Welfare Rationales for Conditionality of Cash Transfers

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Version: October 5, 2020

Abstract

We study efficiency and distributional effects of conditioning transfers on educational investments by parents, in an OLG model with missing financial markets and heterogeneity of learning ability. Conditional cash transfers (CCT) can be designed to generate a Pareto improvement relative to either laissez faire, or unconditional transfers such as universal basic income proposals. This applies irrespective of whether the status quo involves underinvestment or overinvestment in education from a first-best perspective, or the nature or extent of parental altruism towards children. The CCT corrects a market failure of insurance and lack of consumption smoothing for parents with respect to random realizations of ability of their offspring.

Keywords: human capital incentives, conditional cash transfers, universal basic income

Declarations of interest: none

*We acknowledge help and feedback from Brant Abbott, Roland Bénabou, Marcello d’Amato, Patrick Francois, Maitreesh Ghatak, Debraj Ray and two anonymous reviewers, besides participants in various seminars and conferences.
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1 Introduction

In developing countries, cash transfer programs are becoming increasingly widespread in government safety nets and related policy discussions. Prominent among these are conditional cash transfer (CCT) programs, where transfers are conditioned on parental investments in children’s education and health. Unconditional cash transfer (UCT) programs are less common, though there have been a number of policy experiments, and are generating increased interest in policy discussions on Universal Basic Income (UBI) proposals. UCTs and CCTs are sometimes bracketed together in evaluations of cash transfer programs based on RCT experiments (e.g., Banerjee et al. 2017). While the value of conditionality of the transfers has received less attention in RCT experiments, a number of recent empirical papers have assessed their effects on labor force participation and income. These studies indicate larger effects of CCTs on education, labor force participation and income over longer time spans, particularly for women. On the other hand, a number of possible disadvantages of CCTs have been mentioned in policy discussions: narrower coverage, greater paternalism and higher enforcement burdens (Mundle 2017), in some contexts also lack of progressive impact resulting from uneven takeup (Das, Do, and Özler 2004). Hence policy makers face complex tradeoffs in evaluating the merits and disadvantages of conditional transfers.

From a long-term viewpoint, welfare objectives of efficiency or redistribution have traditionally provided the foundations for design of systems of social security, taxation and government welfare programs. The efficiency objective pertains to a market failure (or Pareto inefficiency) that a safety net program is designed to correct, while redistributive goals are incorporated in utilitarian or Rawlsian notions of justice. An explicit argument for either of these rationales requires an underlying model of the economy, incorporating ‘fundamentals’ such as utility functions, technology, market and information structure, which allow a comprehensive evaluation of economy-wide effects on resource allocation and welfare. In particular, goals of efficiency or redistribution are related intrinsically to utilities of agents in allocations attained with and without the program. These are not just abstract criteria used by academic theorists but often play an important role in policy discussions that evaluate the complex trade-offs involved. For example a World Bank discussion paper on CCTs (Das et al. 2004, p. 2f) poses the following questions:

"A rationale for conditionality must then lie in the ability of such schemes to address underlying market failures. . . . conditional cash transfers seek to restore efficiency in

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the economy. . . . The argument developed in this paper is that evidence of an externality, though compelling, may be insufficient grounds for conditional cash transfer schemes without additional information on its extent. This argument relies on the observation that such schemes have historically been used for an entirely different purpose, that of targeting resources and pro-poor redistribution. . . . These two very different rationales for conditional transfers result in a tension. When used to increase investment in human capital, such schemes could have adverse redistributive impacts. Conversely, used as targeting or redistributive mechanisms, they could decrease efficiency. One way for policy-makers to then decide on the overall benefits would be to obtain information on both sides of the coin. How do efficiency gains compare to adverse redistributive impacts when conditional cash transfers are implemented? Similarly, when used for targeting purposes, how successful was the targeting given the associated efficiency loss? . . . Careful analysis and information on the gains and losses is then critical for the overall evaluation of the program.”

A systematic micro-founded welfare analysis can also help evaluate the different advantages and disadvantages of conditionality mentioned in policy discussions, besides indicating other dimensions that may have been overlooked (such as consumption smoothing, financing costs and general equilibrium (GE) effects). Such a welfare analysis requires an underlying dynamic GE model. This constitutes the motivation of this paper, which studies the welfare rationale for CCTs and the related question of design from a normative standpoint, both relative to a laissez faire economy with missing financial markets, and to unconditional transfers such as a UBI financed by a progressive income tax.

The first question we address is the comparison with a laissez faire benchmark: is there a market failure that CCTs can help overcome? This requires demonstration of the existence of a CCT which if suitably designed would achieve a Pareto improvement. In policy discussions of CCTs, it is frequently asserted that missing markets for credit and insurance, and/or parent-child externalities, create market failure (in the form of ‘underinvestment’) in education. The notion of underinvestment usually invoked relates to a first-best benchmark, e.g., whether the rate of return to education among beneficiaries exceeded the social cost. In a world of missing markets or asymmetric information, first-best criteria of Pareto efficiency do not necessarily apply, and need to be replaced by ‘constrained’ Pareto efficiency, where the government may face borrowing constraints just like market agents, and may lack detailed information about agent characteristics just like lenders or insurers that prevent well functioning credit and insurance markets. Matters are further complicated in an OLG setting, where standard theorems of welfare economics do not

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3See e.g. López-Calva and Lustig (2010, p. 15), Kahhat (2010, p. 32) and Das et al. (2004, p. 8)
necessarily apply.

Indeed, steady states of a model with dynastic households and missing financial markets may be constrained Pareto efficient. A Ramsey neoclassical growth model provides a ready illustration: despite lack of access to any borrowing opportunity, an autarkic agent can accumulate own savings to converge to a steady state which is fully Pareto efficient. Mookherjee and Ray (2003) show this extends to a ‘standard’ OLG model of human capital accumulation where households lack access to financial markets. If there are indivisibilities in investment (e.g., in the form of a limited set of occupational choices), they show efficient as well as inefficient steady states co-exist; when such indivisibilities become negligible (with a rich set of occupational options), the set of steady states shrinks to the one that is fully efficient. This implies that the common view that missing financial markets necessarily imply a market failure is incorrect.

The first main result of this paper is that the common intuition of a market failure is actually correct, once the ‘standard’ model is extended to incorporate some learning ability heterogeneity of children, observed by parents but not the government. Specifically, given such heterogeneity, any laissez faire dynamic competitive equilibrium is interim-Pareto dominated by a suitably designed CCT policy. The interim Pareto domination requirement is very demanding: the expected utility of every parent (prior to learning the ability of her child) must rise, irrespective of occupation or generation.

The CCT we consider finances education subsidies for households in any given income class by general income taxes paid by households in the same class. It thereby resembles an insurance program that redistributes from families that do not invest in education of their children, to families earning the same income that do invest. The efficiency improvement generated thereby is driven by a combination of greater investment in education (which raises welfare of succeeding generations), and superior smoothing of parental consumption (since the parents that invest consume less). These welfare benefits arise only in the presence of ability heterogeneity. With homogenous ability, parents of a certain income will make exactly the same education decisions, so there is no variation of parental consumption, conditional on their income. This also explains why the result does not apply in a static deterministic setting, where neither consumption smoothing nor investment play any role – conditionality of transfers then just ends up lowering the welfare of recipients, a manifestation of the welfare loss associated with increased paternalism. These static ‘paternalistic’ welfare losses get transformed into welfare gains in the dynamic setting with heterogeneity.

We show the same logic ensures the welfare dominance of CCTs over UCTs in which taxes and transfers may be conditioned on income or occupation, but not on educational decisions made by parents on behalf of their children. This pertains to the debate on CCTs versus UBI. A UBI can

\[4\] We impose very mild conditions on the progressivity of income taxes, that (effective) marginal tax rates are
be thought of as a uniform level of financial support provided by the government to all citizens, funded by taxes on income.

The welfare dominance of CCTs turns out to be robust to many extensions of our base model, pertaining to the nature of parental altruism, divisibility of educational investments, elastic labor supply or general equilibrium effects on wages. For instance, it applies irrespective of whether parental altruism is paternalistic or non-paternalistic, the degree of altruism and whether or not there is underinvestment or overinvestment in the first-best sense. If parents are non-paternalistic and altruistic enough, the interim-Pareto improving CCT ends up achieving an ex post Pareto improvement as well. Even parents that do not themselves invest in education end up benefitting from the policy in anticipation of the resulting utility benefit to succeeding generations.

