Cross-Layer Co-Optimization of Network Design and Chiplet Placement in 2.5D Systems

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Abstract—2.5D integration technology is gaining attention and popularity in manycore computing system design. 2.5D systems integrate homogeneous or heterogeneous chiplets in a flexible and cost-effective way. The design choices of 2.5D systems impact overall system performance, manufacturing cost, and thermal feasibility. This paper proposes a cross-layer co-optimization methodology for 2.5D systems. We jointly optimize the network topology and chiplet placement across logical, physical, and circuit layers to improve system performance, reduce manufacturing cost, and lower operating temperature, while ensuring thermal safety and routability. We also propose a novel gas-station link, which enables pipelined inter-chiplet links in passive interposers. Our cross-layer methodology achieves better performance-cost tradeoffs of 2.5D systems and yields better solutions in optimizing inter-chiplet network and 2.5D system designs than prior methods. Compared to single-chip systems, 2.5D systems designed using our new approach achieve 88% higher performance at the same manufacturing cost, or 29% lower cost with the same performance. Compared to the closest state-of-the-art, our new approach achieves 40-68% (49% on average) iso-cost performance improvement and 30-38% (32% on average) iso-performance cost reduction.

Index Terms—2.5D Integration, Cross-Layer Optimization, Thermal, Place and Route, Networks, Manycore Systems.

I. INTRODUCTION

CMOS technology scaling has been slowing down over the past decade. It is getting increasingly difficult to continue technology scaling; hence, the industry has started to seek alternative solutions in the ‘More Than Moore’ direction. Instead of putting more transistors in a monolithic chip, one approach is to pack multiple dies in a package [2], [3], [4]. This approach enables flexible integration of homogeneous or heterogeneous dies, and speeds up the design and manufacturing of semiconductor systems. Therefore, die-stacking technologies like 2.5D and 3D integration have gained traction.

These multi-die systems are cost-effective alternatives to single-chip systems (also called 2D systems), as breaking down a chip into multiple chiplets alleviates the manufacturing yield drop suffered in a large 2D chip. 3D integration stacks chiplets vertically to increase memory bandwidth and reduce system footprint [5], but aggravates thermal challenges [6].

2.5D integration places multiple chiplets on a silicon interposer, which can be either passive or active. The chiplets communicate with each other through high-density fine-grained µbumps and interconnects in the interposer. Both 2.5D and 3D integration technologies enable designing high-bandwidth, low-latency networks, which could be utilized to handle the growing data traffic requirements of today’s applications [2], [3], [4]. Compared to 2D systems, 2.5D systems have better thermally-safe system performance [7], enable integration of heterogeneous technologies [8], [4], and have lower cost [5]. Compared to 3D systems, 2.5D systems have better thermal dissipation capability, provide additional routing resources, and are more cost effective [5], [9]. Therefore, 2.5D systems are gaining attention and popularity as competitive candidates to sustain the performance and cost scaling in computing systems [4], [5], [10], [11], [12], [13]. There are already commercial 2.5D products in the market, such as Xilinx Virtex 7 [13], AMD Fiji [14], Nvidia Tesla [15], and Intel Foveros [16]. These existing products typically place the chiplets adjacent to each other on an interposer to embrace the benefits of low communication latency due to short inter-chiplet links and low manufacturing cost resulting from small interposer sizes. However, the design and optimization of 2.5D systems, including chiplet placement, inter-chiplet network architecture, design of inter-chiplet links and µbump assignment, need to be thoroughly explored to maximize the benefits of 2.5D integration [17].

In this paper, we perform a cross-layer co-optimization of 2.5D inter-chiplet network design and chiplet placement across logical, physical, and circuit layers. Our methodology jointly optimizes network topologies, link circuit and routing options, µbump assignment, and chiplet placement. Consider the following two cases that highlight the need for such a cross-layer approach. (1) If we adopt a top-down approach, an architecture-level analysis of network topologies indicates that high-radix, low-diameter networks provide the best overall system performance (in instructions per cycle) for inter-chiplet networks. However, in the physical layer, such networks usually require long wires, which would limit the network performance, and hence, the overall system performance. In the circuit layer, such long wires require repeaters and/or need to be pipelined to achieve high performance, which necessitate active (rather than passive) interposer technology. Since active interposers are 10× more expensive than passive interposers [18], the system cost becomes expensive and so the top-down approach does not provide a desirable solution. (2) A bottom-up, cost-centric approach prefers to use passive interposers, which can only support repeaterless links in the
circuit layer, thus degrading link performance and limiting maximum link length. This leads to the adoption of low-radix, high-diameter inter-chiplet networks, which lowers overall system performance. Our cross-layer methodology comprehends logical layer, physical layer, and circuit layer together, leading to a better system solution compared to using solely top-down or bottom-up approaches as in previous works.

Our cross-layer methodology fills a significant gap in the literature on 2.5D system optimization by including inter-chiplet network design and chiplet placement together. Cross-layer co-optimization allows for simultaneous consideration of thermal behavior of chiplets, multiple potential network topologies, and multiple inter-chiplet link options, including their circuit designs, physical design constraints and routing costs. Previous works have explored limited tradeoffs among cost, power, thermal feasibility and performance of 2.5D systems due to the lack of such a cross-layer co-optimization methodology. For example, our prior work [7] describes a chiplet placement method that results in high-performance, low-cost, and thermally-safe 2.5D systems. However, that method lacks a true cross-layer co-optimization as it considers only a Unified-Mesh network topology in the logical layer, determines the physical design of inter-chiplet links without accounting for the \( \mu \) bump overhead in the physical layer, and uses only a repeaterless link in the circuit layer. Our latest work [1] improves on our prior work [7] by jointly accounting for network topologies, \( \mu \) bump overhead, and inter-chiplet circuit designs across the three layers, but it covers a limited set of chiplet placement options.

As shown in the rest of this paper, our proposed cross-layer co-optimization methodology achieves better performance-cost tradeoffs of 2.5D systems. Our methodology explores a rich solution space. Specifically, in the logical layer, we consider a variety of network topologies, including Mesh, Concentrated-Mesh (Cmesh), Butterfly, Butterdout [5], and Ring. In the physical layer, we search for the chiplet placement that minimizes operating temperature and meets the routing constraints. In the circuit layer, we explore inter-chiplet link designs. We co-optimize network topology, chiplet placement and routing, as well as inter-chiplet link design and provide a solution that achieves 88% iso-cost performance improvement and 29% iso-performance cost reduction compared to a single-chip design. Compared to our prior work [1], we achieve 40-68% (49% on average) iso-cost performance improvement and 30-38% (32% on average) iso-performance cost savings. The main contributions of this paper are as follows.

- We develop a cross-layer co-optimization methodology that jointly optimizes 2.5D systems across logical, physical, and circuit layers. The outcome of our methodology includes network topology, chiplet placement, inter-chiplet link design and routing.
- Our methodology maximizes performance, minimizes manufacturing cost, and minimizes operating temperature. We use a soft constraint for peak temperature in the optimization problem to achieve better overall performance gain or cost reduction by allowing a small amount of thermal violation.
- We develop a simulated annealing algorithm to search the high-dimensional placement solution space. Our placer supports arbitrary placements that consider non-matrix and asymmetric chiplet organizations. We enhance a 2.5D cost model [19] to incorporate a comprehensive \( \mu \) bump overhead analysis on chiplet area and yield. We use gas-station link design [1] to enable pipelining in a passive interposer.

### II. BACKGROUND

2.5D integration is a promising technology that enables the integration of homogeneous or heterogeneous sets of chiplets onto a carrier. The carrier provides additional wiring resources that can be leveraged to increase communication bandwidth between the chiplets and improve system performance [20]. Furthermore, 2.5D integration is more cost effective than large 2D chips and is more thermally efficient than 3D systems [19]. Currently, 2.5D integration technology is being widely explored by both academia [20], [5], [10] and industry [13], [12], [14], [21], [15], [16].

