

Quiz 13

Answer the questions in the spaces provided. If you run out of room for an answer, continue on the back of the page.

Question:	1	2	Total
Points:	20	5	25
Score:			

Name: \_\_\_\_\_

1. Consider a system with three energy levels as described in the table below. Assume the system has Boltzmann-weighted probabilities ( $p(\epsilon) \propto e^{-\epsilon\beta}$ ).

$\epsilon$	$g$
0	1
$\epsilon_0$	1
$2\epsilon_0$	$\gamma$

- (a) (5 points) Write an expression for the partition function  $q$  as a function of energy, degeneracy, and temperature.

$q =$

- (b) (5 points) What is an expression for the average energy? This can be left as a (simplified) function of  $q$ .

$\langle \epsilon \rangle =$

- (c) (5 points) At what temperature will the probabilities of the first and third energy levels be the same (i.e.,  $p_1^* = p_3^*$ ).  $T$  will be a function of  $\epsilon_0$  and  $\gamma$ .

$T =$

- (d) (5 points) For  $\epsilon_0 = \ln(2)/\beta$  and  $\gamma = 2$ , compute the equilibrium probabilities of the three energy levels.

$p_1^* =$

$p_2^* =$

$p_3^* =$

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2. (5 points) For fun if you have time: What could Thomas as the teaching fellow for the course have done better?