Moreover, the resulting equilibrium allocations achieve superior macroeconomic performance on many dimensions: in every generation, per capita income and skill rises, income gaps between skilled and unskilled become smaller, and there is greater upward mobility. Hence utility improvements do not accrue only to households that are better off to start with. If parental altruism is paternalistic, redistribution and efficiency objectives can be separated. If it is non-paternalistic, this is no longer the case, but the CCT can be designed to alter interim utilities of agents at different income levels in exactly the same way, thereby avoiding any redistribution across income classes. This prevents a dilution of parental incentives to invest as a means of achieving upward mobility of their children. With a CCT of this kind the efficiency improvement does not come at the cost of raising inequality across income classes, thereby addressing the concern raised by Das et al. (2004).

Another lesson from our analysis is the necessity to pay attention to dimensions that tend to be overlooked in policy discussions: mechanisms for financing transfers, and effects on parental consumption smoothing, over and above effects of transfer conditionality on education, upward mobility or labor force participation. There is an underlying market failure that the CCT corrects, but it is not a market failure in education. Education could be ‘over-provided’ under laissez faire in the standard first-best sense, and yet the CCT would generate a Pareto improvement at the same time that it induces even higher educational investments. The market failure that is being corrected is one for insurance, and resulting lack of consumption smoothing for parents with respect to random realizations of ability for their offspring. Our analysis indicates the need for empirical analyses of CCTs to focus on this hitherto neglected dimension. To the extent that CCTs in practice have benefitted better-off parents more, our results suggest the possibility of redesigning the subsidy and financing methods to avoid this problem.

positive but less than 100%.

Some authors such as de Janvry et al. (2006) have studied the role of CCTs in providing parents with insurance against other external shocks, but not with respect to ‘ability’ risk of their children.
In order to achieve the demanding requirement of a Pareto improvement, the CCT has to be designed carefully to realize the required improvements in efficiency and incentives. Are the informational or enforcement requirements of the resulting policy too demanding, thereby rendering it impractical? Is it likely to be politically feasible? These questions are difficult to answer in the abstract, and are likely to depend on details of the specific context. Theoretical arguments for efficiency or inefficiency of certain policies (such as free trade, or Pigouvian pollution taxes) however have traditionally been based on the notion of a potential Pareto improvement, as embodied in Kaldor-Hicks welfare criteria where ‘in principle’ losers from the policy could be compensated by the gainers. This is as far as one can go on the basis of theory alone: establishing ‘proof of concept’, a necessary first step before embarking on empirical analyses needed to design and evaluate specific versions of policies, or political feasibility. However, the design of the CCT that we consider in the paper does not seem any more complicated than the design of any insurance program in terms of choosing premiums and benefits to achieve both self-financing and significant take-up objectives.

On the other hand, we do not address ‘third-best’ considerations pertaining to the administration and enforcement of transfer conditionality. Governments have to verify school participation of children and deny transfers to parents if their children do not meet the required conditions. The widespread adoption of CCTs in many countries suggests this is not an overwhelming problem, though in some countries with poor state capacity it could pose an important barrier. In any case, our analysis helps identify the welfare benefits from transfer conditionality, which have to be traded off against the accompanying administration and enforcement costs. It is also worth mentioning that similar problems would arise in implementation of UBI in societies with low levels of financial inclusion, which create problems for direct transfers from the state to citizens outside the formal financial sector. Our results accord with the broad assessment of Ghatak and Maniquet (2019) that it is difficult to provide a convincing rationale for UBI in a second-best environment, which is relevant to longer term considerations in which enforcement of conditionality is a lower-order concern.

The paper is structured as follows. Section 2 illustrates the market failure that CCTs can correct and how they improve on a status quo involving laissez faire or rather arbitrary combinations of UCTs. We start with a simple setting with two occupations which abstracts from general equilibrium effects, endogenous labor supply or the possibility of financial bequests. Section 3 discusses robustness of our results to the previous simplifying assumptions. Section 4 relates our analysis to different economic literatures, before Section 5 concludes.
2 Baseline Model and Results

2.1 Paternalistic Altruism

Consider an economy with multiple dates and a continuum of households, each comprising a parent and a child at any given date. There are two types of occupations, skilled \((c = 1)\) and unskilled \((c = 0)\); work in the former requires an indivisible educational investment when the agent is young. Parental earnings depend on their occupation, but are subject to exogenous shocks. Conditional on realized household income \(y\), the parental occupation does not matter.

Let the cumulative distribution function of \(y\) be denoted \(G_c\) for parents in occupation \(c\). Abstract initially from general equilibrium effects, by assuming that \(G_c\) is not affected by the proportion of agents in occupation \(c\). We can think of \(G_c\) as reflecting a skill-specific probability distribution of numbers of efficiency units of labor, which households supply to firms with a constant returns to scale production function on a competitive labor market. To simplify the exhibition assume a common finite support \(Y \equiv \{y_1, \ldots, y_n\}\) for both \(G_1\) and \(G_0\), with \(y_1 > 0\) and \(y_i < y_{i+1}\) for all \(i = 1, \ldots, n - 1\). The probability of income realization \(y_i\) in occupation \(c \in \{0, 1\}\) is \(\pi_{ic} > 0\). We assume \(G_{j1} \equiv \sum_{i=1}^{j} \pi_{i1} < G_{j0} \equiv \sum_{i=1}^{j} \pi_{i0}\) for all \(j = 1, \ldots, n - 1\), so income distribution \(G_1\) among the skilled (strongly) first order stochastically dominates distribution \(G_0\) among unskilled households.

Every parent privately observes the idiosyncratic cost \(\tilde{x}\) of educating its child; this represents the heterogeneity of learning abilities in the population: realization \(\tilde{x}\) of the education cost of any child is drawn randomly and independently according to a cumulative distribution function \(F\) defined on \([0, \infty)\). \(F\) is \(C^2\) and strictly increasing. Parental income is divided between consumption and education. Households cannot borrow against children’s future earnings to finance \(\tilde{x}\); and they can neither insure against income shocks nor the risk that the child’s learning ability is high or low. So a parent with income realization \(y\) and a child of type \(\tilde{x}\) takes education decision \(e \in \{0, 1\}\) to maximize

\[
u(y - e\tilde{x}) + [eV_1 + (1 - e)V_0]
\]

where \(V_c \equiv \sum_{i=1}^{n} \pi_{ic}V(y_i)\). Function \(u\) is strictly increasing, strictly concave and smooth on \((0, \infty)\) with \(\lim_{c \to 0} u(c) = -\infty\). No restriction is imposed on the function \(V\) that reflects parental altruism towards the child, except that it is strictly increasing. Parents may under-value the benefits of higher earnings of their children, resulting in a large parent-child externality and ‘underinvestment’ in a first-best sense (based on pecuniary rate of return on education). Or they could over-value it.

\[\text{Among many possibilities, the parent might care about its offspring’s earnings only for the prospective aid received after retirement; or high skilled wages might be subjectively discounted because corresponding work by the child increases geographic distance to the family.}\]
resulting in ‘over-investment’. The benefit to the parent of educating the child is \( B \equiv [V_1 - V_0] > 0 \). The combination of paternalism and absence of GE effects implies \( B \) is exogenous and stationary.

We consider a standard OLG model in which a child whose parent chose \( e \in \{0, 1\} \) works in occupation \( c = e \) in the next generation and maximizes (1) for new draws of income and child ability.\(^7\) The proportion of population in the skilled occupation, \( \lambda \), is then the dynamic state variable of interest. Still, each parent in any given occupation at any date will face an independent child ability.

The combination of paternalism and absence of GE effects implies \( B \) is unaffected by decisions of any other variable of interest. Still, each parent in any given occupation at any date will face an independent child ability.

The solution to (1) is the following: \( e(y, \tilde{x}) = 1 \) iff \( \tilde{x} \leq x^*(y) \) where

\[
u(y) - u(y - x^*(y)) = B. \tag{2}
\]

This results in interim parental welfare \( W_y^* \equiv U_y^* + F(x^*(y))B + V_0 \), where

\[
U_y^* = [1 - F(x^*(y))]u(y) + F(x^*(y))E[u(y - \tilde{x})|\tilde{x} \leq x^*(y)] \tag{3}
\]

denotes interim consumption utility before the parent observes \( \tilde{x} \).

