - AGA (Arg)~~

$$s_d = 0.75, n_d = 2.25$$

## Nei-Gojobori (1986) Method

$$3. dN = n_d / n,$$

$$4. dS = s_d / s$$

where  $n_d$  and  $s_d$  are the total number of synonymous and non-synonymous differences across the sequence and  $n$  and  $s$  are the average number of synonymous and nonsynonymous sites in the two sequences

	*		* *	*		* *	*	
	ACG	TAC	GTA	CGT	TTG	CCC	AAG	GAG
	Thr	Tyr	Val	Arg	Leu	Pro	Lys	Glu
s	1	1	1	1	2/3	1	1/3	1/3 = 6.33
	ACA	TAC	GTT	TGT	CTG	CCA	AGG	GAC
	Thr	Tyr	Val	Cys	Leu	Pro	Arg	Asp
s	1	1	1	1/2	4/3	1	1/3	1/3 = 6.5
s <sub>d</sub>	1	0	1	0	1	1	0	0
n <sub>d</sub>	0	0	0	1	0	0	1	1

$$dN = n_d/n = 3/17.585 = 0.171$$

$$dS = s_d/s = 4/6.415 = 0.624$$

$$dN/dS = 0.274$$

## PAML (Phylogenetic Analysis using Maximum Likelihood)

❖ versatile program for modeling sequence evolution

❖ basic transition matrix

$$Q_{ij} = \begin{cases} \mu\pi_j & \text{for a synonymous transversion} \\ \mu\kappa\pi_j & \text{for a synonymous transition} \\ \mu\omega\pi_j & \text{for a nonsynonymous transversion} \\ \mu\omega\kappa\pi_j & \text{for a nonsynonymous transition} \\ 0 & \text{if } \geq 2 \text{ differences} \end{cases}$$

❖ estimates  $d_N$  and  $d_S$  using maximum likelihood, where  $\kappa$  is the transition/transversion ratio and  $\omega$  is equal to  $d_N/d_S$

## $dN:dS$ ratio

- ❖ when measured in relation to the number of synonymous and non-synonymous sites
  - ❖  $dN/dS = 1$  if all substitutions are neutral
  - ❖  $dN/dS > 1$  suggests positive, diversifying selection
  - ❖  $dN/dS < 1$  suggests purifying selection (i.e., constraints on protein evolution)

Hughes & Nei 1988 Pattern of nucleotide substitution at major histocompatibility complex class I loci reveals overdominant selection. *Nature* 335:167-170.

- ❖ examined  $dN / dS$  in human MHC class 1 genes HLA-A, B & C (n = 12 sequences)

**Table 1** Mean numbers of nucleotide substitutions per 100 synonymous sites ( $d_s$ ) and per 100 nonsynonymous sites ( $d_N$ )

Locus (No. sequences)	Comparisons (No.)	Antigen recognition site (ARS) (N = 57)		Remaining codons in exons 2 & 3 (N = 124, 125) <sup>1</sup>			Exon 4 (N = 92)	$d_N$
		$d_s$	$d_N$	$d_s$	$d_N$	$d_s$	$d_s$	
<b>Human</b>								
A (5)	vs A (10)	3.5 ± 2.0	13.3 ± 2.2***	2.5 ± 1.2	1.6 ± 0.5	9.5 ± 3.0	1.6 ± 0.7**	
	vs B (20)	9.1 ± 3.3	25.1 ± 3.4***	11.9 ± 3.0	5.8 ± 0.7*	35.1 ± 8.1	2.2 ± 0.7***	
	vs C (15)	7.1 ± 3.4	21.9 ± 3.5***	17.1 ± 4.0	7.5 ± 1.4*	34.9 ± 7.8	2.1 ± 1.2***	
B (4)	vs B (6)	7.1 ± 3.1	18.1 ± 2.8**	6.9 ± 2.0	2.4 ± 0.7*	1.5 ± 1.1	0.5 ± 0.4	
	vs C (12)	6.0 ± 2.2	22.9 ± 3.4***	14.3 ± 3.2	5.7 ± 1.1*	10.6 ± 4.0	3.1 ± 1.2	
C (3)	vs C (3)	3.8 ± 2.5	8.8 ± 2.2	10.4 ± 2.8	4.8 ± 1.1	2.1 ± 1.5	1.0 ± 0.6	
<b>Overall means</b>								
Intralocus	(19)	4.7 ± 2.6	14.1 ± 2.4***	5.1 ± 2.1	2.4 ± 0.8	5.8 ± 2.0	1.1 ± 0.6**	
Interlocus	(47)	7.7	23.5	14.2	6.3	28.8	2.4	
All comparisons	(66)	6.8 ± 2.3	20.8 ± 2.3***	11.6 ± 2.1	5.2 ± 0.8**	22.1 ± 4.4	2.4 ± 0.7***	
$d_s > d_N : d_N > d_s$		0:66		63:3			61:3†	