Embedded Multi-die Interconnect Bridge (EMIB) [22] and interposer [13] are two commonly used carrier options for 2.5D integration technology. EMIB is a novel integration method, which embeds small pieces of silicon interconnect bridges in the organic package substrate to connect the edges of adjacent chiplets for die-to-die communication. Silicon interposer technology uses a relatively large silicon interposer to house all chiplets. It is more mature and has been used in commercial products [13], [14]. Both EMIB and interposer can provide high density die-to-bridge and die-to-interposer connections, respectively, and correspondingly, high-density die-to-die connections [23]. EMIB-based approach requires less silicon area than silicon interposer-based approach and thus has lower silicon cost [23]. However, the number of die-to-die connections per layer of EMIB is limited by bridge interface length [24], and EMIB increases organic substrate manufacturing complexity [25]. Furthermore, EMIB can only hook up adjacent chiplets. When two chiplets that are far apart are logically connected, they cannot have direct links and need multi-hop communication using EMIB technology. Interposer-based integration provides more flexibility in chiplet placement, network design and interconnect routing, and thus, has better thermal dissipation capability as it does not require chiplets to be placed close to each other. Therefore, we focus on interposer-based 2.5D integration in this paper.

A 2.5D-integrated system consists of three main layers: an organic substrate, a silicon interposer, and a chiplet layer. \( \mu \) bumps connect the chiplets and the silicon interposer. Through-silicon vias (TSVs) connect the top and the bottom of the interposer, and C4 bumps connect the interposer and the organic substrate. Epoxy resin is often used to underfill the
connection layers (C4 bumps layer and µbumps layer) and the empty spaces between chiplets [26]. Figure 1 shows the cross-section view of a 2.5D system in our study.

III. RELATED WORK

2.5D integration of smaller chiplets on a large interposer has been demonstrated to achieve a higher compute throughput per watt (or volume) than a single large die [19], [27]. Several related studies have explored the design and optimization of 2.5D systems, with primary focus being placed on individual design layers: logical, physical, and circuit.

At the logical layer, Jerger et al. [20] present a hybrid network topology between the cores and memory. They account for different coherence and memory traffic characteristics across applications, and design a hybrid network-on-chip (NoC) that has low latency and high throughput. In their follow-up work, Kannan et al. [5] evaluate the impact of different network topologies on 2.5D systems, and demonstrate that disintegration of a large 2D chip into multiple chiplets improves manufacturing yield and lowers costs. However, their work overlooks the µbump overhead. Ahmed et al. [28] identify that interposer’s routing resources are highly under-utilized due to the high interconnect pitch in 2.5D systems. To maximize performance, they propose a hierarchical mesh network for inter-chiplet communication. Akgun et al. [29] perform a design space exploration of different memory-to-core network topologies and routing algorithms. However, a static placement of chiplets in their work limits a complete cross-layer exploration that leaves much of the performance benefits in 2.5D systems untapped. While these works aim to maximize the system performance under different traffic conditions, they do not account for the thermal impact and a complete manufacturing cost model in the NoC design and optimization. In addition, these works do not consider different chiplet placement and link routing options.

At the physical layer, there have been several optimization-based approaches aimed at providing routing and placement solutions for 2.5D systems. Placing chiplets closer to each other results in lower manufacturing cost and higher performance (reduced wirelength), but higher temperature. Therefore, finding a thermally-aware placement and routing solution that maximizes performance and/or minimizes cost is essential in 2.5D systems. Osmolovskiy et al. [30] optimize the chiplet placement to reduce the interconnect length using pruning techniques. Ravishankar et al. [31] determine the quality of different placement options in a 2D grid using a stochastic model and implement a placer for 2.5D FPGAs. Seennuth et al. [32] consider the increased design solution space in 2.5D systems due to flexible I/Os in their chiplet placement problem. They present a method for die placement and pin assignment using simulated annealing to minimize the total wirelength. Much of the focus of routing in 2.5D systems has been placed on minimizing IR drops and total wirelength in inter-chiplet links [33] and minimizing the number of metal layers [34]. None of these physical layer optimization solutions consider thermal effects.

Prior research at the circuit layer of 2.5D systems generally focuses on link optimization techniques to improve the network and system throughput. Karim et al. [35] evaluate the power efficiency of electrical links with and without electrostatic discharge (ESD) capacitance. Stow et al. [19] evaluate both repeater and repeaterless links to explore the benefits of active and passive interposers respectively. There have also been efforts on using emerging technologies like wireless links [36] and silicon-photonic links for communication in 2.5D systems [37], [38], [39].

A common drawback among these previous works is that their design and optimization only focus on a single design layer. In contrast, we optimize the cost, performance and temperature by jointly considering the logical, physical and circuit layers of the inter-chiplet network. We evaluate various logical topologies and their feasibilities at the physical and circuit layer. At the physical layer, we design an overlap-free and thermally-safe routing and placement solution that results in the lowest cost and operating temperature. The circuit layer provides us with multiple circuit design options for inter-chiplet links. Our cross-layer methodology, thus, presents a rich solution space to evaluate a variety of network options at different design layers for 2.5D systems, thus enabling accurate and complete modeling of such systems.

IV. CROSS-LAYER CO-OPTIMIZATION OF NETWORK DESIGN AND CHIPLET PLACEMENT IN 2.5D SYSTEMS

The ultimate goal of our cross-layer co-optimization methodology is to jointly maximize performance, minimize manufacturing cost, and minimize peak operating temperature. Our methodology comprehends a wide design space across logical, physical and circuit layers, and integrates multiple simulation tools and analytical models that evaluate aspects of system performance, manufacturing cost, interconnect performance, temperature, and routing.

In this section, Section IV-A first introduces the cross-layer co-optimization problem formulation and the methodology we use to solve it. Figure 2 shows our cross-layer methodology and provides an outline of upcoming subsections. Section IV-B describes the optimization knobs in the design space across the logical, physical and circuit layers. These knobs form the basis for modeling the 2.5D network and chiplet placement, and enable cross-layer optimization. Section IV-C presents the tools and evaluation framework that models the 2.5D system and evaluates the system metrics of performance, power, temperature and cost. We present five tools that work within the framework to evaluate these system metrics: (1) System Performance Oracle that uses Sniper [40] and McPAT [41]; (2) Cost Oracle that computes the manufacturing cost of the 2.5D system; (3) Interconnect Performance Oracle that uses HSPICE [42] simulations to evaluate the interconnect circuit timing; (4) Thermal Analysis Tool that uses HotSpot [43] to evaluate the temperature; and (5) Routing Optimizer that uses an MILP to solve for the optimal routing solution and the corresponding maximum wirelength. Section IV-D demonstrates the thermally-aware place and route (PNR) tool that is based on simulated annealing and interactively uses the oracles described in Section IV-C to explore the chiplet placement solution space to minimize operating temperature and meet routing constraints.
A. Optimization Problem Formulation and Methodology

Our objective is to jointly maximize performance, minimize manufacturing cost, and minimize peak operating temperature. While minimizing temperature for longer system lifetime, we also maintain the peak temperature below a threshold to avoid failures. We explore various network topologies, link options (stage count and latency), interposer sizes, frequency and voltage settings, and chiplet placements to find an optimal solution that is routable and thermally-safe. Ensuring that timing is met across the inter-chiplet links is crucial for the design, and the placement and routing have a dramatic impact on closing timing. The temperature threshold is relatively negotiable, as there is usually some headroom between the threshold and the actual temperature that causes rapid failures. Exceeding the temperature threshold ($85^\circ C$ in our case) by a few degrees would not immediately burn the system, and the impact on system lifetime could be alleviated by applying reliability management techniques that stress different parts of a chip over time. Thus, in the objective function we apply a soft constraint for peak temperature instead of a hard constraint. We use the notations listed in Table I to formulate our optimization problem as follows:

Minimize:

$$\min \alpha \times \frac{1}{TPS} + \beta \times Cost_{norm} + \gamma \times T_{op} + \eta \times g(T, T_{th})$$

Subject to:

$$g(T, T_{th}) = \frac{1}{10} \left( \max(T - T_{th}, 0) \right)^2$$

$$L \leq L_{th}$$

$$w_{int} \leq 50$$

$$\max(|X_i - X_j|, |Y_i - Y_j|) \geq \frac{W_{D}}{4} + 2 \times w_{ubump} + w_{gap}, \forall i, j, i \neq j$$