A dynamic competitive equilibrium (DCE) in this economy with an initial skill proportion \( \lambda_0 \) at date 0 consists of a sequence of subsequent skill proportions \( \lambda_k \), \( k = 1, 2, \ldots \) such that at each date \( k \geq 0 \): (i) a fraction \( \lambda_k \) of the adult population is in the skilled occupation; (ii) incomes of adults in occupation \( c = 0, 1 \) are drawn from the distribution \( G_c \); (iii) every household with income realization \( y \) then learns its child’s education cost realization \( \tilde{x} \), and chooses \( e \) to maximize utility (1); (iv) these choices give rise to a proportion \( \lambda_{k+1} \) of the population having a skilled occupation at date \( k + 1 \).\(^8\)

This definition can be extended to an economy with a stationary fiscal policy, in which \( Y \) denotes after-tax income levels \( y_i \equiv \bar{y}_i + \tau_i \) that result from market incomes \( \bar{y}_i \in \bar{Y} = \{ \bar{y}_1, \ldots, \bar{y}_n \} \) with \( \bar{y}_i < \bar{y}_{i+1} \), supplemented by progressive net transfers \( \tau_i \) that satisfy \( \tau_{i-1} \geq \tau_i \) and \( \tau_i > -\bar{y}_i \) for all \( i \). A negative net transfer corresponds to an income tax payment. For instance, a universal basic income of \( b > 0 \) financed by proportional or progressive income taxes \( \hat{\tau}_i = \sum_{j=1}^{i} \alpha_j (\bar{y}_j - \bar{y}_{j-1}) \) would correspond to \( \tau_i = b - \hat{\tau}_i \) (with marginal tax rates \( 0 \leq \alpha_i \leq \alpha_{i+1} < 1 \) and \( \bar{y}_0 \equiv 0 \)). Unconditional cash transfers to poor households with pre-tax incomes \( \bar{y} \) below a threshold \( \bar{y}_h \) that are financed by households with \( \bar{y} \geq \bar{y}_h > \bar{y}_l \) would amount to \( \tau_1 \geq \ldots \geq \tau_i > 0 > \tau_h \geq \ldots \geq \tau_n \), and \( \tau_1 = 0 \) otherwise. Laissez faire obviously corresponds to \( \tau_i \equiv 0 \) for all \( i \).

In a DCE, successive generations of every household transit between skilled and unskilled occupations according to a time-homogeneous Markov chain, with transition probabilities \( F_1^* > F_0^* \)

\(^7\)The assumptions could, however, also pertain to a static two-period model as in Jacobs et al. (2012) and other public economics literature (see Section 4.2); the world ends when the child becomes an adult and consumes her entire earnings.

\(^8\)It is evident from the definition that there is a unique DCE corresponding to any initial skill proportion.
(where \( F^*_c \equiv \sum_{i=1}^{n} \pi_{ic} F(x^*(y_i)) \) from occupation \( c \) to the skilled occupation. This stochastic process converges to a limiting distribution which is a steady state, where upward mobility flows from the unskilled to the skilled occupation equal downward flows in the opposite direction. Our analysis does not presume the economy starts at a steady state; hence the status quo DCE may well involve a skill proportion that increases or decreases over time.

Now consider an income-specific CCT program where a household with income \( y_i \) pays a tax of

\[
t_i = \epsilon_i \cdot \frac{F(x_i)}{1 - F(x_i)}
\]

if it does not invest in education, and receives a subsidy of

\[
s_i = \epsilon_i
\]

if it does invest; \( \epsilon_i > 0 \) and \( x_i > x^*(y_i) \) are parameters to be chosen. Intuitively, the policy seeks to raise the education threshold for parents with income \( y_i \) from \( x^*(y_i) \) to \( x_i \), and \( \epsilon_i \) will represent the scale of the intervention, i.e., the size of the subsidy. If the policy is successful in inducing parents with income \( y_i \) to raise their education threshold to \( x_i \), the policy will not affect the public budget surplus. So it is essentially an insurance scheme (breaking even within income class \( y_i \)) where parents with less able children (\( \bar{x} \) above the education cost threshold) do not invest and thus enjoy higher parental consumption, will end up paying taxes that finance subsidies to parents that end up consuming less owing to investing in their children’s education.

**Proposition 1** Consider a DCE involving unconditional taxes/transfers with \( \tau_{j-1} \geq \tau_j \) and \( \tau_j > -\bar{y}_j \), or laissez faire. Take any \( i \). There exist \( x_i > x^*_i \equiv x^*(y_i) \) and \( \epsilon_i > 0 \) such that introducing the corresponding CCT will generate an interim Pareto improvement. Interim welfare of parents with income \( y_i \) at every date increases strictly, their education cost threshold rises from \( x^*_i \) to \( x_i \) (implying the skill proportion rises at every subsequent date), ex post welfare and education decisions of all other income classes remain unchanged, and the public budget surplus improves.

**Proof.** Given any \( x > x^*(y_i) \) and any \( \epsilon \geq 0 \), define \( x_i(\epsilon, x) \) by the condition

\[
u(y_i - \epsilon \frac{F(x)}{1 - F(x)}) - u(y_i + \epsilon - x_i(\epsilon, x)) = B.
\]

Our conditions on \( u \) ensure this is well defined. It is evident that \( x_i(0, x) = x^*(y_i) \), and \( x_i \) rises in \( \epsilon \) (holding \( x \) fixed) with a slope exceeding 1. Hence there exists \( \epsilon_i(x) \in (0, x) \) such that \( x_i(\epsilon_i(x), x) = x \), i.e., a parent with income realization \( y_i \) will select the threshold \( x \) under the CCT corresponding to \( x \) and \( \epsilon_i(x) \). Moreover, \( \epsilon_i(x) \) is strictly increasing in \( x \) with \( \epsilon_i(x^*(y_i)) = 0 \).
Next, we claim that we can select \( x_i > x^*(y_i) \) such that

\[
\frac{\mathbb{E}[u'(y_i + \epsilon_i(x_i) - \bar{x})|\bar{x} \leq x_i]}{u'(y_i - \epsilon_i(x_i)) F(x_i)/(1 - F(x_i))} > \frac{F(x_i)/(1 - F(x_i))}{F(x^*(y_i))/(1 - F(x^*(y_i)))}. \tag{7}
\]

As \( x_i \to x^*(y_i) \), the LHS approaches

\[
\frac{\mathbb{E}[u'(y_i - \bar{x})|\bar{x} \leq x^*(y_i)]}{u'(y_i)} \tag{8}
\]

which strictly exceeds 1 (since \( x^*(y_i) > 0 \)), while the RHS approaches 1. Hence by continuity of all relevant functions, condition \( [7] \) holds for some \( x_i \) in a right neighborhood of \( x^*(y_i) \), thereby establishing the claim.

Suppose the CCT corresponding to \( x_i \) and an intermediate scale \( \epsilon \in (0, \epsilon_i(x_i)) \) is introduced. This would induce a cost threshold \( \hat{x}_i(\epsilon, x_i) \in (x^*(y_i), x_i) \) for parental education decisions, satisfying

\[
u(y_i - \epsilon \cdot \frac{F(x_i)}{1 - F(x_i)}) - u(y_i + \epsilon - \hat{x}_i(\epsilon, x_i)) = B \tag{9}\]

and would generate interim consumption utility

\[
\mathcal{U}_i(\epsilon, x_i) = [1 - F(\hat{x}_i(\epsilon, x_i))]u(y_i - \epsilon \cdot \frac{F(x_i)}{1 - F(x_i)}) + F(\hat{x}_i(\epsilon, x_i))\mathbb{E}[u(y_i + \epsilon - \bar{x})|\bar{x} \leq \hat{x}_i(\epsilon, x_i)]. \tag{10}
\]

Using the Envelope Theorem, the change in interim welfare of a parent with ex post income \( y_i \) from a small rise in the scale \( \epsilon \) of this CCT equals

\[
\frac{\partial \mathcal{U}_i(\epsilon, x_i)}{\partial \epsilon} = F(\hat{x}_i(\epsilon, x_i))\mathbb{E}[u'(y_i + \epsilon - \bar{x})|\bar{x} \leq \hat{x}_i(\epsilon, x_i))] - [1 - F(\hat{x}_i(\epsilon, x_i))] \frac{F(x_i)}{1 - F(x_i)} u'(y_i - \epsilon \cdot \frac{F(x_i)}{1 - F(x_i)}) \tag{11}
\]

which is strictly positive (using \( \hat{x}_i(\epsilon, x_i) \in (x^*(y_i), x_i) \), \( \epsilon < \epsilon_i(x_i) \) and \([7]\)). This implies that interim welfare of the parent is strictly higher than in status quo when the scale \( \epsilon \) is set at its maximum value \( \epsilon_i(x_i) \). This induces threshold \( x_i > x^*_i \) without changing ex post welfare or education decisions at other income levels; nor having a direct effect on the public budget.