$dN / dS > 1$ : evidence of positive, diversifying selection

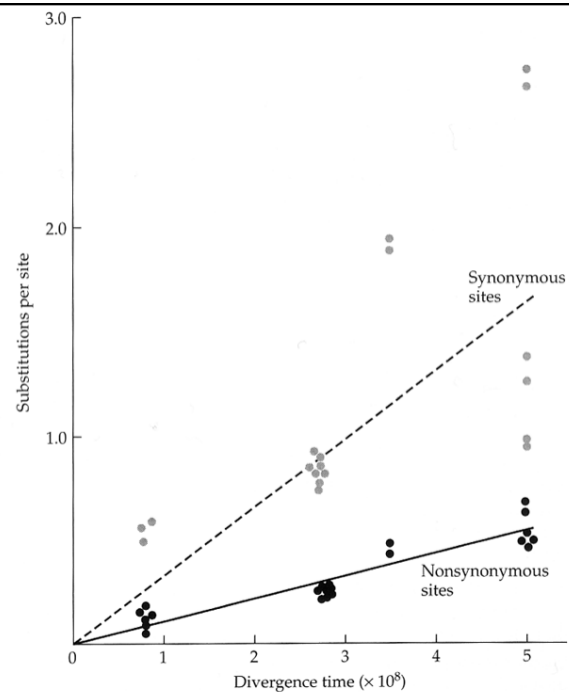
## Positive Selection

- ❖ testing at the gene level is a “dull tool”
  - ❖ positive selection will usually affect one or a few codons, while the rest of the gene remains constrained ( $dN/dS \ll 1$ )
  - ❖ nonetheless, genes associated with immune function and reproduction (self-recognition, sperm competition, sexual conflict) often have  $dN/dS > 1$
- ❖ more sophisticated methods are available to identify individual sites under selection

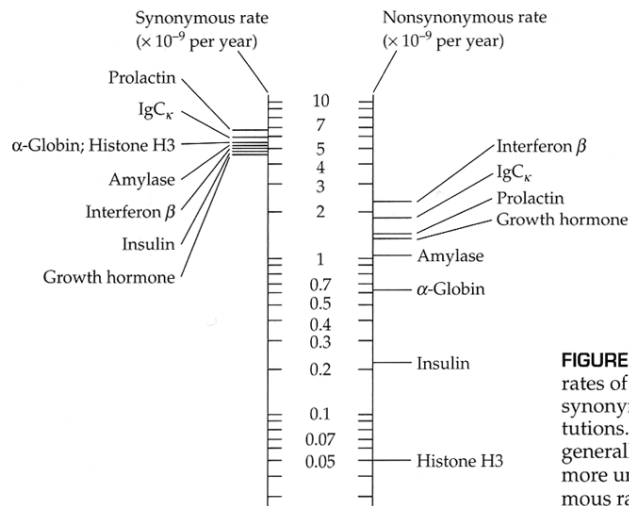
**FIGURE 7.12** Synonymous sites and nonsynonymous sites in the  $\beta$ -globin gene undergo substitutions at different rates, but to a first approximation both may appear to exhibit a clocklike substitution process. (From Li et al. 1985a.)

### purifying selection is the norm:

synonymous substitutions are more frequent than nonsynonymous substitutions in most genes

