

Inequality and Unemployment in a Global Economy

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- Two fundamental Issues in Economics
 - Allocation of resources across economic activities
 - Distribution of incomes across factors of production
- Contributions of this paper:
 - Develops a rich, flexible and tractable model for examining the impact of trade on these two issues
 - Provide predictions regarding trade, inequality and unemployment that match features of the data

- Trade and inequality with neoclassical labor market
 - Yeaple (2005) and Bustos (2009)
 - Ohnsorge and Trefler (2007) and Costinot and Vogel (2009)
 - Burstein and Vogel (2009)
- Trade, unemployment and inequality with labor market frictions
 - Davis and Harrigan (2008)
 - Egger and Kreickemeier (2009a,b) and Amiti and Davis (2009)
 - Felbermayr et al. (2008, 2009) and Helpman and Itskhoki (2000a)

- Framework

- Use standard Diamond-Mortensen-Pissarides search and matching frictions into a Melitz (2003) model.
- Introduce ex-post match specific heterogeneity in a worker's ability.

- Model Setup

- Two countries: Home and Foreign (foreign is denoted by asterisk)
- Continuum of risk neutral workers who are *ex ante* identical.
- Real consumption index for the sector Q is

$$Q = \left[\int_{j \in J} q(j)^\beta dj \right]^{1/\beta}, \quad 0 < \beta < 1$$

$$q(j) = A^{1/1-\beta} p(j)^{-1/1-\beta}$$

- Equilibrium revenue is:

$$r(j) = p(j)q(j) = Aq(j)^\beta$$

Where $p(j)$ and $q(j)$ are price quantity of variety j , respectively, and A is a demand-shifter.

- Sunk entry cost is f_e , f_d is production fixed cost, and f_x is export fixed cost. θ denotes productivity parameter, which follows a Pareto distribution ($G_\theta(\theta) = 1 - (\theta_{min}/\theta)^z$ where $z > 1$).

- τ denotes iceberg variable trade cost
- Output is given by:

$$y = \theta h^\gamma \bar{a}$$

where y denotes output, h denotes measure of worker hired and \bar{a} denotes average ability of workers

- Ability a is drawn from a Pareto distribution:

$$G_a(a) = 1 - (a_{min}/a)^k$$

for $a \geq a_{min} > 0$ and $k > 1$

- b is the search cost and ca_c^δ/δ is the screening cost where $c > 0$ and $\delta > 0$ and a_c is the cutoff ability.

- For a screening threshold a_c we have;

$$h = n\left(\frac{a_{min}}{a_c}\right)^k, \quad \bar{a} = \frac{k}{(k-1)}a_c$$

- Higher screening \Rightarrow higher average ability and lower hired worker. Screen will increase output if k is sufficiently low.
- Firm and worker bargain to share the revenue, corresponding shares are:
Firm's share = $\frac{1}{1+\beta\gamma}$, Workers' share = $\frac{\beta\gamma}{1+\beta\gamma}$

- Firms profit maximization problem is given by;

$$\max_{\substack{n \geq 0, \\ a_c \geq a_{\min}, \\ I_x \in \{0,1\}}} \left\{ \frac{1}{1 + \beta\gamma} \left[1 + I_x \tau^{-\frac{\beta}{1-\beta}} \left(\frac{A^*}{A} \right)^{\frac{1}{1-\beta}} \right]^{1-\beta} A \left(\kappa_y \theta n^\gamma a_c^{1-\gamma k} \right)^\beta - bn - \frac{c}{\delta} a_c^\delta - f_d - I_x f_x \right\}$$

- First order conditions are:

$$\frac{\beta\gamma}{1 + \beta\gamma} r(\theta) = bn(\theta)$$

$$\frac{\beta(1 - \gamma k)}{1 + \beta\gamma} r(\theta) = ca_c(\theta)^\delta$$

- From first order conditions we get:

$$w(\theta) = \frac{\beta\gamma}{1 + \beta\gamma} \frac{r(\theta)}{h(\theta)} = b \frac{n(\theta)}{h(\theta)} = b \left[\frac{a_c(\theta)}{a_{min}} \right]^k$$

$$r(\theta) = \kappa_r \left[c^{-\frac{\beta(1-\gamma k)}{\delta}} b^{-\beta\gamma} \Upsilon(\theta)^{(1-\beta)} A \theta^\beta \right]^{\frac{1}{\Gamma}}$$

$$\pi(\theta) = \frac{\Gamma}{1 + \beta\gamma} r(\theta) - f_d - I_x(\theta) f_x$$

where $\Gamma \equiv 1 - \beta\gamma - \beta(1 - \gamma k)/\delta$ and $\Upsilon(\theta) \equiv 1 + I_x(\theta) \tau^{-\frac{\beta}{1-\beta}} \left(\frac{A^*}{A} \right)^{\frac{1}{1-\beta}}$