The increased proportion of skilled in the population has a beneficial indirect effect on the budget if the status quo involves progressive fiscal policies where some inequality \( \tau_{j-1} \geq \tau_j \), \( j = 2, \ldots, n \), is strict. Namely, suppose the dynamic sequence of skill proportions in the status quo DCE is \( \lambda_0, \lambda_1, \lambda_2, \ldots \) and introduce the intervention at date \( k = 0 \) (w.l.o.g.). Then the post-intervention investment thresholds are \( x(y) = x^*(y) \) for all \( y \neq y_i \) and \( x(y_i) = x_i > x^*(y_i) \). This strictly increases the transition probability from occupation \( c \) to the skilled occupation: \( F_c = \sum_{i=1}^n \pi_{ic} F(x(y_i)) > F^*_c = \sum_{i=1}^n \pi_{ic} F(x^*(y_i)) \); and induces a skill proportion \( \lambda_1 > \lambda^*_1 \). Moreover, \( \lambda_k > \lambda^*_k \) implies

\[
\lambda_{k+1} = \lambda_k^* F_1 + (1 - \lambda_k^*) F_0 + (\lambda_k - \lambda_k^*) [F_1 - F_0] > \lambda_k^* F_1^* + (1 - \lambda_k^*) F_0^* = \lambda_{k+1}^* \tag{12}
\]
using $F_1 > F_0$. So skill proportions in the population stay above their status quo benchmarks in every period of the CCT intervention. Stochastic dominance of the income distribution among the skilled and $\tau_{j-1} > \tau_j$ for some $j$ then imply that public expenditure $\lambda^* \bar{\tau}_1 + (1 - \lambda^*) \bar{\tau}_0$ with $\bar{\tau}_c = \sum_{i=1}^n \pi_{ic} \tau_i$ decreases:

$$\frac{\partial[\lambda \bar{\tau}_1 + (1 - \lambda) \bar{\tau}_0]}{\partial \lambda} = \bar{\tau}_1 - \bar{\tau}_0 < 0. \quad (13)$$

The idea behind the interim Pareto improvement compared to laissez faire or any unconditional transfers is the following. The CCT induces greater educational investment, as education is being subsidized. And at a small scale, the scheme offers a first order improvement in consumption smoothing. This is illustrated in Figure 1: consumption of a parent with income $y_i$ generally varies non-monotonically in education cost realization $\bar{x}$. In status quo (bold line), only parents whose child can costlessly be educated ($\bar{x} = 0$) and non-investing parents consume their full income $y_i$; all those with $\bar{x} \in (0, x^*_i)$ consume less. The CCT reduces this variation (dotted line): parents who would have invested in status quo do still invest and enjoy a consumption increase of $s_i$; parents who invest neither in status quo nor with the CCT see their consumption lowered by $t_i = s_i \cdot F(x_i)/(1 - F(x_i))$ in return. A small share $[F(x_i) - F(x^*)]$ of parents ‘avoid’ the latter: they reduce own consumption further in favor of obtaining paternalistic benefit $B$. If these parents did not change their behavior, the consumption distribution with CCT would constitute a
mean-preserving compression and second-order stochastically dominate the status quo (provided \( x_i \) is not too far above \( x^*_i \), as ensured by (7)). They do, however, change their behavior and switch to investing in their children’s education, and become better off as a result. So interim utility of parents with income \( y_i \) increases by an even greater amount than that implied by the respective mean-preserving compression of consumption.

Note that the scheme can be offered independently for one, some, or all incomes \( y_i \). So the efficiency improvement is orthogonal to effects on inequality of welfare at different income levels. If the government wants to reduce inequality, it can introduce it only for low incomes. Or it can offer it for rich and poor, so that all gain equally. It can also be restricted to higher incomes, should the government want to raise inequality.

Observe also that the result applies irrespective of whether there is underinvestment or over-investment in education in the conventional sense. The market failure is in insurance, and that is being corrected by the CCT which is a form of consumption insurance. This is a novel insight into the welfare role of CCTs, operating partly via consumption smoothing, and partly via enhanced investment. The former ensures all parents are better off (at the interim stage). The latter guarantees that future generations benefit, even if the CCT intervention should be temporary. To ensure the improvement in consumption smoothing, the education subsidy is financed in a specific way: by taxing incomes of those in the same income class. The policy substitutes for missing insurance markets in the status quo (ostensibly owing to adverse selection or other transaction cost / enforcement problems), and functions like an insurance policy. There is a separate policy for each income level, so education subsidies to parents at any income level are funded by others with the same income who do not invest in education, owing to low ability realizations of their children. This ensures that the program does not result in any redistribution between the poor and rich, beyond the fiscal policy that may apply in status quo (such as UBI financed by a proportional income tax, progressive UCTs, or combinations).

Of course if the government wants to additionally redistribute in favor of the poor, the subsidies could be restricted only to the poor, and funded by taxes paid by the rich. In practice, governments often have such a redistributive goal and do fund welfare benefits in this way. But such interventions are not Pareto improving. What Proposition 1 shows is that if the government wants to avoid (additional) redistribution, it is possible in principle to design a CCT that succeeds in doing so and to generate welfare improvements for both rich and poor.

We show below that these results are robust to different extensions of the model.

---

9If CCTs are phased out at some date \( k' \), the skill shares \( \lambda_{k'}, \lambda_{k'+1}, \ldots \) converge to status quo levels \( \lambda_{k'}^*, \lambda_{k'+1}^*, \ldots \) from above, noting that \( F_c \geq F_c^* \) is sufficient for concluding (12).
2.2 Non-Paternalistic Altruism

To demonstrate that the possibility of a Pareto improvement is not limited to contexts where the perceived benefits of education are paternalistic, let us move to a more refined form of parental altruism, where households are dynasties and parents are non-paternalistic à la Barro-Becker. In this specification, parents internalize the utility consequences of education decisions for their offspring, albeit scaled down by a discount factor $\delta \in (0, 1)$. If $\delta$ is close to 1, the parent-child externality tends to vanish. One might guess that market failure in education is now less likely to occur. But as we have argued above, the key market failure is in insurance, and that is unaffected by the magnitude of $\delta$. In fact we will show below in Proposition 3 that $\delta$ large enough ensures that the CCT program generates an ex post Pareto improvement, so the efficiency improvement is if anything enhanced when $\delta$ is high.

We continue to assume a finite support $Y$ of the after-tax income distribution (resulting either from stationary fiscal policies that do not condition on education investment, or laissez faire), a well-behaved consumption utility function $u$, and that the income distribution given $c = 1$ first order stochastically dominates the distribution for $c = 0$ strongly. The definition of DCE is modified in the obvious way. To illustrate, the DCE in the status quo is characterized as follows. Let $x_i^*$ denote the investment threshold for a parent with income $y_i$ in the status quo DCE. The threshold is uniquely determined by

$$u(y_i) - u(y_i - x_i^*) = B^* = \delta [W_1^* - W_0^*]$$

(14)

where

$$W_c^* = \bar{U}_c^* + F_c^* B^* + \delta W_0^*$$

(15)

is the expected dynastic utility of a household in occupation $c$ based on its expected consumption utility

$$\bar{U}_c^* = \sum_{i=1}^{n} \pi_i c U_i^*$$

(16)

where

$$U_i^* = [1 - F(x_i^*)] u(y_i) + F(x_i^*) E[u(y_i - \tilde{x}) | \tilde{x} \leq x_i^*]$$

(17)

is the interim consumption utility of income type $i$ (with income realization $y_i$), and we abbreviate

$$F_c^* = \sum_{i=1}^{n} \pi_i c F(x_i^*).$$

(18)