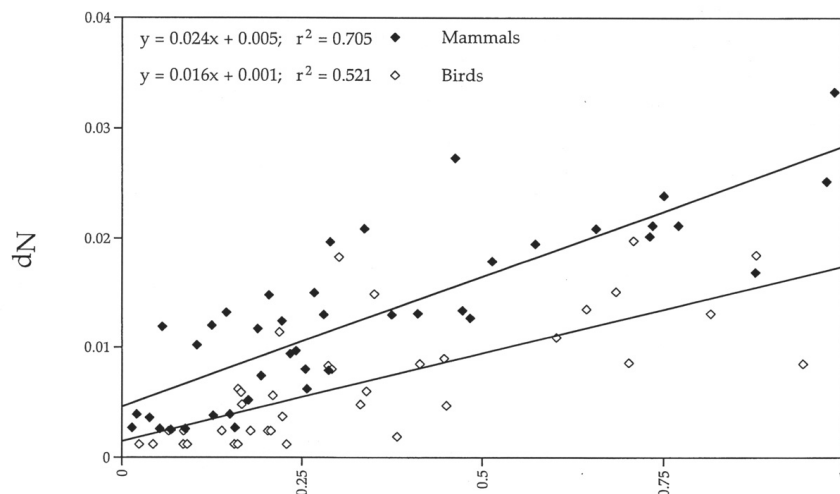


much greater variation among genes in non-synonymous rate than in synonymous rate



**FIGURE 7.14** Comparison of rates of synonymous and non-synonymous nucleotide substitutions. Synonymous rates are generally much faster and much more uniform than nonsynonymous rates. (From Kimura 1986.)

The avian constraint hypothesis...



independent pairwise comparisons of dN and dS for mtDNA protein-coding genes

dS

Stanley & Harrison MBE 1999



Woolfit & Bromham 2003  
 Increased rates of sequence evolution in endosymbiotic bacteria and fungi with small effective population sizes. *MBE* 20:1545-1555.

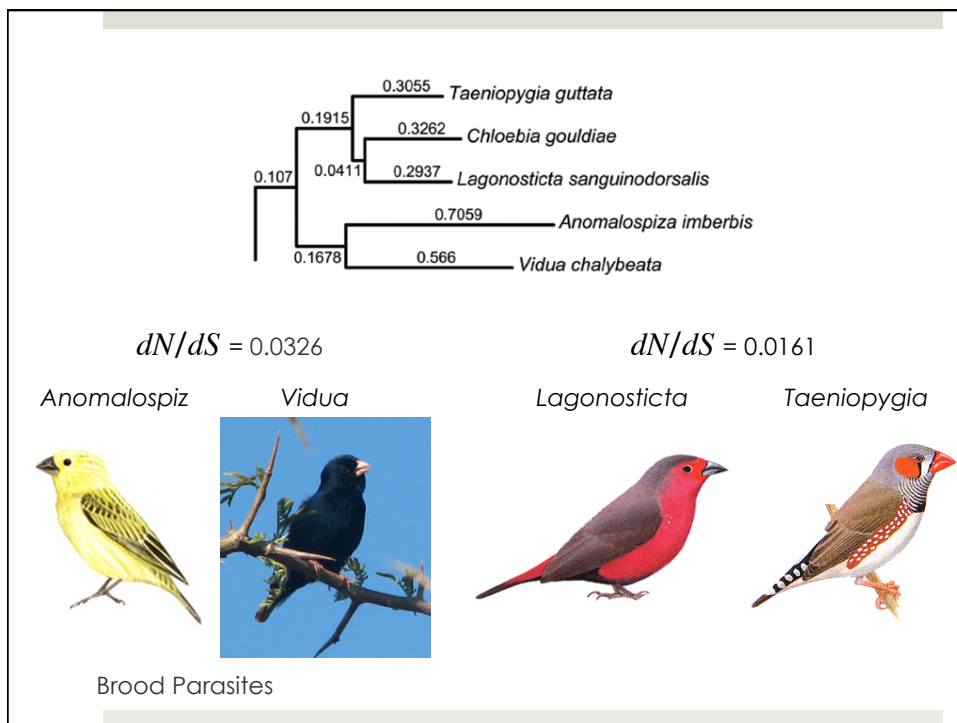
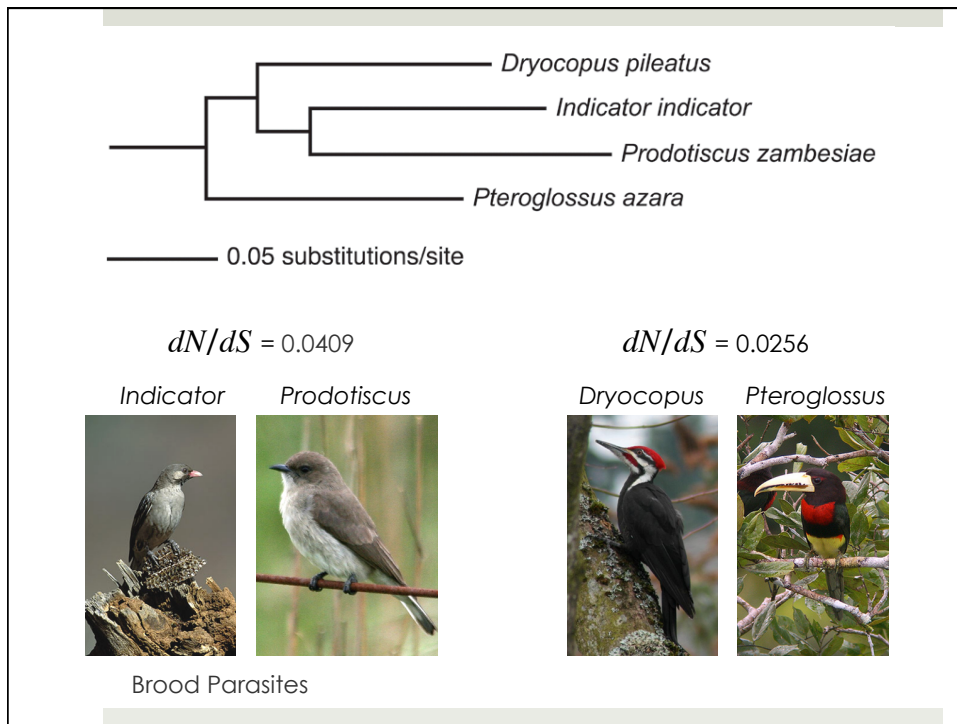
- higher rate in endosymbiotic bacteria interpreted as a consequence of nearly neutral evolution
- if so, these organisms should also have a higher  $d_N/d_S$  ratio...