Equation (1) is the cross-layer objective function, which jointly maximizes performance ($IPS$) while minimizing manufacturing cost ($Cost$) and peak operating temperature ($T$). We normalize each term using Min-Max Scaling ($\frac{X_{norm}}{\max(X_{norm})}$) to reduce the impact of imbalanced ranges and values of raw data. $\alpha, \beta,$ and $\gamma$ are user-specified weights having no units, and we set the sum of $\alpha, \beta,$ and $\gamma$ to 1. The last term $g(T, T_{th})$ is the penalty function for peak temperature, and $\eta$ is the penalty weight. It is important to pick an appropriate value for $\eta$ for a soft-temperature-constrained problem. If $\eta$ is too small, the optimization problem has no thermal constraint, but if $\eta$ is too large, the optimization problem effectively becomes a hard-temperature-constrained problem. In our case, we explore a range of $\eta$ from 0.001 to 1 and pick $\eta$ to be 0.01, which gives a good balance between not having any constraint and having a hard temperature constraint. Equation (2) describes the penalty function. The penalty term is zero when $T$ meets the threshold $T_{th},$ and positive otherwise. We use a quadratic function instead of a linear function to suppress the penalty for a small violation and highlight the penalty for a large violation. Equation (3) is the routing constraint. Where the wirelength must be shorter than the reachable length for a given voltage-frequency setting and target latency (see Figure 6). Equation (4) constrains the interposer size to be no larger than $50mm \times 50mm,$ which is within the exposure field size of 2X JetStep Wafer Stepper [44] and avoids extra stitching cost. Equation (5) ensures there is no overlap between chiplets.

To solve the optimization problem, we integrate simulation tools and analytic models discussed in Section IV-C. We first generate a complete table of all the combinations of network topologies, inter-chiplet link stage counts and latencies, voltage-frequency settings, and interposer sizes (see Section IV-B). We precompute system performance, power, allowable-inter-chiplet link length, and manufacturing cost for each entry in the table. We normalize the performance as well as the cost, and compute the weighted sum of the first two terms in the objective function ($\alpha \times \frac{1}{IPS_{norm}} + \beta \times Cost_{norm}$), and denote it as $Obj2$, where 2 indicates the number of terms. We then sort the table entries based on the values of $Obj2$ in ascending order. To get the temperature term for each table entry, we build a thermally-aware PNR tool to determine the chiplet placement that minimizes the system operating temperature while meeting the routability requirement (see Section IV-D). For our design-time optimization, we assign the worst-case power, which is the highest core power among 256 cores of high-power application Cholesky, to all the cores while determining the optimal chiplet placement using our thermally-aware PNR tool. Then, we run real applications on top of the optimal chiplet placement to get the actual application temperature. Our thermally-aware PNR tool iterates chiplet placement, and interactively evaluates peak operating temperature and maximum inter-chiplet wirelength of each placement. Each temperature simulation takes approximately 30 seconds and each routing optimization takes a few seconds to 10 minutes. For manageable simulation time, for each table entry we limit the number of placement iterations to 1000, while determining the minimum peak temperature.

To speed up the simulation, we progressively reduce the number of table entries for which we need to complete the thermally-aware PNR process, which determines the minimum
peak temperature and the corresponding chiplet placement for each table entry. Once the process completes for a table entry, all the terms (performance, cost, temperature, and penalty) in the objective function for that table entry become available. We add up the four terms to get the objective function value of the entry, and denote it as $\text{Obj}_j$, where 4 indicates the number of terms. We keep track of the minimum of the available $\text{Obj}_j$ values using $\text{Obj}_{j_{\min}}$. For the entries whose $\text{Obj}_2$ value is greater than $\text{Obj}_{j_{\min}}$, there is no need to run the thermally-aware PNR tool, since the tool cannot find a solution whose $\text{Obj}_4$ value is less than $\text{Obj}_{j_{\min}}$. We start the thermally-aware PNR process with the entries in the sorted order based on $\text{Obj}_2$ values, progressively removing the entries that have no chance to be optimal, and stop when all the remaining entries have available temperature and $\text{Obj}_4$ values. Using this technique of progressively reducing solution space, we achieve $6\times$ speedup for the performance-focused case ($(\alpha, \beta, \gamma) = (0.8, 0.1, 0.1)$), $7.8\times$ speedup for the cost-focused case ($(\alpha, \beta, \gamma) = (0.1, 0.8, 0.1)$), and $1.5\times$ speedup for the case that jointly focuses on performance, cost, and temperature ($(\alpha, \beta, \gamma) = (0.333, 0.333, 0.333)$). For the temperature-focused case ($(\alpha, \beta, \gamma) = (0.1, 0.1, 0.8)$), we only achieve $1.02\times$ speedup because the temperature term dominates, and thus, we can barely rule out any of the table entries using the $\text{Obj}_2$ and $\text{Obj}_{j_{\min}}$ comparison. In this paper, our experiments are based on the performance-focused case.

B. Cross-layer Optimization Knobs

1) Logical Layer: One of the main questions in 2.5D logical design is how to connect multiple chiplets using the interposer. In the logical layer, we explore two types of network topologies for 2.5D systems. In Figure 3, we show the logical views of network topologies. These views only illustrate the logical connections and not the actual chiplet placement. The first type is a unified network, which directly maps a NoC topology designed for a 2D system onto a 2.5D system to preserve the same logical connections and routing paths. We explore Unified-Mesh (U-M), where each core has a router, and Unified-Cmesh (U-CM), where four cores share a router, as shown in Figure 3(a)-(b). Unlike single-chip NoCs, the source and the destination of a logical channel in 2.5D systems may not reside on the same chiplet. The inter-chiplet link has to travel through the silicon interposer, which may not always meet the single-cycle latency due to long physical wires. In our evaluation, we consider inter-chiplet links with latencies varying from single cycle to five cycles.

The second type is a hierarchical network, which breaks down the overall network into two levels: one level has multiple disjoint local networks and the other level has a global network. In 2.5D systems, each chiplet has an on-chip local network and an access router. The global network hooks up all the access routers using inter-chiplet links embedded in the interposer. Intra-chiplet packets travel through the local network, while inter-chiplet packets first travel through the local network to the access router of the source chiplet, then use the global network to reach the access router of the destination chiplet, and finally use the local network of the destination chiplet to reach the destination. The local network and the global network can be designed independently. For local networks, we explore Mesh (M) and Cmesh (CM) topologies (Figure 3(c)); while for global networks, we explore Mesh (M), Butterfly (BF), Butterdonut (BD) [5] and Ring (R) topologies, (see Figure 3(d)-(g)). We use $G-X-L-Y$ notation to denote a hierarchical network, where $X$ and $Y$ correspond to the global and local network topologies, respectively.

2) Physical Layer: Physical design of 2.5D systems determines the chiplet placement and a routing solution, subject to the chosen network topology. The placement of chiplets not only impacts the system temperature profile, but also affects the inter-chiplet link lengths. The routing solution affects the $\mu_b$umps and the inter-chiplet link transceivers that are placed along the peripheral regions of the chiplets.

$\mu_b$umps connect chiplets and the interposer. Inter-chiplet signals first exit the source chiplet through $\mu_b$umps, travel along the wires in the interposer, and then pass through $\mu_b$umps again to reach the destination chiplet. $\mu_b$umps are typically placed along the periphery of the chiplet, for the purpose of signal escaping [45]. The $\mu_b$ump area overhead is determined by the number of inter-chiplet channels, channel bandwidth, and $\mu_b$ump pitch. We list the $\mu_b$ump area overhead for various network topologies in Table II, where we use a 128-bit wide bus for each channel, $45 \mu m$ $\mu_b$ump pitch, and $4.5 \times 4.5 \times 5 \mu m$ chiplet size, and assume 20% additional $\mu_b$umps are reserved for power delivery and signal shielding [45]. Here, $w_{\mu_b}$ump indicates the stretch-out width from the chiplet edge to accommodate the $\mu_b$umps, as shown in Figure 4. In Table II, we also include Global Clos topology [46], which is a commonly used low-diameter-high-radix network. However, the area overhead is too high to make Clos a feasible inter-chiplet network option.