$^{10}$A household’s value function can be bounded by $u(y_1)/(1 - \delta)$ and $u(y_n)/(1 - \delta)$ from below and above, given $\delta \in (0, 1)$. Blackwell’s sufficient conditions then hold, thereby guaranteeing a unique solution.
We first verify that Proposition 1 extends to dynamic Barro-Becker preferences. The respective policy involves a new education threshold $x_i$, expected consumption utility $\mathcal{U}_t$ for income type $i$, $\bar{\mathcal{U}}_c$ for occupation $c$, and investment probability $F_c$ for occupation $c$ satisfying analogous conditions:

$$u(y_i - t_i) - u(y_i + s_i - x_i) = B \equiv \delta [W_1 - W_0]$$  \hspace{1cm} (19)
$$W_c = \bar{\mathcal{U}}_c + F_c B + \delta W_0$$  \hspace{1cm} (20)
$$\bar{\mathcal{U}}_c = \sum_{i=1}^n \pi_i \mathcal{U}_i$$  \hspace{1cm} (21)
$$\mathcal{U}_i = [1 - F(x_i)] u(y_i - t_i) + F(x_i) \mathbb{E}[u(y_i + s_i - \bar{x}) | \bar{x} \leq x_i]$$  \hspace{1cm} (22)
$$F_c = \sum_{i=1}^n \pi_i c F(x_i).$$  \hspace{1cm} (23)

With Barro-Becker preferences, the post-CCT benefits of investing in education, $B$, are jointly determined by all new investment thresholds $x_i$ via (20)–(23). This renders an intervention that affects welfare of just one income type $i$ infeasible. But it is still possible to achieve an interim Pareto improvement – for instance, by introducing CCTs simultaneously for all income classes.

**Proposition 2** Consider a DCE involving unconditional taxes/transfers with $\tau_{j-1} \geq \tau_j$ and $\tau_j > -\bar{y}_j$, or laissez faire. There exist $t_i = \epsilon_i \frac{F(x_i)}{1 - F(x_i)}$ and $s_i = \epsilon_i$ for some $\epsilon_i > 0$ and $\bar{x}_i > x_i^*$ for all $i = 1, \ldots, n$ such that introducing the corresponding CCTs will generate an interim Pareto improvement. At every subsequent date, interim welfare of parents in every income class increases by the same positive amount, the education cost threshold for income $y_i$ households rises from $x_i^*$ to some $x_i \in (x_i^*, \bar{x}_i)$, and the public budget surplus improves.

**Proof.** As in Proposition 1 select $\bar{x}_i > x_i^*$ such that

$$\frac{\mathbb{E}[u(y_i + \bar{\epsilon}_i - \bar{x}) | \bar{x} \leq \bar{x}_i]}{u'(y_i - \bar{\epsilon}_i \frac{F(\bar{x}_i)}{1 - F(\bar{x}_i)})} > \frac{F(\bar{x}_i) / [1 - F(\bar{x}_i)]}{F(x_i^*) / [1 - F(x_i^*)]}$$  \hspace{1cm} (24)

where $\bar{\epsilon}_i$ is defined by

$$u(y_i - \bar{\epsilon}_i \frac{F(\bar{x}_i)}{1 - F(\bar{x}_i)}) - u(y_i + \bar{\epsilon}_i - \bar{x}_i) = B^*.$$  \hspace{1cm} (25)

Choose $\epsilon_i \in [0, \epsilon_i]$ and CCT with $s_i = \epsilon_i, t_i = \epsilon_i \frac{F(x_i)}{1 - F(x_i)}$. Let $x_i = x_i(\epsilon_i)$ denote the corresponding investment threshold for type $i$ with the same education return $B^*$ as in the status quo:

$$u(y_i - \epsilon_i \frac{F(\bar{x}_i)}{1 - F(\bar{x}_i)}) - u(y_i + \epsilon_i - x_i) = B^*.$$  \hspace{1cm} (26)

Previous arguments imply $x_i \in [x_i^*, \bar{x}_i]$ with $x_i = x_i^*$ if $\epsilon_i = 0$ at the status quo, and $x_i = \bar{x}_i$ if $\epsilon_i = \bar{\epsilon}_i$. By construction, the CCT generates the same budget surplus as the status quo in the
latter case, and improves the budget surplus if $\epsilon_i, x_i$ are respectively smaller than $\bar{\epsilon}_i, \bar{x}_i$. Interim consumption utility

$$U_i(\epsilon_i) \equiv [1 - F(x_i)]u\left(y_i - \epsilon_i \frac{F(\bar{x}_i)}{1 - F(\bar{x}_i)}\right) + F(x_i)\mathbb{E}[u(y_i + \epsilon_i - \bar{x})|\bar{x} \leq x_i]$$

is strictly increasing in $\epsilon_i$ over this range. It remains to show that we can select $\epsilon_i \in (0, \bar{\epsilon}_i)$ for all $i = 1, \ldots, n$ such that the gross return from education is unchanged compared to the status quo:

$$B^* = \frac{\delta \sum_{i=1}^{n} \pi_{i1} - \pi_{i0}}{1 - \delta \sum_{i=1}^{n} \pi_{i1} - \pi_{i0}} U_i(\epsilon_i).$$

This is because (28) is a necessary and sufficient condition for investment thresholds $x_i$ to constitute a DCE following the chosen CCT.

This condition can also be written as

$$\delta \sum_{i=1}^{n} (\pi_{i1} - \pi_{i0}) [U_i(\epsilon_i) + B^* F(x_i)] = B^*,$$

and it holds at the status quo:

$$\delta \sum_{i=1}^{n} (\pi_{i1} - \pi_{i0}) [U_i(0) + B^* F(x_i^*)] = B^*.$$

Hence (28) reduces to

$$\sum_{i=1}^{n} (\pi_{i1} - \pi_{i0}) \psi_i(\epsilon_i) = 0$$

where

$$\psi_i(\epsilon_i) \equiv [U_i(\epsilon_i) + B^* F(x_i)] - [U_i(0) + B^* F(x_i^*)]$$

is a measure of the relative interim welfare improvement for income type $i$, as the actual improvement is $\psi_i(\epsilon_i) + \delta[W_0 - W_0^*]$ and $\delta[W_0 - W_0^*]$ does not vary with $i$. $\psi_i(\epsilon_i)$ is strictly increasing in $\epsilon_i$ over the range $[0, \bar{\epsilon}_i]$. Hence there exists a small $\eta > 0$ such that $\epsilon_i = \psi_i^{-1}(\eta) \in (0, \bar{\epsilon}_i)$ for all $i = 1, \ldots, n$. It follows from $\sum_{i=1}^{n} \pi_{ic} = 1$ that (31) and hence (28) hold with these choices for $\epsilon_i$. The public budget surplus, already improved because $\epsilon_i \in (0, \bar{\epsilon}_i)$, is additionally aided if the status quo involves progressive fiscal policies where $\tau_{j-1} \geq \tau_j$ holds strictly for some $j$, by the same argument as in Proposition 1.

In this construction, the CCT intervention generates an equal welfare improvement for all income classes. It is possible to modify it to ensure that lower income groups attain a higher welfare improvement, with an exception at the very top. Specifically, we can choose $\epsilon_i \in [0, \bar{\epsilon}_i], i =
1, ..., \( n - 1 \) such that \( 0 < \psi_i(\epsilon_i) < \psi_{i-1}(\epsilon_{i-1}) \) for all \( i = n - 1, n - 2, \ldots, 2 \). Now (31) requires

\[
(\pi_{n1} - \pi_{n0})\psi_n(\epsilon_n) = -\sum_{i=1}^{n-1} (\pi_{i1} - \pi_{i0})\psi_i(\epsilon_i)
\]

\[
= (\pi_{n1} - \pi_{n0})\psi_{n-1}(\epsilon_{n-1}) + \sum_{i=1}^{n-2} [G_{i1} - G_{i0}][\psi_{i+1}(\epsilon_{i+1}) - \psi_i(\epsilon_i)].
\] (33)

Since \( \psi_i(\epsilon_i) \) is decreasing in \( i \) by construction, the strong first order stochastic dominance property implies that \( (\pi_{n1} - \pi_{n0}) \) and the RHS of (33) are both positive. Hence the required value of \( \psi_n(\epsilon_n) \) is positive. If \( \epsilon_i, i = 1, \ldots, n - 1 \), are chosen sufficiently close to 0, this required value is close to 0. Then there exists \( \epsilon_n \in (0, \bar{\epsilon}_n) \) such that (33) holds.