Moran (1996) Accelerated evolution and Muller's ratchet in endosymbiotic bacteria. *PNAS* 93: 2873-2878

- $\diamond$  *Buchnera*: endosymbiont of aphids
- $\diamond$  higher  $d_N/d_S$  than free living bacteria

Table 3. Distances based on synonymous ( $d_S$ ) and nonsynonymous ( $d_N$ ) substitutions for *trp* genes of two *Buchnera* and of *E. coli*-*S. typhimurium* and for *argS* of the two *Buchnera*

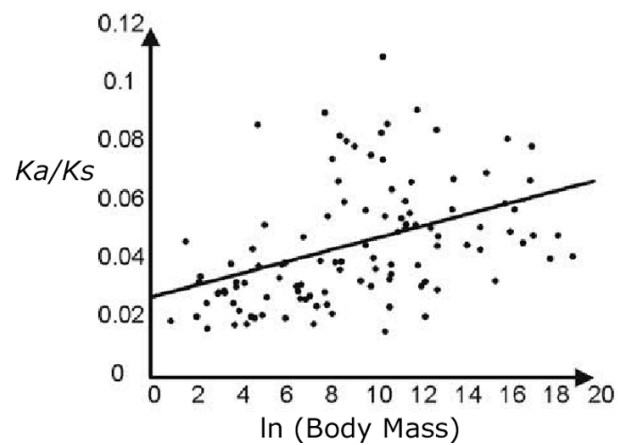
Gene (no. of codons)	Comparison	$d_S$	$d_N$	$d_S/d_N$
<i>trpa</i> (266)	<i>E. coli</i> - <i>S. typhimurium</i>	0.704 ± 0.032	0.083 ± 0.011	8.48
	<i>Buchnera</i> (Sg)- <i>Buchnera</i> (Sc)	0.570 ± 0.037	0.281 ± 0.018	2.03
<i>trpb</i> (397)	<i>E. coli</i> - <i>S. typhimurium</i>	0.581 ± 0.029	0.022 ± 0.005	26.77
	<i>Buchnera</i> (Sg)- <i>Buchnera</i> (Sc)	0.578 ± 0.031	0.167 ± 0.012	3.47
<i>trpc</i> (f)(469)	<i>E. coli</i> - <i>S. typhimurium</i>	0.629 ± 0.038	0.036 ± 0.018	17.5
	<i>Buchnera</i> (Sg)- <i>Buchnera</i> (Sc)	0.590 ± 0.035	0.273 ± 0.008	2.16
<i>trpd</i> (337)	<i>E. coli</i> - <i>S. typhimurium</i>	0.556 ± 0.031	0.016 ± 0.005	36.61
	<i>Buchnera</i> (Sg)- <i>Buchnera</i> (Sc)	0.567 ± 0.034	0.269 ± 0.016	2.11
<i>trpe</i> (520)	<i>E. coli</i> - <i>S. typhimurium</i>	0.577 ± 0.025	0.071 ± 0.008	8.13
	<i>Buchnera</i> (Sg)- <i>Buchnera</i> (Sc)	0.689 ± 0.026	0.264 ± 0.013	2.61
<i>argS</i> (131)	<i>Buchnera</i> (Sg)- <i>Buchnera</i> (Sc)	0.533 ± 0.056	0.370 ± 0.029	1.44