Inter-chiplet links can be routed on either a passive interposer or an active interposer. An active interposer enables better link bandwidth and latency because repeaters and flip-flops (for pipelining) can be inserted in the interposer [18]. However, an active interposer is expensive due to FEOL (front-end-of-line) process and yield loss. A passive interposer is a cost-effective alternative. The passive interposer is transistor-free, can be fabricated with BEOL (back-end-of-line) process, and inherently has high yield [18]. We conducted a study of the performance benefit of an active interposer over a passive interposer. We observed $2 \times$ to $3 \times$ latency improvement for the same link length, or 50% longer maximum allowed link length for the same throughput, but these benefits come at a $10 \times$ cost overhead ($500$ per wafer for passive interposer vs. $5000$ per wafer for active interposer [18]). Due to this cost overhead, we focus on the passive interposer in our present study. Active interposers, however, are currently being considered for 2.5D systems [20], [5]. Our methodology can be easily extended to active interposers, and we leave this as future work.

3) Circuit Layer: In the circuit layer, we explore multiple circuit designs for inter-chiplet links. Due to the high cost of an active interposer, we do not consider repeatered links. A link on a passive interposer is naturally repeaterless and non-pipelined. Such a link has limited performance, especially in 2.5D systems, where inter-chiplet links could reach a few
TABLE II: \( \mu \)bump count, stretch-out width of \( \mu \)bump region (\( w_{\mu\text{bump}} \)), and \( \mu \)bump area (\( A_{\mu\text{bump}} \)) overhead per chiplet for different network topologies designed using repeaterless links, 2-stage and 3-stage gas-station links.

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<td>#bumps</td>
<td>W_{\mu\text{bump}} (mm)</td>
<td>( A_{\mu\text{bump}} )%</td>
<td>( A_{\mu\text{bump}} )%</td>
<td>( A_{\mu\text{bump}} )%</td>
<td></td>
</tr>
<tr>
<td></td>
<td>149.6</td>
<td>74.2</td>
<td>0.405</td>
<td>39.2</td>
<td>39.2</td>
<td>39.2</td>
<td>21.0</td>
</tr>
</tbody>
</table>

Fig. 3: Logical view of network topologies. (a)-(b) are unified meshes, (c)-(g) are used to form hierarchical networks.

Fig. 4: Illustration of (a) chiplet placement on an interposer with logical connections, (b) a chiplet with \( \mu \)bump overhead, and (c) \( \mu \)bumps with TX/RX regions (not drawn to scale).

Fig. 5: Illustration of (a) top-down view and (b) cross-section view of inter-chiplet link implementation, and distributed wire models for (c) repeaterless link (Path 1 in (a)-(b)) and (d) gas-station link (Path 2 in (a)-(b)).

Essentially, a passive interposer cannot always ensure single-cycle communication latency due to signal degradation and rise/fall-time constraints. Hence, we explore a range of repeaterless inter-chiplet link (Path 1 in Figure 5) latencies from single cycle to five cycles, which corresponds to a variety of inter-chiplet link lengths (see Figure 6). This provides sufficient flexibility in chiplet placement. In addition, we use a novel ‘gas-station’ link design [1], which enables pipelining in a passive interposer, to overcome the performance loss. Our ‘gas-station’ link leverages flip-flops placed on other chiplets along the way to ‘refuel’ a passive link. As shown in Figure 5, Chiplet #2 is a gas station for Path 2 from Chiplet #1 to Chiplet #3, where signals first enter Chiplet #2 through \( \mu \)bumps, get repeated or retimed, and then return to the passive interposer through \( \mu \)bumps. Here we trade off \( \mu \)bump area overhead computed in Table II for performance. It is important to note the differences between an inter-chiplet repeaterless pipelined link and a gas-station link [1]. A repeaterless pipelined link requires an active interposer to house flip-flops and these flip-flops are designed using the active interposer’s technology node. A gas-station link only needs a passive interposer and inserts active elements in the intermediate chiplets. Thus, the active elements are designed using the chiplets’ technology node (22\( nm \) in our case). In our analysis, we set \( t_{\text{rise}}/t_{\text{cycle}} \) upper bound to be 0.5 and ensure full voltage swing at all nodes in the inter-chiplet link to account for non-idealities such as supply noise and jitter. We also explore \( t_{\text{rise}}/t_{\text{cycle}} \) of 0.8, which allows signals to go longer distances without repeaters. Relaxing the clock period or allowing for multi-cycle bit-periods permits us to use longer inter-chiplet links.

Figure 5(c) and (d) show the distributed circuit models in a passive interposer for repeaterless link and gas-station link, respectively. We model wire parasitics using a distributed, multi-segment \( \pi \) model. We use 22\( nm \) technology parameters for intra-chiplet components (drivers, receivers, repeaters, and flip-flops) and 65\( nm \) parameters for the inter-chiplet wires. Table III shows technology parameters used in our experiments. We calculate capacitance and resistance based on the model in Wong et al. [50], and we calibrate our stage and path delay estimates based on extraction from layout and Synopsys PrimeTime timing reports. Figure 6 shows maximum reachable

TABLE III: Technology node parameters.

<table>
<thead>
<tr>
<th>Technology Node</th>
<th>22( nm )</th>
<th>65( nm )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wire Thickness</td>
<td>300( \mu )m</td>
<td>1.5( \mu )m</td>
</tr>
<tr>
<td>Dielectric Height</td>
<td>300( \mu )m</td>
<td>0.3( \mu )m [35]</td>
</tr>
<tr>
<td>Wire Width</td>
<td>200( \mu )m</td>
<td>1( \mu )m [45]</td>
</tr>
<tr>
<td>( C_{\text{ds}} )</td>
<td>4.5( F/\mu )m</td>
<td>4.5( F/\mu )m [35]</td>
</tr>
<tr>
<td>( C_{\text{pp}} )</td>
<td>50( F )</td>
<td>50( F ) [35]</td>
</tr>
<tr>
<td>( C_{\text{ggd}} ) (Gate Cap)</td>
<td>1.05( F/\mu )m</td>
<td>1.05( F/\mu )m</td>
</tr>
<tr>
<td>( C_{\text{gdd}} ) (Drain Cap)</td>
<td>1.5 ( C_{\text{g}} )</td>
<td>1.5 ( C_{\text{g}} )</td>
</tr>
<tr>
<td>( R_{\text{t}} ) (Inverter resistance)</td>
<td>40( \Omega )/( \mu )m</td>
<td>100( \Omega )/( \mu )m</td>
</tr>
<tr>
<td>Driver NMOS Sizing</td>
<td>22( \mu )m x 100</td>
<td>65( \mu )m x 100</td>
</tr>
<tr>
<td>Wire Pitch</td>
<td>0.4( \mu )m</td>
<td>2( \mu )m [45]</td>
</tr>
<tr>
<td>Flip-Flop Energy Per Bit</td>
<td>14.7( f )J/bit [47]</td>
<td>28( f )J/bit [48]</td>
</tr>
<tr>
<td>Flip-Flop ( t_{\text{setup}} )</td>
<td>49( ps ) [47]</td>
<td>70.9( ps ) [49]</td>
</tr>
</tbody>
</table>
wirelengths that meet both the propagation time constraint and the rise-time constraint for various frequencies and cycles. For a given rise time constraint, as the inter-chiplet link latency constraint increases, the distance that a signal can travel in a single cycle increases. In a single cycle, a signal can travel more than 10 mm owing to the relaxed rise time constraint as well as low interconnect RC parasitics (i.e., due to using an older technology node for the interposer).

C. Evaluation Framework

1) System Performance Oracle: We construct a manycore system performance oracle that tells us the manycore system performance and core power for a given choice of network topology, voltage-frequency setting, link type, and link latency. We use Sniper [40] to precompute system performance. Our target system has 256 homogeneous cores, whose architecture is based on the IA-32 core from the Intel Single-Chip Cloud Computer (SCC) [51], with size and power scaled to 22 nm technology [52]. We divide the 256-core system into 16 identical chiplets.1 In Sniper, we implement the unified and hierarchical network models described in Section IV-B1. For inter-chiplet links, we use either passive links or gas-station links (see Section IV-B2). We vary link latency from one to five cycles for passive links and explore 2-stage and 3-stage pipelines for gas-station links. We explore three voltage-frequency settings: (0.9 V, 1 GHz), (0.8 V, 800 MHz), and (0.71 V, 533 MHz). We use multi-threaded benchmarks that cover high-power applications (Cholesky from SPLASH-2 suite [53]), medium-power applications (Streamcluster and Blackscholes from PARSEC suite [18]), and low-power applications (Latcont from SPLASH-2 suite). We fast-forward the sequential initialization region and simulate 10 billion instructions in the parallel region with all cores active to collect performance statistics. Then, we feed the performance results to McPAT [41] to compute the core power. We calibrate the McPAT power output with the measured power dissipation data of Intel SCC [51], scaled to 22 nm.