However, it is also clear that this kind of CCT cannot be designed to generate redistribution across the entire income scale, as that would require \( \psi_i \) to be decreasing in \( i \) throughout, and stochastic dominance would then imply that the sign of the LHS of (31) is negative. Conversely it cannot be designed to be throughout regressive. But as shown, it is possible to construct it to ensure that every income class attains the same welfare improvement \( \eta > 0 \). This improvement \( \eta \) can be chosen by the policymaker from an interval \( (0, \hat{\eta}) \), where \( \hat{\eta} > 0 \) is determined by the status quo DCE and economic fundamentals. Among the latter, the discount factor \( \delta \) represents the extent to which a parent internalizes the utility of its child and succeeding generations of offspring. We prove in the appendix that if \( \delta \) is large enough, the scheme results in an ex post Pareto improvement, since parents’ valuation of the benefit of increased education among their descendants outweighs their own tax burden even if they themselves do not invest and avail of the subsidy.

**Proposition 3** Let a collection of economies with identical consumption utility function \( u \) and probability distributions \( F, G_0, G_1 \), but different parental discount factors \( \delta \in (0, 1) \) be given. For each corresponding DCE, consider CCTs \( \{t_{\delta,i}(\eta), s_{\delta,i}(\eta)\}_{i=1,...,n} \) that induce an interim Pareto improvement according to Proposition 2. Then there exist \( \hat{\delta} \in (0, 1) \) and \( \bar{\eta} > 0 \) such that for any \( \eta \in (0, \hat{\eta}) \) and \( \delta \in (\hat{\delta}, 1) \) the intervention also generates an ex post Pareto improvement, i.e., the welfare of every agent in the economy at every subsequent date is higher, irrespective of income or child’s learning ability.

### 3 Extensions

We provide an informal discussion of how the preceding results are modified when the model is extended in different directions.
3.1 Endogenous Labor Supply

A first extension of the baseline model allows labor supply to vary. Interpret $y \in Y$ as the wage rate available to a given household, and let households choose how many hours of labor they supply, together with the binary decision whether to invest in education or not. Consider for simplicity the case of paternalistic altruism. Then each household facing wage rate $y$ and education cost $\tilde{x}$ selects $e \in \{0,1\}$ and $l \geq 0$ to maximize

$$u(ly - e\tilde{x}) - d(l) + eV_1 + (1 - e)V_0$$

(34)

for strictly increasing and convex disutility of labor $d$ given $V_c \equiv \sum_{i=1}^{n} \pi_{ic}V(y_i)$. Here $V(y)$ denotes the benefit perceived by the parent from the child’s future when the latter would be able to earn a wage rate $y$, and we naturally assume that $V$ is strictly increasing.

The optimal investment strategy $e(y, \tilde{x})$ in this case is of the same threshold form as in the baseline model. Namely, if we define

$$v(y_i, \tilde{x}, e(y_i, \tilde{x})) \equiv \max_{l_i} \left[ u(l_i y_i - e\tilde{x}) - d(l_i) \right]$$

(35)

then a parent with wage rate $y_i$ who faces education cost $\tilde{x}$ will invest iff $\tilde{x} < x_i$, where threshold $x_i$ is defined by

$$v(y_i, x_i, 0) - v(y_i, x_i, 1) = V_1 - V_0.$$  

(36)

Parents with wage rate $y_i$ and cost $\tilde{x} = 0$ or cost $\tilde{x} \geq x_i$ have identical (indirect) utilities of consumption $v(y_i, 0, 1) = v(y_i, \tilde{x}, 0)$, while those with cost $\tilde{x} \in (0, x_i)$ consume less. In particular, from (35) and the Envelope Theorem, we have

$$\frac{\partial v(y_i, \tilde{x}, e(y_i, \tilde{x}))}{\partial \tilde{x}} = -u'(l(y_i, \tilde{x})y_i - \tilde{x}) < 0$$

for each $\tilde{x} \in (0, x_i)$.  

(37)

It follows that consumption utilities $v(y_i, \tilde{x}, e(y_i, \tilde{x}))$ are decreasing on $[0, x_i)$, jump back to $v(y_i, 0, 1)$, and then stay at this level. That is, they exhibit a non-monotonic pattern with respect to education cost $\tilde{x}$ just like in the baseline model. A variation of the baseline policy intervention can therefore be applied in order to create an interim Pareto improvement.

3.2 Continuous Education Choices

What if educational investments can be varied continuously, rather than being indivisible? CCTs are designed to subsidize only variations in education on the extensive margin rather than the intensive margin – i.e., parents are eligible for the subsidy provided their children are enrolled in school; the size of the subsidy does not vary with the extent of educational achievement.\footnote{Of course the extent of enrollment as measured by proportion of classes attended can also vary continuously. We refer to enrollment as the achievement of a minimum target for the proportion of classes attended, as commonly...}

It is
presumably for this reason that they are typically offered for enrollment of children in secondary schooling in countries with significant dropout rates in secondary but not primary schooling. So we consider an extension of our model consistent with non-universal enrollment in the status quo situation, and show that the CCT can continue to be designed on the basis of enrollment decisions.

Let the extent of education be described by a compact interval $E \equiv [0, \bar{e}]$ of the real line. Enrollment corresponds to a positive choice of $e$. Conditional on education $e \in E$, the distribution of earnings is given by a cdf $G_e$, where $e' > e$ implies $G_{e'}$ strongly first order stochastically dominates $G_e$. To simplify the exposition, we assume that $\tilde{V}(e) \equiv \int_Y V(y) dG_e(y)$ is a concave $C^2$ function with $0 < \frac{\partial \tilde{V}(e)}{\partial e} < \infty$ for all $e \in E$. Next, let $I(e; \tilde{x})$ denote the expenditure that must be incurred by a parent to procure education $e \geq 0$ for its child whose learning ability gives rise to a learning cost parameter $\tilde{x}$. The latter varies according to a continuous distribution with full support on $[0, \infty)$, similar to the preceding section. The function $I$ is strictly increasing and differentiable in both arguments. It satisfies $I(0; \tilde{x}) = 0$ for all $\tilde{x}$, and for any given $e \geq 0$ the marginal cost $\frac{\partial I(e; \tilde{x})}{\partial e}$ is increasing in $\tilde{x}$, zero at $\tilde{x} = 0$ and approaches $\infty$ as $\tilde{x} \to \infty$.

A parent with income $y$ and a child with learning cost $\tilde{x}$ then solves

$$\max_{0 \leq e' \leq \bar{e}} \left[ u(y - I(e'; \tilde{x})) + \tilde{V}(e') \right].$$

Let the corresponding policy function be $e'(y; \tilde{x})$.

Under these assumptions $x^*(y) > 0$ is well-defined as the solution for $x$ in the equation $u'(y) \frac{\partial I(0; x)}{\partial e} = \frac{\partial \tilde{V}(0)}{\partial e}$, and the optimal policy function takes the form $e'(y; \tilde{x}) = 0$ if $\tilde{x} \geq x^*(y)$ and positive otherwise. In other words, parents decide to acquire no education for their children if and only if their learning cost parameter is larger than a threshold $x^*(y)$. These ‘non-investors’ consume their entire earnings $y$ – just like those parents with the same income $y$ whose children have learning cost parameter $\tilde{x} = 0$. For those whose children have intermediate learning ability, parents spend a positive amount on education.

We thus have a similar non-monotone pattern of variation of parental consumption with their children’s learning costs as in the two-occupation case. Parents whose children do not enroll therefore consume more than parents earning the same whose children do enroll. The educational subsidy funded by the income tax in this group then redistributes consumption away from those consuming high amounts to those consuming less. Since these consumption variations arise from the ‘ability lottery’ of their children, the policy increases interim expected utilities of each income class.
3.3 Financial Bequests

In the baseline model educational investments constitute the sole means by which parents transfer wealth to their children. In practice parents have other means as well, such as leaving them financial bequests or physical assets. The simple logic then breaks down: a parent that does not invest in his or her child’s education owing to low learning ability of the latter could provide financial bequests instead. It no longer follows that education non-investors invest less when we aggregate across different forms of intergenerational transfers.