- Labor market tightness and search cost
 - Search cost in standard Diamond-Mortensen-Pissarides is

$$b = \alpha_0 x^{\alpha_1}, \quad \alpha_0 > 1, \quad \alpha_1 > 0$$

- Equilibrium search condition for worker is

$$\omega = xb, \quad \text{where} \quad b = \frac{\omega(\theta)h(\theta)}{n(\theta)}$$

- From these two conditions we get

$$b = \alpha_0^{\frac{1}{1+\alpha_1}} \omega^{\frac{\alpha_1}{1+\alpha_1}} \quad \text{and} \quad x = \left(\frac{\omega}{\alpha_0}\right)^{\frac{1}{1+\alpha_1}}$$

Where $\alpha_0 > \omega$ so that $0 < x < 1$

- Productivity cutoff and Demand

- Exit cutoff (θ_d) is determined by zero profit condition

$$\frac{\Gamma}{1 + \beta\gamma} \kappa_r [c^{-\frac{\beta(1-\gamma k)}{\delta}} b^{-\beta\gamma} A \theta_d^\beta]^{\frac{1}{\Gamma}} = f_d$$

- Export cutoff (θ_x) is determined by firm's indifference between catering domestic or foreign market

$$\frac{\Gamma}{1 + \beta\gamma} \kappa_r [c^{-\frac{\beta(1-\gamma k)}{\delta}} b^{-\beta\gamma} A \theta_d^\beta]^{\frac{1}{\Gamma}} [\Upsilon_x^{(1-\beta)/\Gamma} - 1] = f_x$$

- Demand shifter (A) is determined free entry condition

$$f_d \int_{\theta_d}^{\infty} [(\frac{\theta}{\theta_d})^{\frac{\beta}{\Gamma}} - 1] dG_\theta + f_x \int_{\theta_x}^{\infty} [(\frac{\theta}{\theta_x})^{\frac{\beta}{\Gamma}} - 1] dG_\theta = f_e$$

- Combining firm's first order condition and productivity cutoff, we can rewrite firm specific variables as follows:

$$\begin{aligned}
 r(\theta) &= \Upsilon(\theta)^{\frac{1-\beta}{\Gamma}} \cdot r_d \cdot \left(\frac{\theta}{\theta_d}\right)^{\frac{\beta}{\Gamma}}, & r_d &\equiv \frac{1+\beta\gamma}{\Gamma} f_d, \\
 h(\theta) &= \Upsilon(\theta)^{\frac{1-\beta}{\Gamma}(1-k/\delta)} \cdot h_d \cdot \left(\frac{\theta}{\theta_d}\right)^{\frac{\beta(1-k/\delta)}{\Gamma}}, & h_d &\equiv \frac{\beta\gamma}{\Gamma} \frac{f_d}{b} \left[\frac{\beta(1-\gamma k)}{\Gamma} \frac{f_d}{c a_{\min}^\delta} \right]^{-k/\delta}, \\
 w(\theta) &= \Upsilon(\theta)^{\frac{k(1-\beta)}{\delta\Gamma}} \cdot w_d \cdot \left(\frac{\theta}{\theta_d}\right)^{\frac{\beta k}{\delta\Gamma}}, & w_d &\equiv b \left[\frac{\beta(1-\gamma k)}{\Gamma} \frac{f_d}{c a_{\min}^\delta} \right]^{k/\delta},
 \end{aligned}$$

- Here Firm's revenue, firm's size and wage paid by the firm increase discretely at the productivity threshold for entry into export market.