2) Cost Oracle: We construct a cost oracle that computes the manufacturing cost of 2.5D systems for a given choice of network topology, chiplet size and count, link type and stage count, and interposer size. We adopt the 2.5D manufacturing cost model published by Stow [19], which takes into account the cost and yield of CMOS chiplets, µ bump bonding, and the interposer. The model assumes known-good-dies. We enhance the cost model to account for the impact of µ bump overhead on the dies per wafer count and yield.

Equation (6) (see Table IV for all notations) computes the equivalent functional area of chiplets generated by dividing a 2D chip. Equation (7) evaluates the µ bump area overhead. Equations (8) and (9) determine the number of interposer dies and the number of CMOS dies, respectively, that can be cut from a wafer [19]. Here the first term counts the number of dies purely based on the wafer area and the die area, and the second subtraction term compensates for incomplete dies along the wafer periphery. In Equation (9), we take into account the µ bump area overhead. Equation (10) is the negative binomial yield model, where \( \Delta_{\text{bump}} \) is the defect density and \( \epsilon = 3 \) indicates moderate defect clustering [19]. Unlike the center area of chiplets that has high transistor density, the µ bump regions have very limited active regions that contain inter-chiplet link transmitters (TXs) and receivers (RXs). Only the defects occurring in the active regions would cause a failure, while the rest of the passive region is non-critical. Hence, our yield calculation (Equation (10)) uses only the critical active area. The yield of a passive interposer is as high as 98% [54] because it does not have any active components. Equations (11) and (12) calculate the per-die cost of the interposer and the chiplets, respectively. Equation (13) estimates the overall manufacturing cost of the 2.5D system by adding up the costs of the chiplets, the interposer, and bonding.

Figure 7 shows the manufacturing cost of 2.5D systems with respect to interposer sizes from 20 mm to 50 mm for two different µ bump stretch-out widths, which correspond to the minimum value (for G-R-L/M/CM topology without gas stations) and maximum value (for U-M topology with 3-stage gas-station links) in our experiments. The 2.5D system costs
Fig. 7: Comparison between the cost of a 2D system, and the cost of a 2.5D system estimated using prior cost models [7], [1] and our enhanced cost model for interposer sizes from 20nm to 50nm and µ bump stretch-out widths \( w_{\text{ubump}} \) of 0.09mm and 1.305mm, which correspond to the lower and upper limits of \( w_{\text{ubump}} \) in our analysis, respectively.

are normalized to the cost of 2D system. The 2.5D system cost increases with the interposer size. The cost model in our prior work [7] did not consider µ bump overhead and thus, the 2.5D system cost is independent of \( w_{\text{ubump}} \). The cost model in our latest work [1] overestimated the yield drop due to µ bump regions and thus, overestimated the overall cost. This error of this cost model [1] is trivial with a small \( w_{\text{ubump}} \), but with a large \( w_{\text{ubump}} \), the error is not negligible (up to 10% of the 2D system cost in our example). With a small \( w_{\text{ubump}} \), the predicted cost of a 2.5D system using our enhanced model is cheaper than the cost of a 2D system, when the interposer is smaller than 40mm × 40mm. With a large \( w_{\text{ubump}} \), the predicted cost of a 2.5D system using our enhanced model is always higher than that of a 2D system. This eliminates some network topologies, such as Clos, that require large \( w_{\text{ubump}} \).

3) Interconnect Performance Oracle: We build an interconnect performance oracle that analyzes the maximum reachable length of inter-chiplet link for a given operating voltage and frequency, rise-time constraint, and propagation time constraint in the unit of cycles. We use HSPICE [42] to simulate the link models discussed in Section IV-B3. The TX circuit is designed using up to six (the exact number depends on the wirelength) cascaded inverters with standard fan-out of 4, and the RX circuit consists of two cascaded inverters of the minimum size. We estimate the TX and RX area using the physical layout of the standard inverter cell in NanGate 45nm Open Cell Library [48], and scale it down to 22nm technology. The area of TX and RX logic \( A_{\text{TXRX}} \) takes up less than 1% of the µ bump area. The interposer wire resistance is \( 14.666 \times 10^{-3} \Omega/\mu m \) and the capacitance is \( 114.726 \times 10^{-3} fF/\mu m \), for the wire dimensions provided in Table III for 65nm technology. Since the inter-chiplet link latency is wire dominated, we set a sizing upper limit of 100× the minimum size for the last inverter in the set of cascaded inverters of TX in 22nm technology since the drivers are placed in chiplets instead of the interposer. We do not increase the size beyond 100× because we do not observe latency improvement. For the workloads that we have considered, the inter-chiplet link power is up to 22W, which is insignificant compared to the total average system power of 508W. Hence, inter-chiplet link power has negligible influence on chiplet placement.

4) Thermal Simulation: We use HotSpot [43] to simulate thermal profiles for given chiplet placement choices and core power values. We use an extension of HotSpot [55] that provides detailed heterogeneous 3D modeling features. To model our 2.5D system, we stack several layers of different thickness and heterogeneous materials on top of each other and model each layer with a separate floorplan on a 64×64 grid. Our 2.5D system model follows the properties (such as layer thickness, materials, dimensions of bumps and TSVs) of real systems [12], [11]. We use the HotSpot default conventions for the thermal interface material properties, the ambient temperature of 45°C, and the sizing of the spreader and the heatsink such that the spreader edge size is 2× the interposer edge size and the heatsink edge size is 2× the spreader edge size. To keep the heat transfer coefficient consistent across all simulations, we adjust the convective resistance of the heatsink.

We implement a linear model of temperature-dependent leakage power based on published data of Intel 22nm processors [56]. We assume 30% of power is due to leakage at 60°C [52]. We update the core power to include the leakage power based on initial temperature obtained from HotSpot and iterate the thermal simulation. In all of our studies, the leakage-dependent temperature quickly converges after two iterations.

Figure 8 shows the temperature of the best chiplet placement for each interposer size, while running Cholesky benchmark with Mesh network using single-cycle links without gas stations. As the interposer size increases, the peak temperature decreases due to the increasing flexibility of chiplet placement. Although the main direction of heat dissipation is vertical through the heatsink on top of the system and the lateral heat transfer is relatively weak, the effect of lateral heat flow is sufficient to motivate thermally-aware chiplet placement [57]. The temperature benefit shown in Figure 8 comes at the cost of a larger interposer. The cost of the interposer has been accounted in our cost model and the user can adjust the cost weight in the objective function for different design needs.