Consider the consequences of allowing parents to leave financial bequests besides investing in their children’s education. To simplify matters, suppose that the rate of return \((1 + r)\) on financial bequests is exogenously given, as in Becker and Tomes (1979) or Mookherjee and Ray (2010). To simplify the exposition, assume incomes are non-stochastic and depend only on occupation: \(w_c\) now denotes wage earnings in occupation \(c\) with \(w_1 > w_0\). The idiosyncratic education cost needed for working in the skilled occupation is again \(\tilde{x}\), that for the unskilled occupation equals zero. Parental altruism is paternalistic, where a parent with lifetime wealth \(W\) and education cost \(\tilde{x}\) chooses financial bequest \(b \geq 0\) and education investment \(e \in \{0, 1\}\) to maximize \(u(W - b - e\tilde{x}) + \delta V(W')\) where \(V\) is a strictly increasing and strictly concave function of the child’s future wealth \(W'\) which equals \((1 + r)b + ew_1 + (1 - e)w_0\).

The details of the analysis are provided in the working paper version (Mookherjee and Napel 2019). We highlight here the solutions for two ranges of parental wealths.

Case A. \(W\) sufficiently large: For \(W\) large enough, the parent will always make a financial bequest that is possibly supplemented by an education investment. The sum of expenditures on education and financial bequests is lowest – and parental consumption highest – for the most talented education cost type \(\tilde{x} = 0\). From there, total spending for the child increases in \(\tilde{x}\) until some threshold \(\tilde{x}_W^*\), and then it becomes optimal to transfer a constant amount of wealth purely via financial bequests.

Case B. \(W\) sufficiently small: Suppose \(W = w_0\), \(\delta(1 + r) \leq 1\) and \(V \equiv u\). Then the parent never makes a financial bequest. If however the child learning cost \(\tilde{x}\) is below a positive threshold level \(\tilde{x}_{w_0}^*\), the parent will invest in education.

Parents in case B behave exactly as described in previous sections and their consumption varies with cost \(\tilde{x}\) exactly as in Figure 1. So our previous arguments continue to apply for poor households in case B, who never make any financial bequests. Offering educational subsidies for them, funded by corresponding income taxes, would be interim Pareto improving. The model of Abbott et al.\(^{12}\) This corresponds to a globalized capital market where the savings of any given country leave the interest rate unaffected. Even if the interest rate depends on the supply of savings, a ‘neutralization’ policy allows policy-makers to ensure that the after-tax interest rate is unchanged.
(2019) calibrated to fit NLSY 1997 data, suggests that case A applies to the top 5% of the US population and case B applies to the bottom third. We speculate that the respective share of population described by case B is even bigger in most developing countries.

3.4 General equilibrium wage effects; non-stationary fiscal policy

Finally consider a setting where skilled and unskilled wages depend on the skill composition in the population. Then increases in skill composition induced by a CCT would lower the skill premium in wages: skilled wages would fall while unskilled wages would rise. This would lower educational investment incentives. Moreover, the outcome would lower the welfare of skilled households, so would not be Pareto improving. This necessitates further modification to the design of the CCT. In particular, it needs to be accompanied by an offsetting regressive change in fiscal policy which ‘neutralizes’ these GE effects, lowering taxes on high incomes and raising them on low incomes, so as to keep inter-occupation wage and welfare differences the same as in the status quo. In the working paper version (Mookherjee and Napel 2019), we consider the case of two occupations, non-stochastic income and non-paternalistic utility, and show that the CCT design can indeed be modified in this manner to ensure that a Pareto improvement results in which welfare of skilled and unskilled households within each generation rise by exactly the same extent. The extension also includes the case where the status quo involves a non-stationary fiscal policy, and the government is required to balance its budget at every date.

4 Related Literature

Our paper is related to literatures in development and occupational choice, public economics and macroeconomics. We discuss these in turn.

4.1 Development and Occupational Choice

The closest connection is with the literature on occupational choice with credit market imperfections. With few exceptions, this literature focuses on poverty dynamics under laissez faire, rather than normative properties of laissez faire or effects of fiscal policy. Mookherjee and Ray (2003) study a model which is a special case of the one we consider here, which abstracts from ability heterogeneity and fiscal policy interventions. In this framework Mookherjee and Ray (2008)  

compare properties (such as per capita output and social welfare corresponding to differing degrees of inequality aversion) of (suitably selected) steady states resulting from conditional and unconditional transfers. Their analysis is subject to a number of problems which we overcome in the current paper: by focusing on the long run they ignore impacts in the short run and the transition to a new steady state. They ignore ability heterogeneity and do not investigate the possibility of efficiency improvements resulting from CCTs.

The role of ability heterogeneity was investigated in an earlier paper of ours (Mookherjee and Napel 2007) on uniqueness and stability of steady states under laissez faire, in the presence of paternalistic altruism. However, welfare effects of fiscal policy were not addressed, so this paper is a natural complement of the earlier one. Fender and Wang (2003) incorporate ability heterogeneity in what is, essentially, a two-period model of occupational choice with credit rationing arising owing to moral hazard. Their model is relevant to higher education by young adults rather than education of children: there is no parental altruism; agents finance their own education and consumption utility is linear. By contrast our model focuses on investments in children by their parents, incorporates consumption smoothing preferences, transition dynamics and identifies a general and robust source of Pareto improvements resulting from CCTs.

Finally, D’Amato and Mookherjee (2013) investigate the efficiency role of a different policy instrument: public provision of education, rather than CCTs. They focus on a two-skill OLG model with paternalistic altruism, ability heterogeneity and missing financial markets. Similar to this paper, they show that Pareto improving interventions exist. However, they focus on a different policy instrument: public provision of education, where children receiving a public schooling are required to pay back to the government when they become adults. The nature of the efficiency improvement in that paper is also different, consisting of reducing misallocation of education between children in rich and poor families, while leaving unchanged the aggregate proportion educated. They additionally show the result is robust when education signals unobserved productivity of workers to employers.

4.2 Public Economics

Sinn (1995, 1996) and Varian (1980) evaluate incentive and insurance effects of social insurance provided by a progressive fiscal policy in a setting with ex ante representative households and missing credit and / or insurance markets. Interim or ex post Pareto improvements do not arise in

\[^{14}\text{They evaluate effects of public provision of education according to different methods of financing. Interventions that improve utilitarian welfare are shown to generally exist, but the tax burdens on those who remain uneducated make part of the population worse off. An exception arises when additional education investments prompt interest rates to increase so much (assuming there is no access to world capital markets) that this could dominate the direct effects for some parameter values.}\]
those settings. Subsequent literature in public economics has examined implications of redistributive tax distortions for education subsidies. For instance, Bovenberg and Jacobs (2005) argue in a static context without any borrowing constraints or income risk that redistributive taxes and education subsidies are ‘Siamese twins’: the latter are needed to counter the effects of the former in dulling educational incentives. Jacobs, Schindler, and Yang (2012) show the same result obtains when the model is extended to a context with uninsurable income risk. Unlike our paper, these arguments for educational subsidies arise from pre-existing income tax distortions, which disappear in the case of a laissez faire status quo. None of these models incorporate ability heterogeneity and missing credit markets, which create an efficiency role for educational subsidies in our model, even in the absence of any progressive income taxes.

4.3 Macroeconomics

Dynamic models of investment in physical and/or human capital which incorporate missing credit and insurance markets and agent heterogeneity have been studied in the literature on macroeconomics and fiscal policy. Most of these papers examine dynamic properties of competitive equilibria, and show that redistributive policies could raise aggregate output and welfare, but do not explore the possibility of Pareto improving fiscal policy. An exception is Bénabou (1996) who shows that collective financing of education can be ex post Pareto improving in a sufficiently patient society, similar to our Proposition 3.

Versions of these models have been calibrated to fit data of real economies in order to evaluate the welfare and macroeconomic effects of various fiscal policies in numerical simulations. These studies rely on specific functional forms for technology and preferences, and focus on aggregate measures of welfare. These papers leave open the question whether there may exist other policies which could have resulted in a Pareto improvement, or what the effects might be in economies with different preferences and technology. Our paper complements this literature by providing purely qualitative results concerning Pareto improving fiscal policies which apply irrespective of the specific welfare function, technology or preferences.

5 Concluding Observations

We have provided a theoretical argument for Pareto-superiority of cash transfers that condition on investments in child education, in a second-best environment with imperfect financial markets, and privately observed learning ability. Pareto-improvements arise when the CCTs are funded by

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income taxes imposed on the same income/occupational class, thereby avoiding redistribution across income groups. The results hold irrespective of specific assumptions on preferences or technology, initial conditions, general equilibrium effects, and incorporate short as well as long run effects. We have argued the results also apply irrespective of labor supply elasticity or investment divisibility. When parents have the additional option of leaving financial bequests to their children, subsidizing education is still desirable for parents in income classes who do not supplement education investments with financial bequests, which seems plausible for most poor households.

