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ENG EC/ME/SE 501:

**Exercises (Set 2)** (Due 10/1/24)

1. For the following two matrices:

$$\mathbf{A} = \begin{pmatrix} -2 & 0 & -1 \\ 4 & 2 & 4 \\ 0 & 0 & -1 \end{pmatrix} \quad \mathbf{B} = \frac{1}{8} \begin{pmatrix} 9 & 0 & -3 \\ 10 & -8 & 2 \\ 3 & 0 & -1 \end{pmatrix}$$

find (a) the characteristic polynomial; (b) the determinant and trace; (c) the eigenvectors.

2. Find the Jordan Normal Form  $\mathbf{J}_{\mathbf{A}}$  of

$$\mathbf{A} = \begin{pmatrix} 5 & -7 & 4 \\ 8 & -7 & 4 \\ 12 & -12 & 7 \end{pmatrix}.$$

3. For the matrix in Problem 2, find a nonsingular matrix (change of basis)  $\mathbf{U}$  such that

$$\mathbf{U}^{-1} \cdot \mathbf{A} \cdot \mathbf{U} = \mathbf{J}_{\mathbf{A}}.$$