5) Routing Optimization: We build an MILP to solve for the optimal routing solution and the corresponding maximum wirelength given the logical network topology, chiplet placement, link stage count, and µ bump resources. The MILP objective is a weighted function of the maximum length of a route on the interposer and the total routing area overhead. We group the µ bumps along the chiplet periphery into pin clumps to limit the problem size and the MILP runtime. We use 4 pin clumps per chiplet in our experiments. We frame the delivery of required number of wires between chiplets as multi-commodity flow, and formulate the MILP to find optimal
TABLE V: Notations used in routing optimization.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P$</td>
<td>Set of pin clumps.</td>
</tr>
<tr>
<td>$N$</td>
<td>Set of nets.</td>
</tr>
<tr>
<td>$c, i, j$</td>
<td>Index of a chiplet $c \in C$.</td>
</tr>
<tr>
<td>$p, j, k$</td>
<td>Index of a pin clump $p \in P$.</td>
</tr>
<tr>
<td>$n$</td>
<td>Set of pin clumps.</td>
</tr>
<tr>
<td>$t_n$</td>
<td>Source chiplet of net $n$.</td>
</tr>
<tr>
<td>$s_n$</td>
<td>Sink chiplet of net $n$.</td>
</tr>
<tr>
<td>$x_{p,j}$</td>
<td>Distance from pin clump $h$ to pin clump $k$ on chiplet $j$.</td>
</tr>
<tr>
<td>$f_{ihj,k}^n$</td>
<td>Pin capacity for a pin clump $h$ on chiplet $j$.</td>
</tr>
<tr>
<td>$R_{ij}$</td>
<td>Input requirement on the wire count between chiplet $i$ and chiplet $j$.</td>
</tr>
<tr>
<td>$f_{ihj,k}$</td>
<td>Flow variable. Number of wires from pin clump $h$ of chiplet $i$ to pin clump $k$ of chiplet $j$ that belong to net $n$.</td>
</tr>
<tr>
<td>$\lambda_{ihj,k}^n$</td>
<td>Binary indicator for a route between pin clump $h$ on chiplet $i$ to pin clump $k$ on chiplet $j$ belonging to net $n$.</td>
</tr>
<tr>
<td>$S_{max}$</td>
<td>Maximum permissible segment count allowed for any route; a segment is defined as a route between chiplets. For the case where no gas stations are permitted, $S_{max} = 1$. Permitted values of $S_{max}$ include 1, 2 or 3.</td>
</tr>
<tr>
<td>$\theta$, $\varphi$</td>
<td>Coefficients for the objective function of routing optimization.</td>
</tr>
</tbody>
</table>

TABLE VI: Inputs to routing optimization.

<table>
<thead>
<tr>
<th>Input</th>
<th>Properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chiplets</td>
<td>$</td>
</tr>
<tr>
<td>Pin Clumps</td>
<td>$</td>
</tr>
<tr>
<td>Required Connections</td>
<td>$R_{ij} &gt; 0$ then a net $n$ exists between chiplet $i$ and chiplet $j$ with source $s_n = i$ and sink $t_n = j$.</td>
</tr>
<tr>
<td>Routing Rules</td>
<td>Maximum number of segments $S_{max}$, equal to 1, 2 or 3.</td>
</tr>
</tbody>
</table>

Routing solutions that comprehend the finite availability of $\mu$bumps in each pin clump.

Table V describes the notations used in the MILP. We use ILOG CPLEX v12.5.1 to implement and run the MILP. The number of variables and constraints in the MILP instance are both bounded by $O(|C|^2 \cdot |P|^2 \cdot |N|)$. For our 16-chiplet design, $|N|$ is 48 for Mesh/Cmesh, 56 for Butterdonut, 64 for Butterfly and 32 for Ring networks. The outputs of our MILP implementation are the optimal value of the objective function and the values of the variables $f_{ihj,k}^n$, which describe the routing solution and $\mu$bump assignment to pin clumps.

Based on the inputs to the routing optimization step (see Table VI), we precompute $d_{ihj,k}$, the routing distance (assuming Manhattan routing) from pin clump $h$ on chiplet $i$ to pin clump $k$ on chiplet $j$, using Equation (14). Equation (15) is the objective function for the MILP that includes the maximum length $L$, and the total length of the routes. In all reported experiments, we set $\theta = 1$ and $\varphi = 0$. Equation (16) ensures that the flow variable $f_{ihj,k}^n$ is a non-negative number. Equation (17) is the flow constraint governing the flow variables $f_{ihj,k}^n$. It guarantees the sum of all flows for a net $n$, over all pin clumps from chiplet $s_n$ to chiplet $t_n$, meets the $R_{ij}$ requirement. It also makes sure that net flow is 0 for all other (non-source, non-sink) chiplets for the given net. $\sum_{h \in P, j \in C, k \in P} f_{ihj,k}^n$ is the outgoing flow of chiplet $i$, while $\sum_{h \in P, j \in C, k \in P} f_{ihj,k}^n$ is the incoming flow of chiplet $i$. Equation (18) assures that there is no input flow (for net $n$) for any pin clump in the source chiplet $s_n$ from any other chiplet’s pin clump. Similarly, Equation (19) ascertain that there is no output flow (for net $n$) for any pin clump in the sink chiplet $t_n$ to any other chiplet’s pin clump. Equation (20) maintains that the sum of input and output flows from a given pin clump is always less than or equal to the capacity of the pin clump. This insures that all routes have availability of pins. Equation (21) defines $\lambda_{ihj,k}^n$ as a boolean value based on $f_{ihj,k}^n$. This helps identify the maximum route length $L$, as shown in Equation (22). Equation (23) constrains the maximum number of segments $(S_{max})$ to be either 1, 2 or 3. A segment is defined as a portion of the net connecting two chiplets. If $S_{max} = 1$, then the net connects $s_n$ and $t_n$ directly, and no gas stations are permitted, while if $S_{max} = 2$ or $S_{max} = 3$, then gas stations are permitted, where the net connects $s_n$ and $t_n$ through 1 or 2 other chiplets respectively, i.e. gas station hops.

$$f_{ihj,k}^n \geq 0, ~ \forall i \in C, h \in P, j, p \in j, k \in P, n \in N$$

$$\lambda_{ihj,k}^n = \begin{cases} 1 & \text{if } f_{ihj,k}^n > 0, \forall i \in C, h \in P, j, p \in j, k \in P, n \in N \\ 0 & \text{otherwise, } \forall i \in C, h \in P, j, p \in j, k \in P, n \in N \end{cases}$$

$$L \geq d_{ihj,k} \cdot \lambda_{ihj,k}^n, ~ \forall i \in C, h \in P, j, p \in j, k \in P, n \in N$$

**D. Thermally-Aware Placement Algorithm**

Our thermally-aware PNR tool supports arbitrary chiplet placements that consider non-matrix and asymmetric chiplet organization styles while searching for the optimal placement for each table entry. Including arbitrary placements, the solution space explodes to quadrillions ($10^{15}$) placement options with $1mm$ granularity. It is impractical to exhaustively search such a vast space. In addition, the solution space is non-convex. Approaches like gradient descent or greedy search [7] can easily get trapped in a local minima. Therefore, we use simulated annealing to explore chiplet placement and find the optimal placement solution that gives lowest peak temperature while maintaining the maximum wirelength. Simulated annealing is a probabilistic technique to approximate the global optimum. We introduce the key components of our algorithm below.

**Placement Description.** Prior works [7], [1] only consider $4 \times 4$ matrix-style chiplet placement, which covers a small portion of the overall solution space and the chiplets have limited freedom to move. For example, the corner chiplets cannot move, the edge chiplets can only slide along the periphery of the interposer, and the center chiplets can only slide along the interposer diagonal. Thus, the previous approach of matrix-style chiplet placement cannot cover the cases where the four chiplets along an edge of the interposer do not align or the cases where the first row does not always have four chiplets. In addition, the previous assumption of 4-fold rotational symmetry does not allow us to ever find the
optimal placement for some topologies. For Butterdonut and Butterfly networks, because of the 4-fold rotational symmetry, the maximum wirelength cannot be shortened with chiplet movement due to the connection between a chiplet and its reflection in any one of the remaining quadrants. Therefore, we enhance our cross-layer co-optimization methodology to support arbitrary placement and relax our symmetry assumption to 2-fold rotational symmetry. We use x- and y-coordinates to specify the locations of the first eight chiplets, and the coordinates of the remaining eight chiplets are based on the rotational image of the first eight. We assume 1mm granularity for placement, such that the coordinates of the center of each chiplet has to be positive integer numbers. The chiplets cannot overlap with each other and there is a 1mm guardband along the interposer periphery. The minimum gap between two chiplets is 0.1mm [12], [58].

**Neighbor Placement.** A neighbor placement is the placement obtained by either moving a chiplet by the minimum step size in any of the 8 directions (N, S, E, W, NE, NW, SE, SW) or swapping a pair of chiplets from a current placement. Without swapping, it is likely to have a ‘sliding tile puzzle’ issue. For instance, a chiplet cannot move in some directions because other chiplets block the way, especially when the interposer size is small.