## “Constancy” of the Molecular Clock

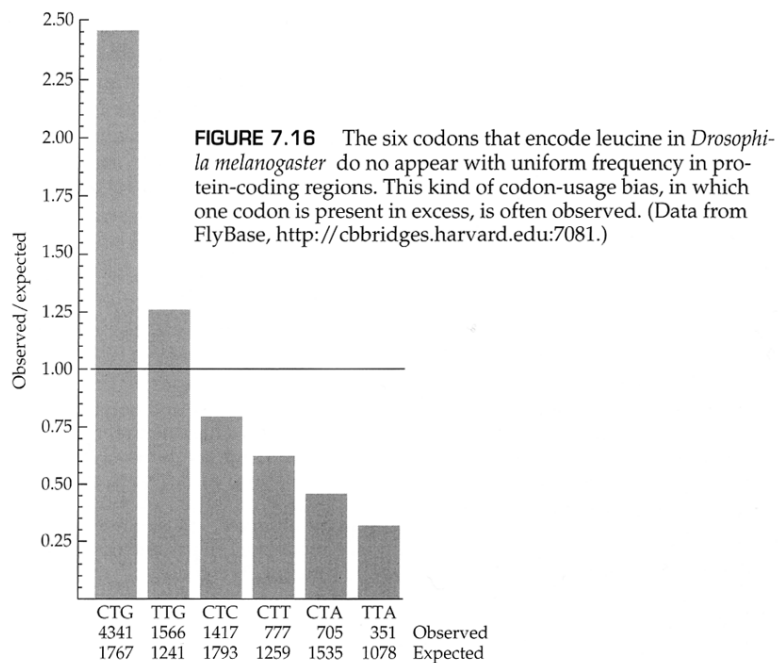
- ❖ data on sequence divergence suggest that evolutionary rate in many organisms is roughly constant when time is measured in years even if generation times vary
- ❖ if nearly neutral evolution is important, then the inverse correlation between generation time and population size may help to explain the relative constancy of rate among organisms with different life histories
  - ❖ small critters have shorter generation time resulting in a higher rate of neutral evolution
  - ❖ large critters have longer generation time but also smaller populations, resulting in a higher rate of nearly neutral evolution