Normative discussions of CCTs usually argue that inefficient underinvestment in human capital is the relevant market failure and the key rationale for conditional transfers. Addressing this can, however, involve tension with other rationales for CCTs, e.g., using them to achieve pro-poor redistribution (see, e.g., [Das et al. 2004]). Our analysis identifies a market failure in education that differs from what is widely supposed among applied economists and policy-makers. It is unrelated to any notion of underinvestment or biased valuation of children’s education through their parents. Instead it relates to a failure of insurance markets, manifested in family consumptions that vary inefficiently with respect to ability realizations of children. This is a dimension in the welfare evaluation of CCTs which has been overlooked so far both in theoretical or empirical research. While the design we propose addresses directly an insurance rather than underinvestment problem, it nevertheless results in increased investments, per capita income and upward intergenerational mobility.

Comparatively little attention has also been devoted so far on how a CCT program should be financed. In practice it is typically financed by general income taxes, collected primarily from better-off households who do not qualify for the pertinent education subsidies. A CCT program is then explicitly redistributive, involving trade-offs between efficiency and distribution objectives, and potentially vulnerable to political opposition from better off households that end up paying for the program. We have argued there is an alternative funding mechanism for CCTs in which efficiency can be enhanced without adverse redistributive impacts, which could avoid such political opposition. So our paper may help promote consideration of a new form of CCT policy proposal.

Our analysis also casts a different perspective on arguments in the debate of universal basic income as an alternative to CCT schemes, by showing that any UBI scheme would be Pareto dominated by a CCT. This addresses two common criticisms of CCTs concerning narrow coverage and greater paternalism that have arisen in these debates. The ‘narrow coverage’ concern is an articulation of an ex post perspective, where some households end up ineligible for the subsidy. A similar concern could be raised about any insurance program, where some agents (often the vast majority) end up worse off ex post as a result of having paid premiums but not received any payout on account of not having experienced an accident. This indicates the need to adopt an ex ante or interim perspective instead. And most concerns of paternalism are based on a static
riskless perspective where there are no investment or insurance considerations at play. It therefore seems that the only credible argument against CCTs is that transfer conditionalities entail higher costs of monitoring and enforcement. But given CCT adoption and experience of many middle and low income developing countries, this does not seem to be very widely applicable. At any rate, if weak state capacity happens to be a binding constraint, such countries should aspire to adopt CCTs as they enhance their capacity over time.
Appendix – Proof of Proposition 3

It is sufficient to show that, for any realized income \( y_i \), parents who do not invest but pay tax \( t_{δ,i}(η) \) to finance the respective CCT, are still rendered better off when \( η \) is small and \( δ \) is large enough. The parents who invest only under the CCT reveal to be even better off. Those who already invested in status quo are rendered better off by subsidy \( s_{δ,i}(η) \) and higher dynastic welfare \( δ(B + W_0) \). We show that \( W_0 \) actually increases at an unbounded rate, as \( δ → 1 \), while non-investors’ losses of consumption utility are bounded.

Let us indicate variables and policy parameters that vary in \( δ \) with a corresponding subscript. Note that \( η \) fixes \( ε_{δ,i} = \psi_{δ,i}^{-1}(η) \) and investment thresholds \( x_{δ,i}(ε_{δ,i}) \), and implicitly induces bounds for \( \tilde{x}_{δ,i} \), which scales taxation and associated budget gains. Strong stochastic dominance of the skilled income distribution \( G_1 \) ensures that expected welfare of skilled households is strictly higher than that of unskilled households, independently of \( δ \). This bounds the benefits of investing in education, \( B^*_δ \), away from zero. Since \( u \) is increasing, thresholds \( x_{δ,i}^* \) are also bounded away from zero. Moreover, our conditions on \( u \) ensure \( x_{δ,i}^* < y_i \).

Raising the scale \( η \) of the CCT policy from status quo \( η = 0 \) lowers a non-investing parent’s consumption utility at a rate of
\[
\frac{∂}{∂η} \left[ u(y_i) - u(y_i - \psi_{δ,i}^{-1}(η)) \frac{F(\tilde{x}_{δ,i})}{1 - F(\tilde{x}_{δ,i})} \right] \bigg|_{η=0} = u'(y_i) \cdot \frac{F(x_{δ,i}^*)}{1 - F(x_{δ,i}^*)} \cdot \frac{∂ψ_{δ,i}^{-1}(0)}{∂η}.
\]

The first two factors are bounded, respectively, by \( u'(y_1) \) and \( F(y_1)/[1 - F(y_1)] \), noting that \( \tilde{x}_{δ,i} \) can be chosen arbitrarily close to \( x_{δ,i}^* \) as \( η → 0 \). To see that also \( \frac{∂ψ_{δ,i}^{-1}(0)}{∂η} \) is bounded as \( δ → 1 \), recall that
\[
ψ_{δ,i}(ε_i) = [U_{δ,i}(ε_i) + B^*_δ F(x_{δ,i}(ε_i))] - [U_{δ,i}^* + B^*_δ F(x_{δ,i}^*)]
\]
and
\[
U_{δ,i}(ε_i) = [1 - F(x_{δ,i}(ε_i))] u(y_i - ε_i \frac{F(\tilde{x}_{δ,i})}{1 - F(\tilde{x}_{δ,i})}) + F(x_{δ,i}(ε_i)) \mathbb{E}[u(y_i + ε_i - \tilde{x} \mid \tilde{x} ≤ x_{δ,i}(ε_i))]
\]
with \( ψ_{δ,i}(0) = 0 = ψ_{δ,i}^{-1}(0) \). So, using the Envelope Theorem,
\[
\frac{∂ψ_{δ,i}^{-1}(0)}{∂η} = \left[ \frac{∂ψ_{δ,i}(0)}{∂ε_i} \right]^{-1} = \left[ \frac{∂U_{δ,i}(0)}{∂ε_i} + B^*_δ f(x_{δ,i}^*) \cdot \frac{∂x_{δ,i}(0)}{∂ε_i} \right]^{-1}
\]
\[
= \left[ F(x_{δ,i}^*) \mathbb{E}[u'(y_i - \tilde{x} \mid \tilde{x} ≤ x_{δ,i}^*)] - [1 - F(x_{δ,i}^*)] u'(y_i) \frac{F(x_{δ,i}^*)}{1 - F(x_{δ,i}^*)} \right]^{-1}
\]
\[
= \frac{1}{F(x_{δ,i}^*)} \left[ \mathbb{E}[u'(y_i - \tilde{x} \mid \tilde{x} ≤ x_{δ,i}^*)] - u'(y_i) \right]^{-1} < L
\]
for some positive constant \( L \), given that \( x_{δ,i}^* \) is bounded away from zero.
The increase in the dynastic component of a non-investing parent’s welfare, \( \delta[W_{\delta,0} - W_{\delta,0}^*] \), is such that for every \( M < \infty \) there exist \( \delta \in (0, 1) \) so that for all \( \delta \in (\bar{\delta}, 1) \)

\[
\frac{\partial}{\partial \eta} \left\{ \frac{1}{1 - \delta} \left[ U_{\delta,0}(\psi_{\delta,i}^{-1}(\eta)) + F_{\delta,0}(\psi_{\delta,i}^{-1}(\eta))B_{\delta}^* \right] \right\} = \frac{1}{1 - \delta} \geq M. \tag{43}
\]

Combining (42) and (43), we can conclude that the total welfare change of non-investing parents with income \( y_i \) satisfies

\[
\frac{\partial}{\partial \eta} \left\{ u(y_i - \psi_{\delta,i}^{-1}(\eta)) \frac{F(\bar{x}_{\delta,i})}{1 - F(\bar{x}_{\delta,i})} + \delta W_{\delta,0}(\eta) \right\} - \left\{ u(y_i) - \delta W_{\delta,0}^* \right\} \bigg|_{\eta=0} \geq m \tag{44}
\]

for all \( \delta \in (\bar{\delta}, 1) \) for some \( m > 0 \). We can therefore choose \( \bar{\eta} > 0 \) such that each households’s ex post welfare change is positive for any \( \eta \in (0, \bar{\eta}) \) for every \( \delta \in (\bar{\delta}, 1) \).

References