**Acceptance Probability.** The decision of whether a neighbor placement is accepted or not depends on the delta calculated using Equation (24). Here \( T_{curr}, L_{curr}, T_{nei}, L_{nei} \) are the peak temperature of current placement, the longest wirelength of current placement, the peak temperature of neighbor placement, and the longest wirelength of neighbor placement, respectively. When both the current placement and the neighbor placement meet the wirelength constraint, we emphasize the temperature difference when calculating delta. Similarly, when either the neighbor or the current placement violates the wirelength constraint, we emphasize the wirelength difference while calculating delta as there is no point in considering temperature because we do not have a viable solution. We compute the acceptance probability \( AP \) using Equation (25), where \( K \) is the annealing temperature. Here \( K \) decays from 1 to 0.01 with a factor of 0.8 every \( v \) iterations, where \( v \) is proportional to the interposer edge width \( w_{int} \). We accept the neighbor placement if \( AP \) is greater than a random number between 0 and 1. In the case that a neighbor placement is better (\( \delta > 0 \)), \( AP \) evaluates to greater than 1 and we are forced to accept the neighbor placement. In the case that a neighbor placement is worse (\( \delta < 0 \) and \( 0 < AP < 1 \)), there is still a nonzero probability of accepting the worse neighbor placement to avoid being trapped in a local minima. The worse a neighbor placement is, the lower is the probability of accepting it. As the annealing temperature \( K \) decays, the solution converges since the probability of accepting a worse neighbor placement decreases.

\[
\delta = \begin{cases} 
0.9 \times (T_{curr} - T_{nei}) + 0.1 \times (L_{curr} - L_{nei}), & \text{if } L_{curr} \leq L_{th} \text{ and } L_{nei} \leq L_{th} \\
0.1 \times (T_{curr} - T_{nei}) + 0.9 \times (L_{curr} - L_{nei}), & \text{if } L_{curr} > L_{th} \text{ or } L_{nei} > L_{th}
\end{cases}
\]

\[
AP = e^{\frac{-\delta}{K}}, \text{ accept if } AP > \text{rand}(0, 1)
\]

**Multi-Start and Multi-Phase Techniques.** As a probabilistic algorithm, simulated annealing approximates the global minimum but provides no guarantee to find it. It is also challenging to find a good enough solution due to the astronomical non-convex solution space (up to quadrillions of placement options) and the limited simulation time (up to a thousand moves). In order to improve the solution quality of simulated annealing, we adopt multi-start and multi-phase techniques. For multi-start, we repeat the thermally-aware PNR process ten times for each table entry and pick the placement solution which has the lowest peak temperature and meets the routing constraint. Given the probabilistic nature of the simulated annealing algorithm, the multi-start technique is helpful in reducing the chance of getting a poor solution. We can run the multiple starts of the multi-start technique in parallel, so as not to increase the time required to arrive at the solution. For multi-phase, we map an existing placement solution of a smaller interposer to a larger interposer (while keeping all the other tuning knobs the same) and use it as the initial starting placement to find the placement solution for the larger interposer. This improves the quality of the final placement solution for a table entry without increasing the simulation time or the electricity bill. The multi-phase step size must be a multiple of 2mm since we assume 1mm placement granularity. A smaller step size yields better solution quality, but requires longer actual simulation time. In our case, we set the multi-phase step size to 4mm, which provides a good balance between the simulation time and the solution quality.

**V. Evaluation Results**

In this section, we first provide the maximum performance and the optimal chiplet placement for various networks. We compare the maximum performance using our new approach against the prior work [1], with and without gas stations. Next, we present the iso-cost performance improvement, the iso-performance cost reduction using our new approach, and the Pareto Frontier curve of performance and cost. We then show the thermal maps for high-power, medium-power, and low-power applications on their respective optimal chiplet placement solution. In addition, we evaluate the running of medium-power and low-power applications on the optimal chiplet solution for a high-power application. Lastly, we conduct a sensitivity analysis to show the optimal combinations of performance, cost and peak temperature with respect to different temperature thresholds and different choices of constraints.

**A. Optimal Chiplet Placement Analyses**

Figure 9 shows the maximum performance, the corresponding cost and the corresponding peak operating temperature for various networks and link designs running the high-power Cholesky benchmark for three different approaches. Here the focus is on performance. The first approach corresponds to our prior work [1] that only considers matrix-style chiplet placement (Mat) and a hard temperature constraint (HTC) of 85°C, with and without gas stations. We use Mat-HTC-GS and Mat-HTC-noGS to denote these cases. The second approach uses the same HTC of 85°C but allows arbitrary placement of chiplets (Arb). We use Arb-HTC-GS and Arb-HTC-noGS to
denote these cases. The third approach uses a soft temperature constraint (STC) of 85°C and arbitrary placement, as described in Section IV-D. We use Arb-STC-GS and Arb-STC-noGS to denote these cases.

For the mesh-like networks (G-M-L-M, G-M-L-CM, U-M, and U-CM), our Arb-HTC approach does not improve the performance over the previous Mat-HTC approach [1]. This is because the previous approach already achieves the maximum performance for G-M-L-M, G-M-L-CM, and U-M, while for U-CM, there is not much room for improvement with arbitrary placement since the optimal placement also follows a matrix style. However, we achieves a 8-19% (11% on average) reduction in cost. The Arb-STC approach achieves the highest performance (10% improvement) with U-CM network at a manufacturing cost which is equal to the Mat-HTC-noGS case, while exceeding the temperature threshold by less than 0.5°C. For the remaining three mesh-style networks, the Arb-STC approach does not improve performance but it does reduce cost in some cases. Even when using our thermally-aware PNR tool with the option of arbitrary placement, the optimal chiplet placements are matrix style. Since these four mesh-like networks have similar optimal placement patterns, we just show the logical connection and thermal map of U-CM network in Figure 10(a).

For Butterfly networks, the Arb-STC-GS approach achieves the same maximum performance as achieved using Mat-HTC-GS approach [1] and reduces the cost by 5% (see Figure 9). The optimal placement for Butterfly network is shown in Figure 10(b). Note in the top subfigure, we only show the logical connections instead of actual routing path of gas-station links. For Butterdonut networks, the Arb-STC-GS approach improves the performance by 25% without increasing the cost (see Figure 9). Figure 10(c) shows the optimal placement for Butterdonut network. The Ring networks (G-R-L-M/CM) are not included in the prior work [1], thus we do not show the comparison. The chiplets are distributed along the periphery of the interposer in the optimal placement for the Ring topology (see Figure 10(d)), which is good for heat dissipation. Thus, the performance of the Ring topology saturates at a relatively small interposer size, and we observe lower cost and temperature than those of other networks (see Figure 9).

**B. Iso-cost and Iso-performance Analyses**

Figure 11 shows the iso-cost performance for various networks running Cholesky benchmark, while not exceeding the cost of a 2D system. In general, our Arb-HTC approach improves the iso-cost performance by 13-37% (20% on average), and our Arb-STC approach improves the iso-cost performance by 40-68% (49% on average), compared to our prior Mat-HTC approach [1]. The previous work [1] shows that the U-M network cannot be implemented feasibly due to the large µbump area overhead and the incorrectly estimated yield drop. Using our more accurate cost model, it is actually feasible to implement the U-M network within the cost budget.

Figure 12 shows the iso-performance cost and the corresponding peak temperature for each network. Here, for each network, we match the performance of the 2.5D system designed using our proposed approach with the corresponding maximum performance of the 2.5D system designed using prior Mat-HTC approach [1] when running Cholesky benchmark. The cost values are normalized to the cost of a 2D system. Under the same hard temperature constraint as the prior work [1], our Arb-HTC approach reduces manufacturing cost by 5-20% (14% on average) without lowering the performance. Using the Arb-STC approach, we can push the iso-performance cost saving to 30-38% (32% on average) with up to 91°C overall system peak temperature.

Figure 13 shows the Pareto Frontier Curve of normalized performance (1/IPS) and normalized cost using Mat-HTC approach [1], Arb-HTC approach, and Arb-STC approach. Our arbitrary placement pushes the Pareto frontier curve towards...
and placement solutions using medium-power application, we get identical network choices between chiplets and forms a matrix-style placement. For chiplet links without gas stations temperature threshold by 0.5 15% lower cost. The improvement is achieved by violating the condition approach [1] and reduce the manufacturing cost by 19%, 14%, 9%, and 3% for high-power, medium-power, and low-power applications, respectively. The equivalent performance is achieved at a smaller interposer size where the chiplets are pushed to the periphery of the interposer to ease the heat dissipation. For high-power and medium-power applications, 2-stage gas-station links are used, which provides flexibility in chiplet placement to form a ring shape for mesh-like networks, while for low-power application, such a ring shape placement is not feasible as we need to provide routability of single-cycle links.