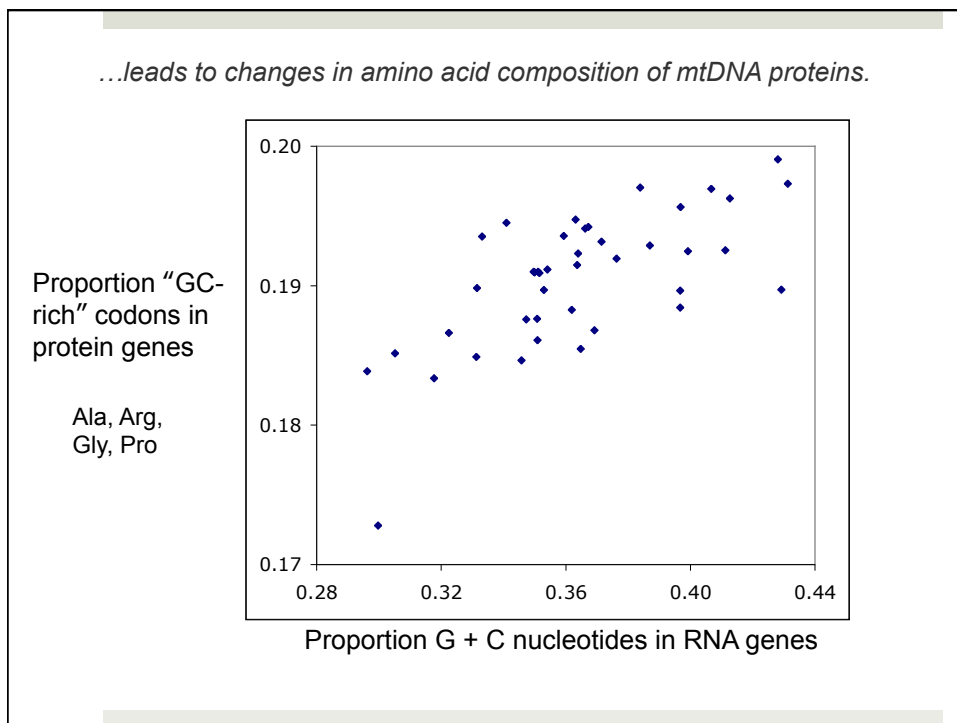
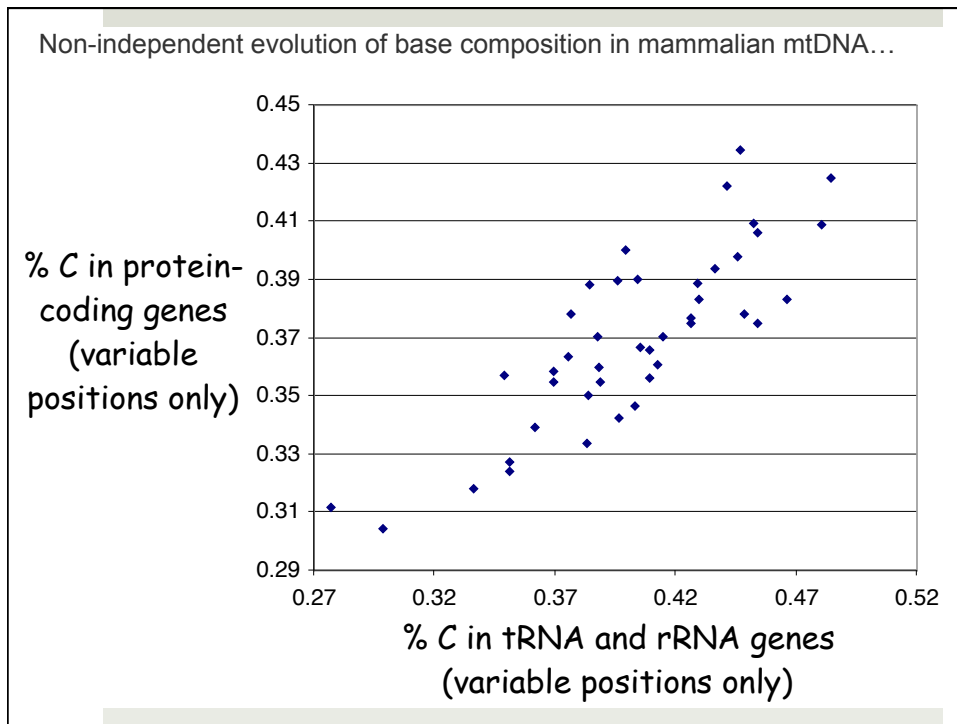
Popadin et al. (2007) Accumulation of slightly deleterious mutations in mitochondrial protein-coding genes of large versus small mammals. *PNAS* **104**, 13390-13395.



## But wait, are synonymous substitutions really neutral?

- ❖ codon-bias
  - ❖ “favored” codons (corresponding to more abundant tRNAs) are present at higher frequency in highly expressed genes than in genes with lower expression levels
- ❖ base composition bias
  - ❖ significant and sometimes substantial differences between lineages
    - ❖ e.g., birds have > GC content than mammals





Berglund *et al.* 2009 Hotspots of biased nucleotide substitutions in human genes. *PLoS Biology* 7: e1000026

❖ the fastest-changing genes in terms of amino acid substitutions show a biased pattern of fixation for AT-to-GC mutations

Category	Significance Level	Number of Genes	Ancestral GC Content	S→S	W→W	S→W	W→S	W→S Bias
<b>Genes</b>	**-sig	20	0.51	6	9	74	66	0.47
	*-sig	124	0.50	67	30	388	297	0.43
	non-sig	3,754	0.51	1,220	482	8,533	5,417	0.39
	Total	3,878	0.51	1,287	512	8,921	5,714	0.39
<b>Most diverged exons</b>	**-sig	20	0.51	2	1	21	34	0.62
	*-sig	124	0.50	22	10	167	138	0.45
	non-sig	3,754	0.51	535	208	3,533	2,281	0.39
	Total	3,878	0.51	557	218	3,700	2,422	0.40

AT→GC = weak→strong