- Wage and Productivity

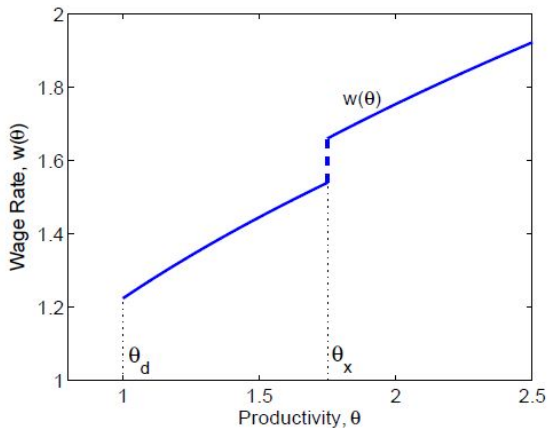


Figure 1: Wages as a function of firm productivity

- Wage distribution of workers employed by domestic firms

$$G_{w,d}(w) = \frac{1 - \left(\frac{w_d}{w}\right)^{1+1/\mu}}{1 - \rho^{z - \frac{\beta(1-k/\delta)}{\Gamma}}} \quad \text{for } w_d \leq w \leq w_d/\rho^{\frac{k\beta}{\delta\Gamma}}.$$

- Wage distribution of workers employed by exporters

$$G_{w,x}(w) = 1 - \left[\frac{w_d}{w} \Upsilon_x^{\frac{k(1-\beta)}{\delta\Gamma}} \rho^{-\frac{k\beta}{\delta\Gamma}} \right]^{1+1/\mu} \quad \text{for } w \geq w_d \Upsilon_x^{\frac{k(1-\beta)}{\delta\Gamma}} / \rho^{\frac{k\beta}{\delta\Gamma}}.$$

- Here both distributions have same shape parameter $1 + 1/\mu$, where $\mu \equiv \frac{\beta k/\delta}{z\Gamma - \beta}$ and $0 < \mu < 1$, and $\rho \equiv \frac{\theta_d}{\theta_x}$.

- Wage Inequality in the Closed Economy
 - The Coefficient of Variation of Wage is $\mu\sqrt{1 - \mu^2}$
 - The Gini Coefficient is $\frac{\mu}{2+\mu}$
 - The Theil Index is $\mu - \log(1 + \mu)$
- Higher $\mu \Rightarrow$ higher wage dispersion of the wage distribution and so higher wage inequality.
- Higher μ is due to lower z (Davis and Haltiwanger, 1991; Faggio et al., 2007)

- Wage Inequality and Trade liberalization
 - If $\rho = 0$ before and after trade liberalization \Rightarrow No change in Inequality.
 - If $\rho = 1$ before and after trade liberalization \Rightarrow No change in Inequality.
 - If initially $\rho = 0$ or $\rho = 1$ and after trade liberalization $0 < \rho < 1 \Rightarrow$ Increase in Inequality.

- $0 < \rho < 1$: Counterfactual Analysis

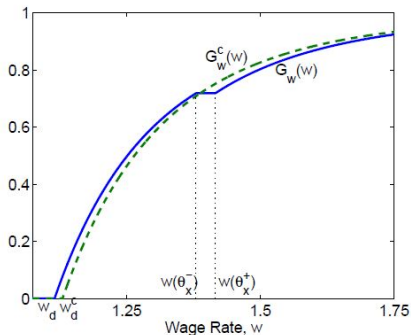


Figure 2: Cumulative distribution function of wages

Here $G_w(w)$ is open economy wage distribution and $G_w^c(w)$ is counterfactual wage distribution.

- $G_w^c(w)$ SOSD $G_w(w) \Rightarrow$ Higher Wage Inequality in Open Economy.

- Unemployment and Trade
 - Unemployment rate (u) is given by

$$u = \frac{L - H}{L} = 1 - \frac{H}{L} = 1 - \sigma x$$

Here σ is the hiring rate and x is the labor market tightness.

- In partial equilibrium analysis, the greater trade openness, the larger magnitudes of σ and x , so the greater unemployment rate.
- In general equilibrium analysis, the greater trade openness may or may not affect σ and x , so the impact on unemployment rate is uncertain.

- Under risk neutrality, opening trade in one-sector economy has following impacts:
 - Increases expected worker income (ω) \Rightarrow *ex ante* welfare.
 - Increases labor market tightness (x) and search costs (b).
- Under risk aversion, opening trade in two-sector economy has following impacts:
 - Increases expected worker income (ω) \Rightarrow *ex ante* welfare.
 - Increases labor market tightness (x) and search costs (b).

- Complementarities between workers' ability and firm productivity \Rightarrow Screen workers. Larger firms have higher returns to screening
- Opening of the closed economy to trade reallocates resources to more productive firms, more productive firms screen more intensively and have workforces of higher average ability.
- Opening of trade increases the dispersion of firm revenue, and rises wage inequality.
- Wage inequality is at first increasing and later decreasing in trade openness.
- Impact on unemployment is uncertain, depends on the hiring rate and labor market tightness.