Using Arb-STC approach, for high-power application, we can achieve the maximum possible performance (3% higher than both Mat-HTC approach [1] and Arb-HTC approach) and 15% lower cost. The improvement is achieved by violating the temperature threshold by 0.5°C and using single-cycle inter-chiplet links without gas stations, which constrains distance between chiplets and forms a matrix-style placement. For medium-power application, we get identical network choices and placement solutions using Arb-STC and Arb-HTC approaches. For low-power application, our Arb-STC approach achieves the maximum possible performance while violating the temperature threshold by 1.4°C. This improvement also comes with 40% cost overhead, but in this example, cost is not our concern. The chiplets cluster in the center of the interposer to meet single-cycle latency constraint for a butterfly topology, and leave large empty space on the edges of the interposer to help heat dissipation.

It should be noted that the results we show in Figure 14 assume that we know what application will be running at the design time, and we optimize for each application. For unknown target applications or a mix of known and unknown applications, we optimize for the worst-case (highest power application) scenario at the design time, and run the target application on the optimized organization (including network topology, interposer size, chiplet placement, and inter-chiplet link design). For example, if a system is expected to run high-power (Cholesky), medium-power (Streamcluster), and low-power (Lu.cont) applications, we design and optimize the system using the high-power application. When running medium-power application on the system optimized for high-power application, we observe the same performance, 23% higher cost, and 6°C lower temperature compared to that of a system custom designed for medium-power application. When running low-power application on the system designed for high-power application, we observe 5% lower performance, 5% higher cost, and 12°C lower temperature compared to that of a system custom designed for low-power application.

D. Analyses of Cross-layer Co-optimization Benefits

To understand the benefits of co-optimizing across multiple design layers simultaneously, we conduct a comparison between cross-layer and single-layer methodologies while running the Blacksholes benchmark. We compare multiple cases in Table VII. The baseline is the optimal solution of our cross-layer co-optimization methodology. We use three letters
to represent the choices at each of the logical, physical, and circuit layers, for the remaining nine cases. Here O means optimal, W means worst possible, F means prefixed, B means best possible. So for example, the OOW case corresponds to the use of the same design choices as the optimal cross-layer solution at the logical and physical layers, and use of the worst possible choice at the circuit layer. This case shows the contribution of the circuit layer in our cross-layer co-optimization methodology. In the FFB case, we fix the design choices at the logical and physical layers, and only optimize the circuit layer. We report performance improvement, cost increase, and temperature for each case. To better compare the different cases, we use the Performance/Unit Cost metric. For the OOW and OWO cases, we observed a cost reduction and/or slight performance improvement, but at a high infeasible peak temperature. For the case of WOO, the temperature is acceptable but we get 20% lower performance and 50% higher cost. For the cases of FFB, FBW, BFF, and BFB, we get either higher performance at higher cost or lower performance at lower cost, but the temperature becomes infeasibly high. For the cases of FFB and BBF, the temperature is safe, while performance and cost offset each other. In terms of the Performance/Unit Cost metric, our cross-layer co-optimization approach performs better than all cases except OOW, OWO and BFF, but these cases have high infeasible temperature.

E. Sensitivity Analysis

We conduct a sensitivity analysis (see Figure 15) to show the optimal combinations of performance, cost and peak temperature, and the corresponding objective function values with respect to different temperature thresholds from 75°C to 95°C and different temperature constraint choices (including hard temperature constraint, soft temperature constraint with linear and square penalty functions, and no temperature constraint). We choose the weights to be \((\alpha, \beta, \gamma) = (0.8, 0.1, 0.1)\) as an example for a performance-focused objective function. 

With no temperature constraint, we can always achieve the maximum performance and the lowest cost, at a temperature of 93.2°C. Thus, with a temperature threshold of 94°C or higher, the optimal performance, cost, and temperature combinations with different constraint choices are the same. With a hard temperature constraint, any case that exceeds the temperature threshold is considered as infeasible, thus, the peak temperature is close to, but below the temperature threshold. As the temperature threshold increases, there are more feasible design choices and the objective function value decreases. A soft temperature constraint allows violating the temperature threshold and translates the violation into a penalty in the objective function. The soft temperature constraint approach provides more choices and thus is guaranteed to have a solution that better or equal to that obtained using hard temperature constraint approach. For the soft temperature constraint approach with a linear penalty function, we are allowed to violate the temperature threshold only slightly to find a solution that has higher performance and/or lower cost than the hard temperature constraint approach. A square penalty function suppresses the penalty for a small violation and highlights the penalty for a large violation of the temperature threshold. Thus, with a soft temperature constraint approach with the square penalty function, we can achieve higher performance and lower cost compared to the case with the linear penalty function. For example, with a temperature threshold of 80°C, the result with the hard temperature constraint has lowest performance. With the soft temperature constraint with the linear penalty function, we violate the temperature threshold by 0.59°C and achieve 6% higher performance but at 5% higher cost compared to the hard temperature constraint approach. With the soft temperature constraint with the square penalty function, we violate the temperature threshold by 0.93°C and achieve 5% higher performance at the same cost compared to the hard temperature constraint approach.

VI. Conclusion

In this paper, we introduce a cross-layer co-optimization methodology for network design and chiplet placement in 2.5D systems. Our methodology optimizes network topology design, inter-chiplet link design, and chiplet placement across logical, physical, and circuit layers to jointly improve performance, lower manufacturing cost, and reduce operating temperature. Compared to our prior work, we improve the optimization methodology by enhancing the cost model, including operating temperature in the optimization goal, applying a soft temperature constraint, and improving the optimization algorithm to enable arbitrary chiplet placement. Our new methodology shifts the performance-cost Pareto tradeoff curve for 2.5D systems substantially. Our approach improves thermal constrained performance by 88% at the same manufacturing cost and reduces the cost by 29% at the same performance in comparison to 2D systems. Compared to our prior work [1], for the same hard temperature constraint our enhanced placement algorithm with arbitrary placement improves iso-cost performance by 13-37% (20% on average) and reduces iso-performance cost by 5-20% (14% on average). Overall, our new optimization methodology with a soft temperature con-

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**TABLE VII: Cross-layer vs. single-layer optimization.**

<table>
<thead>
<tr>
<th>Case</th>
<th>Perf Improvement</th>
<th>Cost Increase</th>
<th>Temperature [°C]</th>
<th>Perf/Unit Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cross-layer</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>OOW</td>
<td>-0%</td>
<td>-30%</td>
<td>99.9</td>
<td>3.30</td>
</tr>
<tr>
<td>OWO</td>
<td>0%</td>
<td>-22%</td>
<td>138.0</td>
<td>3.37</td>
</tr>
<tr>
<td>WOQ</td>
<td>-0%</td>
<td>-50%</td>
<td>94.2</td>
<td>1.99</td>
</tr>
<tr>
<td>FFB</td>
<td>-39%</td>
<td>-14%</td>
<td>100.9</td>
<td>2.88</td>
</tr>
<tr>
<td>FBB</td>
<td>9%</td>
<td>-11%</td>
<td>102.5</td>
<td>2.92</td>
</tr>
<tr>
<td>BBF</td>
<td>-10%</td>
<td>-50%</td>
<td>95.4</td>
<td>2.09</td>
</tr>
<tr>
<td>BBF</td>
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<td>-14%</td>
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<td>0.79</td>
</tr>
<tr>
<td>BFB</td>
<td>-35%</td>
<td>-5%</td>
<td>100</td>
<td>3.09</td>
</tr>
<tr>
<td>BFB</td>
<td>2%</td>
<td>3%</td>
<td>86.2</td>
<td>3.06</td>
</tr>
</tbody>
</table>

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category and arbitrary placement achieves 40-68% (49% on average) higher iso-cost performance and 30-38% (32% on average) lower iso-performance cost over our prior work [1].

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REFERENCES

Authors: Photos and bios unavailable.